

Measurement of sin2b

with charmonium decays and gluonic penguin decays

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- CP violation N(B \rightarrow f) ? N($\overline{B}\rightarrow\overline{f}$)
- Introduction: Standard Model CP violation & the CKM mechanism
- Testing the Standard Model: measurement of sin(2β) from charmonium K_s decays
- Looking for signs of new physics: measurement of sin(2β) from b→s penguin decays
- Comparison and summary



The Cabibbo-Kobayashi-Maskawa matrix

- In the Standard Model, the CKM matrix elements V_{ij} describe the electroweak coupling strength of the W to quarks
 - CKM mechanism introduces quark flavor mixing



- Complex phases in V_{ii} are the origin of SM CP violation

$$\frac{\overline{b}}{V_{ub}} \xrightarrow{W^+} \overline{u}$$

$$\frac{b}{V_{ub}} \xrightarrow{W^-} u$$

$$V_{ub}^* \xrightarrow{W^-} U$$

Transition amplitude violates CP if V_{ub} ? V_{ub} *, i.e. if V_{ub} has a non-zero phase



- The CKM matrix V_{ij} is unitary with 4 independent fundamental parameters (including 1 irreducible complex phase)
 - Magnitude of elements strongly ranked (leading to ~diagonal form)
 - Choice of overall complex phase arbitrary only V_{td} and V_{ub} have non-zero complex phases in Wolfenstein convention



– Measuring SM CP violation \rightarrow Measure complex phase of CKM elements

Visualizing the phase – the unitarity triangle

- Phases of CKM elements V_{td} and V_{ub} are related to CPV in SM
 - Visualization: **b** and **g** are two angles of a triangle.
 - Surface of triangle is proportional to amount of CPV introduced by CKM mechanism



Amplitude phases and observables CP violation

- How do complex phase affect decay rates
 - Only affects decays with >1 amplitude
 - − Decay rate $\propto |A|^2 \rightarrow$ phase of sole amplitude does not affect rate
- Consider case with 2 amplitudes with same initial and final state Decay rate $\propto |A_1 + A_2|^2$



Amplitude phases and observables CP violation

 Observable summed amplitude clearly depends on phase difference



Amplitude phases and observables CP violation

- Dependence on $\Delta \phi$ scales with amplitude ratio
 - Observation in practice requires amplitudes of comparable magnitude



Measuring the CKM phases from CP violation

- Decay rate of interfering amplitudes sensitive to phase difference
 - How disentangle weak phase from overall phase difference between amplitudes?
- Exploit that weak phase flips sign under CP transformation

- Look at decay rates for
$$B \rightarrow f$$
 and $\overline{B} \rightarrow \overline{f}$

 B^+

$$\begin{array}{c}
\begin{array}{c}
\begin{array}{c}
\begin{array}{c}
\begin{array}{c}
\end{array} \\
B^{-} & \overbrace{V_{ub}}^{V_{ub}} & \overbrace{\overline{c}}^{u} & \overbrace{i\overline{b}}^{0} & \overline{D}_{cp}^{0} \\
\hline \overline{u} & \overbrace{\overline{u}}^{v} & \overbrace{\overline{u}}^{v} & \overbrace{\overline{b}}^{v} & \overline{K}^{-} \\
\end{array} \\
\begin{array}{c}
\end{array} \\
A(B \to f) = |A_{B \to f}| \exp i(\mathbf{j}_{weak} + \mathbf{d}_{other}) \\
\hline A(\overline{B} \to \overline{f}) = |A_{B \to f}| \exp i(-\mathbf{j}_{weak} + \mathbf{d}_{other}) \\
\end{array}$$

 $u \xrightarrow{V_{cs}} \underbrace{\overset{c}{\overline{s}}}_{u} \operatorname{pr}_{u} \overset{c}{\operatorname{pr}}_{k} K^{+}$

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How the weak phase introduces observable CPV

• Effect of weak phase sign flip on interfering amplitudes

B→f







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• Effect of weak phase sign flip on interfering amplitudes





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A clean way to measure the CP angle β

- Find 2 interfering amplitudes with relative weak phase β
 - Requires CKM element V_{td}
 - V_{td} appears twice B^0 - B^0 mixing process



- Mixing process introduces a weak phase of 2β and a CP-invariant phase of $\pi/2$
- Find process with two interfering amplitudes: one *with* mixing and one *without*
 - $\begin{array}{l} & \mathbf{B} \rightarrow \mathbf{f} & \text{phase} = \phi_{\text{decay}} \\ & \mathbf{B} \rightarrow \mathbf{F} & \text{phase} = \phi_{\text{decay}} + \phi_{\text{mixing}} \end{array} \right\} \quad \mathbf{D}\mathbf{f} = \mathbf{f}_{\text{mixing}} \\ & \text{Final state } f \text{ must be CP eigenstate as both B and B must decay into it} \end{array}$

\sim The golden mode BO \rightarrow J/ ψ K_s

• An experimentally and theoretically clean CP eigenstate f_{CP} with no weak phase of its own is B⁰ \rightarrow J/ ψ K_s



• But mixing amplitude is decay time dependent



 $B^{0} \rightarrow \overline{B^{0}} \rightarrow f$ amplitude is decay time dependent

Interference and observable CPV is decay time dependent

Maximal CPV when amplitudes equal, around $t = 2p_{B}Dm_{d} \sim = 2t_{B}$

\sim The golden mode B0 \rightarrow J/ ψ K_s

• When mixed and unmixed amplitude are of equal magnitude



• Working out the more general case gives

$$\begin{split} A_{CP}(f;t) &= \sin(2b)\sin(\Delta m_d t) & \text{Generalized for any decay time} \\ A_{CP}(f;t) &= \frac{2 \operatorname{Im} \lambda_f^{*}}{1 + |\lambda_f|^2} \sin \Delta m_d t - \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \cos \Delta m_d t \\ I_f &= e^{-i2b} \frac{A(\overline{B}^0 \to f)}{A(B^0 \to f)} \end{split} \quad \begin{array}{c} \text{Generalized for any decay time} \\ \text{Generalized for an$$



• What will it look like?



- Why is it 'golden'?
 - Virtually free of Standard Model pollution.
 Next largest decay amplitude for B⁰ → J/ψ K_s has same weak phase as leading diagram.
 - Theoretical uncertainty on procedure of order 1%



The PEP-II B factory – specifications

- Produces B⁰B⁰ and B⁺B⁻ pairs via Y(4s) resonance (10.58 GeV)
- Asymmetric beam energies
 - Low energy beam 3.1 GeV
 - High energy beam 9.0 GeV
- Boost separates B and B and allows measurement of B⁰ life times
- Clean environment

- ~28% of all hadronic interactions is BB



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The PEP-II B factory – performance

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- PEP-II top lumi: 9.2x10³³ cm⁻²s⁻¹
 - ~10 BB pairs per second
- Continuous 'trickle' injection
 - Reduces data taking interruption for 'top offs'



- Integrated luminosity
 - PEP-II delivered: 254 fb⁻¹
 - BaBar recorded: 244 fb⁻¹
 - Most analyses use 205fb⁻¹ of on-peak data (227M *BB* pairs)



- Outstanding K[±] ID
- Precision tracking (Δt measurement)
- High resolution calorimeter
- Data collection efficiency >95%



SVT: 5 layers double-sided Si.

DCH: 40 layers in 10 superlayers, axial and stereo.

DIRC: Array of precisely machined quartz bars. .

EMC: Crystal calorimeter (CsI(TI)) Very good energy resolution. Electron ID, π^0 and γ reco.

IFR: Layers of RPCs within iron. Muon and neutral hadron (K_1)



Electromagnetic





Cerenkov Particle Identification system

• Cerenkov light in quartz

 Transmitted by internal reflection Detector Quartz Surface Rings projected in standoff box Thin (in X_0) in detection volume, n_s yet precise... Side View 154 -15 1 · Beat additions of Wouter Verkerke, NIKHEF

Selecting B decays for CP analysis

- Principal event selection variables
 - Exploit kinematic constraints from beam energies
 - Beam energy substituted mass has better resolution than invariant mass

Energy-substituted mass

Energy difference

Event shape



Collecting CP event samples



Measuring (time dependent) CP asymmetries

- Need to measure $N(B^{\circ} \rightarrow f)$ and $N(\overline{B^{\circ}} \rightarrow f)$
 - So need to know initial flavor of decay. Exploit fact that $B^{0}\overline{B^{0}}$ system evolves coherently → Flavor of 'other B' tags flavor of B0 → f at t=0
 - Measure N(Y(4s) $\rightarrow \overline{B^0}(\rightarrow f_{flav}) \xrightarrow{B^0}(\rightarrow f_{CP})$), N(Y(4s) $\rightarrow \overline{B^0}(\rightarrow f_{flav}) \xrightarrow{B^0}(\rightarrow f_{CP})$) and decay time difference





Determine flavor of $B_{tag} \equiv B_{CP}(\Delta t=0)$ from partial decay products

Leptons : Cleanest tag. Correct >95%



Kaons :

Second best. Correct 80-90%

 $\begin{array}{c} W^{-} \\ b \\ \hline \\ W^{+} \\ W^{+} \\ d \end{array} \begin{array}{c} S \\ \overline{u} \\ W^{+} \\ W^{-} \\ W^{-} \\ \overline{d} \end{array} \begin{array}{c} W^{+} \\ \overline{c} \\ W^{-} \\ \overline{c} \\ W^{-} \\ \overline{d} \end{array} \begin{array}{c} \overline{s} \\ \overline{s} \\ \overline{d} \end{array} \right] K^{+}$

Full tagging algorithm combines all in neural network

Four categories based on particle content and NN output.

Tagging performance



Putting it all together: $sin(2\beta)$ from $B^0 \rightarrow J/\psi K_s$



- Effect of detector imperfections
 - Dilution of A_{CP} amplitude due imperfect tagging
 - Blurring of A_{CP} sine wave due to finite At resolution

Measurement method: tagging efficiency & time resolution

- Flavor tagging performance and decay tim<u>e resolution are</u> measured from sample of Y(4s) → B⁰(f_{flav}) B⁰(f_{flav}) events
 - Determine flavor of 1st B with usual flavor tagging algorithm
 - Determine flavor of 2nd B from explicit reconstruction in flavor eigenstate



Combined golden modes result for sin2b



 $sin_{2}B = 0.722 \pm 0.040 (stat) \pm 0.023 (sys)$ No evidence for additional CPV in decay $|?|=0.950\pm0.031(stat.)\pm0.013$

 $(2002 \text{ measurement:} \sin(2\beta) = 0.741 \pm 0.067 \pm 0.034)$

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Standard Model interpretation

4-fold ambiguity because we measure sin(2b), not b



Method as in Höcker et al, Eur.Phys.J.C21:225-259,2001





Measurement of sin(2β) now real precision test of Standard Model

Results are still statistics dominated and will be for the foreseeable future

Four-fold ambiguity because we measure $sin(2\beta)$, not β

 $\beta \rightarrow -\beta$, $\beta \rightarrow \beta + \pi$

We can eliminate 1^{st} ambiguity if we also know $\cos(2\beta)$ More precisely, we only need to know the sign of $\cos(2b)$

Measuring cos(2ß) with B⁰? J/? $K^{*0}(K_{s}p^{0})$

- Decay $B^0 \rightarrow J/? K^{*0}(K_s \pi^0)$ is one of charmonium samples used to measure sin(2 β)
 - But it is a scalar → vector vector decay, so there are 3 decay amplitudes with different polarizations
- Composition in terms of amplitudes (in transversity basis)



 In sin2β measurement we account for this by using a weighted average of CP eigenvalues of +0.51

Measuring cos(2ß) with B⁰? J/? $K^{*0}(K_{s}p^{0})$

- But if you also include *angular information* from the decay products you can disentangle the 3 amplitudes
 - Many extra terms in time-dependent decay rate, including two that are proportional to cos(2B) :

 $g(\vec{w}, \mathbf{A}(t), \sin 2\mathbf{b}, \cos 2\mathbf{b}) = \dots$

 $\pm e^{-\Gamma|\Delta t|} f_4(\vec{w}) |A_T| |A_{\parallel}| \cos(d_T - d_{\parallel}) \cos(2b) \sin(\Delta m \Delta t)$

 $\pm e^{-\Gamma|\Delta t|} f_6(\vec{w}) |A_T| |A_0| \cos(d_T - d_0) \cos(2b) \sin(\Delta m \Delta t)$

decay angles:

 $\vec{w} = (\cos(\boldsymbol{q}_{K^*}), \cos(\boldsymbol{q}_{tr}), \boldsymbol{f}_{tr})$

 $A_{T} = |A_{T}|e^{id_{T}} \text{ (CP odd)}$ $A_{0} = |A_{0}|e^{id_{0}} \text{ (CP even)}$ $A_{\parallel} = |A_{\parallel}|e^{id_{\parallel}} \text{ (CP even)}$

Measuring cos(2ß) with B⁰? J/?K^{*0}(K_sp⁰)

- We know many of the amplitudes, phase differences
 - From measurement of B[±]? J/ ψ K^{*}[±] and B⁰? J/ ψ K^{*0} (K⁺ π ⁻) using time-integrated angular analysis



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Measuring cos(2ß) with B⁰? J/?K^{*0}(K_sp⁰)

- We know many of the amplitudes, phase differences
 - From measurement of B[±]? J/ ψ K^{*±} and B⁰? J/ ψ K^{*0} (K⁺ π ⁻) using time-integrated angular analysis

PROBLEM!

We don't know the sign of the phase difference, so we can only measure cos(2β) **except for its sign**

But to break the ambiguity in b we precisely *need the sign!*

Amplitude phase differences (with 2-fold ambiguity) $d_{\parallel} - d_0 = 2.729 \pm 0.0101 \pm 0.052$ $d_T - d_0 = 0.184 \pm 0.070 \pm 0.046$ ion 2" $d_{\parallel} - d_0 = -2.729 \pm 0.0101 \pm 0.052$ $d_T - d_0 = 2.958 \pm 0.070 \pm 0.046$

Plug into time dependent cross

 $\pm \mathrm{e}^{-\Gamma|\Delta t|} f_4(\vec{w}) |A_T| |A_{\parallel}| \cos(\mathbf{d}_T - \mathbf{d}_{\parallel}) \cos(2\mathbf{b}) \sin(\Delta m \Delta t)$

 $\pm e^{-\Gamma|\Delta t|} f_6(\vec{w}) |A_T| |A_0| \cos(d_T - d_0) \cos(2b) \sin(\Delta m \Delta t)$

Measuring $cos(2\beta)$ with B⁰? J/? K^{*0}(K_sp⁰)

- Solution: find a new way to measure the sign of the phase differences $\delta_{\prime\prime}-\delta_{_0}$ and $\delta_{_T}-\delta_{_0}$

- Central idea: include (K π) S-wave in angular analysis 'non-resonant events': $A_s = |A_s|e^{id_s}$



- Extra terms due to interference of S-wave and P-wave contributions to K π final state and help solve the ambiguity $\pm f_8(?) |A_{\parallel}| |A_s| \cos(d_{\parallel} - d_s) \dots \pm f_{10}(?) |A_0| |A_s| \cos(d_s - d_0) \dots \pm f_9(?) |A_T| |A_s| \cos(d_T - d_s) \dots$



• Why it works: Phase difference $\delta_s - \delta_0$ has special property as consequence of Wigner causality:



cos(2ß) with B⁰? J/?K^{*0}(K_sp⁰) – result

• $\cos(2\beta)$ from 104 tagged B⁰? $J/\psi(K_s\pi^0)^{*0}$ decays with floating sin(2ß) with sin(2ß) fixed to 0.731

 $\cos(2\beta) = 3.32^{+0.76}_{-0.96}(stat.) \pm 0.27(syst.)$ $\sin(2\beta) = -0.1 \pm 0.57$

 $\cos(2\beta) = 3.32^{+0.76}_{-0.96}(stat.) \pm 0.27(syst.) \qquad \cos(2\beta) = 2.72^{+0.50}_{-0.79}(stat.) \pm 0.27(syst.)$

- Now quantify probability that sign of $cos(2\beta) > 0$
 - Use MC approach to include non-Gaussian effects





Standard Model interpretation



Measurement of sin(2β) now real precision test of Standard Model

Results are still statistics dominated and will be for the foreseeable future

Solutions 2 & 4 excluded at 86.6% CL

Method as in Höcker et al, Eur.Phys.J.C21:225-259,2001

Switching from charmonium to penguin modes

- Golden mode B0 \rightarrow J/ ψ K_s now precision measurement of CKM CPV
 - But CPV also a good place to look for signs of new physics
 - 'New Physics' couplings are expected to have non-zero phases, and may cause deviations in measured CPV
- Good place to look for new physics are loop diagrams
 - Loop diagrams are dominated by heavy particles in the loop → contribution of new physics may be non-negligible
 - Look at decay modes where loop diagram is leading order: $b \rightarrow s$ penguins



Switching from charmonium to penguin modes

- Measurement works otherwise as usual
 - Interfere decay amplitude with mixing + decay amplitude
 - Also works with several other decay amplitudes ($\eta' K^0$, $f^0 K^0$,...)



- Leading order SM for CPV is same as golden modes
 - But not all modes are as clean as $B^0 \rightarrow J/\psi K_s$ golden mode, so
 - Watch for other SM decay amplitudes that contribute, e.g.

$$\overline{B}^{0} \begin{cases} b & \downarrow & \downarrow & \downarrow \\ \overline{d} &$$

But highly suppressed as $|V_{ub}|$ tiny Wouter Verkerke, NIKHEF

Penguin olympia – ranking channels by SM pollution



Note that within QCD Factorization these uncertainties turn out to be much smaller !

 $\propto V_{\mu}V_{\nu}^{*}$

Selecting penguin decays – Experimental issues

- From an experimental point of view, penguin decays are more difficult to select
 - Signal branching fraction O(20) times smaller
 - Particle identification more challenging (high- $p K^{\pm} PID vs I^{\pm} PID$)
- Basic fit strategy same as for $J/\psi K_s$ except
 - Strong DIRC Particle ID to separate Cherenkov PID performance pions from kaons
 - Event shape monomials (L0,L2), and B kinematics optimally combined in Multivariate Analyzer [MVA]
 - Neural Network (NN) or Fisher Discriminant
 - 6-dimensional ML fit using

 (1) beam-energy substituted B mass (m_{ES}),
 (2) B-energy difference (ΔE),
 (3) the resonance mass,
 - (4) the resonance decay angle,
 - (5) the Multivariate Analyzer, and (6) Δt



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hep-ex/0502019

Selection of 'golden penguin mode' $B^0 \rightarrow f K^0$

- Modes with K_{S} and K_{L} are both reconstructed





Plots shown are 'signal enhanced' through a cut on the likelihood on the dimensions that are not shown, and have a lower signal event count

CP analysis of 'golden penguin mode' $B^0 \rightarrow f K^0$



Reaching for more statistics – $B^0 \rightarrow f K^0$ revisited

- Analysis does not require that ss decays through φ resonance, it works with non-resonant K⁺K⁻ as well
 - 85% of KK is non-resonant can select clean and high statistics sample
 - But not 'golden' due to possible additional SM contribution with ss popping



- But need to understand CP eigenvalue of K+K-K_s:
 - $-\phi$ has well defined CP eigenvalue of +1,
 - CP of non-resonant KK depends angular momentum L of KK pair
- Perform partial wave analysis
 - Estimate fraction of S wave (CP even) and P wave (CP odd) and calculate average CP eigenvalue from fitted composition
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CP analysis of B \rightarrow K⁺K⁻ K_S

• Result of angular analysis

$$f_{CP-\text{even}} = \frac{A_s^2}{A_s^2 + A_p^2} = 0.89 \pm 0.08 \pm 0.06$$

 Result consistent with cross check using iso-spin analysis (Belle)

$$f_{CP\text{-even}} = \frac{2\Gamma(B^+ \to K^+ K_S^- K_S^-)}{\Gamma(B^0 \to K^+ K^- K^0)} = 0.75 \pm 0.11$$

• Result of time dependent CP fit $S_{K^+K^-K_S^0} = -0.42 \pm 0.17 \pm 0.04$ $C_{K^+K^-K_S^0} = +0.10 \pm 0.14 \pm 0.06$

$$\eta_{f} \times S_{K+K-KS} / (2f_{CP-even} - 1)] = +0.55 \pm 0.22 \pm 0.04 \pm 0.11 \\ (stat) \quad (syst) \quad (f_{CP-even} - 1) = 0$$





hep-ex/0502017 hep-ex/0406040 The Silver penguin modes: $B^0 \rightarrow \eta' K_S \& B^0 \rightarrow f_0 K_S$

 $B^{0} \rightarrow \eta' K_{S}$

- Large statistics mode BR($B^0 \rightarrow h' K^0$) ~ 65.2×10⁻⁶ BR($B^0 \rightarrow h'_{rec} K^0_s$)~14.9×10⁻⁶
- Reconstruct many modes



Fit finds 819 ± 38 events

 $B^{0} \rightarrow f_{0}(980)K_{S}$

- Modest statistics mode BR($B^0 \rightarrow f_0(980)K_S^0$) ~ 6.0×10⁻⁶
- CP analysis more difficult
 - Requires thorough estimate of *CP* dilution due to interference in $BO \rightarrow p + p K_s$ Dalitz plot



Fit finds 152 ± 19 events

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The Silver penguin modes: $B^0 \rightarrow \eta' K_s \& B^0 \rightarrow f_0 K_s$

 $B^0 \rightarrow \eta' K_S$ $\eta_{\phi K0} \times \frac{S_{h'K_{S}^{0}}}{S_{h'K_{S}^{0}}} = +0.27 \pm 0.14 \pm 0.03$ $C_{h'K_c^0} = -0.21 \pm 0.10 \pm 0.03$

sin2**b** [cc] @ 3.0o

 $\eta_{\phi KO} \times \frac{S_{f_0 K_S^0}}{S_{f_0 K_S^0}} = +0.95 + 0.32 \pm 0.10$ $C_{f_0K_0^0} = -0.24 \pm 0.31 \pm 0.15$ sin2**b** [cc] @ 0.6σ 35 30 BABAR 25 B⁰ Tags 20 15





 $B^0 \rightarrow f_0(980)K_s$

hep-ex/0503018

The bronze penguin modes: $B^0 \rightarrow \omega K_s$ (New!)

• Modest statistics mode (BF $\approx 5 \times 10^{-6}$)



sin2b [cc] @ 0.7o



The bronze penguin modes: $B^0 \rightarrow \pi_0 K_S$

- Experimentally challenging! Construct decay vertex, decay time without tracks from primary vertex
 - Use beam line as constraint
 - Use only K_S decays with at least 4 hits in the silicon tracker to obtain required precision, ~60% meets requirements





More vertexing exercises – $B^0 \rightarrow K_S K_S K_S$

- But wait! If you can vertex $B^0 \rightarrow \pi^0 K_s$ with sufficient precision for a time dependent CP fit, then you can also analyze $B^0 \rightarrow K_s K_s K_s$
 - Average Ks momentum lower than in $\mathbf{p}^{\rho}K_{s'}$ larger fraction of events will have SVT hits
- Decay $B^0 \rightarrow K_S K_S K_S$ is 'golden' penguin – little SM pollution expected



Result consistent with SM

 $\eta_{\text{KO}} \times S = +0.71 \pm_{0.32}^{0.38} \pm 0.04$ $C = -0.34 \pm_{0.25}^{0.28} \pm 0.05$





Sin2b from $b \rightarrow$ s penguins – summary of BaBar results

- None if the *individual* results (except perhaps η'K_s) has a sizeable discrepancy with SM
 - But penguin average 2.8 away from (cc)s value...
 - Note that new physics will generally have different effect on modes – averaging not necessarily sensible...



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sin2b from b \rightarrow s penguins – World averages

- And the discrepancy becomes more significant in a BaBar/Belle average: 3.7σ
 - But note that uncertainty due to sub-leading SM contributions are ignored in this discrepancy statement
 - What is SM prediction for $sin(2\beta)$ various penguin modes?



Average(s-penguin) $S = 0.43 \pm 0.07$

Average(s-penguin) C = -0.021 ± 0.05

Various approaches to predict SM value of $sin(2\beta)_{peng}$

	'Gold'	'Bronze'
	$\Delta S(\phi K_S)$	$\Delta S(\pi^0 K_S)$
 Naive approach Calculate relative importance of 'polluting terms' using powers of λ, ignore strong phase differences Easy, but may not be good enough (for all modes) 	~0.06	~0.3
[Kirkby,Nir, Phys. Lett. B592 (PDG review)] [Hoecker, hep-ex/0410069]		
	0.025	0.13
 Best limits, but results dependent on models and model assumptions (e.g. QCD factorization) 	±0.012	±0.07
 Some models have problems predicting known BFs [Beneke, Buchalla, Neubert, Sachrajda, NPB591] [Buras, Fleischer, Recksiegel, Schwab, NPB697] [Ciuchini at al., hep-ph/0407073] 	±0.01	
Flavor symmetry	~0.3	~0.2
 Relate hadronic processes in b→dqq (tree dominated) and b→sqq (penguin dominated) 		
 Assumes SU(3) flavor symmetry, but no other model assumptions 		
 Limits not yet very good. Need to measure many suppressed BF, but will improve over time 		
[Grossman, Isidori, Worah, Phys Rev D58] [Gronau, Grossman, Rosner, Phys.Lett.B579] [Grossman, Liget, Nir, Quinn, Phys Rev D68] [Gronau, Rosner, Zupan, Phys.Lett.B596] [Gronau, Rosner, Phys.Lett. B564] [Chiang,Gronau,Rosner,Suprun, Phys.Rev.D70]		



- Precise measurement of sin(2 β) from charmonium K_{S} events

 $sin2\beta_{ccs} = 0.722 \pm 0.040 \text{ (stat)} \pm 0.023 \text{ (sys)}$

• Measurement of $sin(2\beta)$ from b \rightarrow s penguin decays

 $\langle \sin 2\beta \rangle_{peng} = 0.45 \pm 0.09$

- Belle/BaBar combined results show an apparent discrepancy of 3.7σ between these results
 - Present challenge to theorists and experimentalists: Is the apparent discrepancy real?