



Why three generations of particles?

Why is there no antimatter?

Why is an atom electric neutral?



Re

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Recap: Broken Symmetry and Unobservables: Parity

Before 1956 physicists were <u>convinced</u> that the laws of nature were left-right symmetric. Strange?

A "gedanken" experiment: consider two perfectly mirror symmetric cars:





What happens in case the ignition mechanism uses, say, $Co^{60} \beta$ decay?



Recap: Broken Symmetry and Unobservables: CP Violation



Compare $K_L^0 \to \pi^+ e^- \bar{\nu}$ to $K_L^0 \to \pi^- e^+ \nu$

Compare the charge of the most abundantly produced electron with that of the electrons in your body: If opposite: matter If equal: anti-matter



Recap: Weak interaction in three Flavour Generations

- Weak Interaction is 100% parity violating.
 - Wolfgang Pauli: "I cannot believe God is a weak left-hander."
- Implement an SU(2)_L symmetry for *massless* particles:

$$\mathcal{L}_W = \frac{g}{\sqrt{2}} u'_L \gamma_\mu W^\mu d'_L \qquad x3!$$

- Flavour universality: *identical interactions* in three generations.
 - In fact: how to distinguish a massless d' quark from s' quark?



• What happens when particles acquire mass?





Recap: Flavour Universality in very Early Universe

- Quark and lepton generations interact identically
 - No difference between particles of different generation?
 - No matter antimatter asymmetry (CP Violation)?



- Universality violation: Higgs !
 - Higgs coupling is *not universal*, and mixes generations
 - Complex couplings: allows for CP Violation!





Recap: Flavour Universality

• Weak charged current interaction: $(i \leftrightarrow i)$



- Universality violation: Higgs ! $(i \leftrightarrow j)$
 - Higgs coupling is not universal, and mixes generations
 - Complex couplings: allows for CP Violation!





Recap: Flavour Universality \rightarrow Symmetry Breaking

• Weak charged current interaction: $(i \leftrightarrow i)$





Recap: Flavour Universality \rightarrow Symmetry Breaking \rightarrow Flavour Mixing \ast

• Weak charged current interaction: $(i \leftrightarrow j)$







Recap: Flavour Universality –

Weak charged current interaction:

 d^m

 $V = S^{m}$

S^m Vuc

 b^m

+m

- Weak interactions mixes the generations of *mass eigenstates*.
- Complex couplings V_{ij} allow for CP violating phenomena.

 \mathbf{N}

• At least 3 generations required!

• Higgs: redefines quark states in mass eigenstates:





Aixing 9

• CKM in terms of *phases*:

$$V_{CKM} = \begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ -|V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}|e^{-i\beta} & -|V_{ts}|e^{i\beta_s} & |V_{tb}| \end{pmatrix}$$

Triangle in the complex plane:
$$V_{CKM}^{\dagger} V_{CKM} = 1$$

$$V_{CKM} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

Triangle in the complex plane:
$$V_{CKM} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

Triangle in the complex plane:
$$V_{CKM} = \begin{pmatrix} V_{td} | e^{-i\beta} & V_{tb} | e^{-i\beta}$$

2001

Beauty particles:Timedependent *CP* violation in *B*⁰ meson decays BaBar and Belle collaborations

2004

Beauty particles: Timeintegrated *CP* violation in *B*⁰ meson decays BaBar and Belle collaborations

2013

Beauty-strange particles: Time-integrated *CP* violation in *B*⁰_s meson decays LHCb collaboration

<u>2020</u>

Beauty-strange particles: Time-dependent *CP* violation in *B*⁰_s meson decays LHCb collaboration

TODAY

<u>1964</u>

Strange particles: CP violation in K meson decays J. W. Cronin, V. L. Fitch et al.

<u>1999</u>, <u>2001</u> Strange particles: *CP* violation in decay KTeV and NA48 collaborations

2012 Beauty particles: CP violation in B⁺ meson decays LHCb collaboration

2019

Charm particles: CP violation in D⁰ meson decays LHCb collaboration

Recap: CP violation vs matter – antimatter asymmetry

• To explain the absence of antimatter in the universe *requires* a primordial baryon asymmetry of: $\frac{\Delta n_B}{n} \approx 10^{-10}$





- Jarlskog criterion (1987) for amount of CP violation in SM: $det[M_u M_u^{\dagger}, M_d M_d^{\dagger}] = 2 i J (m_t^2 - m_c^2) (m_c^2 - m_u^2) (m_u^2 - m_t^2)$ $\times (m_b^2 - m_s^2) (m_s^2 - m_d^2) (m_d^2 - m_b^2)$ From CKM: $A_{CP}/T_c^{12} \approx 10^{-20}$ \rightarrow Too small
- Explanation requires existence of **new massive** particles.



Contents:

- 1. CP Violation
 - a) Discrete Symmetries
 - b) CP Violation in the Standard Model
 - c) Jarlskog Invariant and Baryogenesis

2. B-Mixing

- a) CP violation and Interference
- b) B-mixing and time dependent CP violation
- c) Experimental Aspects: LHC vs B-factory

3. B-Decays

- a) Effective Hamiltonian
- b) Lepton Flavour Non-Universality



CP violation: a quantum interference experiment

- Quantum process with two amplitudes A_1 and A_2 :
 - Eg.: $A_1 = B^0 \rightarrow J/\psi K_s$ and $A_2 = B^0 \rightarrow \overline{B^0} \rightarrow J/\psi K_s$



 $|A_1| = |\overline{A_1}|, |A_2| = |\overline{A_2}|,$ but $|A_1 + A_2| \neq |\overline{A_1 + A_2}|$

CP violation: a quantum interference experiment

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$$|A_1| = |A_1|, |A_2| = |A_2|,$$

but $|A_1 + A_2| \neq |\overline{A_1 + A_2}|$

Weak phase from CKM: $e^{-i2\beta} \rightarrow e^{i2\beta}$ Strong phase from mixing process: $e^{i\pi} \rightarrow e^{i\pi}$

CP violation: a quantum interference

 $\mathcal{A}_{J/\psi K^0_{\mathrm{S}}}(t) = \frac{1}{\Gamma(\overline{B}^0(t) \to J/\psi K^0_{\mathrm{S}}) + \Gamma(B^0(t) \to J/\psi K^0_{\mathrm{S}})}$ $= S_{J/\psi K^0_{\mathrm{S}}} \sin(\Delta m_d t) - C_{J/\psi K^0_{\mathrm{S}}} \cos(\Delta m_d t).$



• Eg.:
$$A_1 = B^0 \rightarrow J/\psi K_s$$
 and $A_2 = B^0 \rightarrow \overline{B^0} \rightarrow J/\psi K_s$

$$A_{1} \bigvee_{i} A_{2} \bigvee_{i} (a,c,t) \to V_{k}} \int_{a}^{J/\psi} A = A_{1} + A_{2}e^{i\phi}e^{i\delta} \qquad \bar{A} = A_{1} + A_{2}e^{-i\phi}e^{i\delta}$$

$$|A|^{2} = |A_{1}|^{2} + |A_{2}|^{2} + A_{1}A_{2}(e^{i\phi}e^{i\delta} + e^{-i\phi}e^{-i\delta})$$

$$|\bar{A}|^{2} = |A_{1}|^{2} + |A_{2}|^{2} + A_{1}A_{2}(e^{-i\phi}e^{i\delta} + e^{i\phi}e^{-i\delta})$$

$$|A|^{2} - |\bar{A}|^{2} = 4A_{1}A_{2}\sin\phi\sin\delta$$

$$A_{1} \bigvee_{a,s} \int_{a,s} A_{1} \bigvee_{a,s} \bigvee_{a,s} \int_{a,s} A_{1} \bigvee_{a,s} \bigvee_{a,s} \int_{a,s} A_{1} \bigvee_{a,s} \bigvee$$

 $\overline{B^0}_{\textcircled{0}}$

 B^0

 A_2

$$|A_{1}| = |\overline{A_{1}}|, |A_{2}| = |\overline{A_{2}}|,$$

but $|A_{1} + A_{2}| \neq |\overline{A_{1}} + A_{2}|$

 CP violation is a pure quantum interference effect.





2013

- Thought: Assuming CPT symmetry, CP violation imp<mark>lies & guap</mark>
 - Quantum interference $\leftarrow \rightarrow$ arrow of time?

Three types of observable CP violation



Observed CP violation in "Mixing", "Decay", "Induced"

B ⁰ Mixing induced	I CPV CPV in I	B ^o decay CPV ir	B _s decay B _s Mixing	induced CPV
2001 Beauty particles:Tim dependent <i>CP</i> violat in <i>B</i> ⁰ meson decays BaBar and Belle collaborations	ne- tion <u>2004</u> Beauty partie integrated <i>Cl</i> <i>B</i> ⁰ meson de BaBar and Be collaboration	2013cles: Time- P violation in ecaysBeauty-str Time-integra violation in decays LHCb collation	range particles: grated <i>CP</i> n <i>B</i> ⁰ _s meson boration	nge particles: dent <i>CP</i> <i>B</i> ⁰ meson oration
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CPV in K ⁰ mixing	CPV in K decay	CPV in B⁺ de	Primarily CPV in	D ⁰ decay

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Three types of observable CP violation

- a) "indirect" CP Violation: 1964 (CCFT) • $\operatorname{Prob}(K^0 \to \overline{K^0}) \neq \operatorname{Prob}(\overline{K^0} \to K^0)$ $|\varepsilon| = (2.228 \pm 0.011) \times 10^{-3}$ (PDG)
 - Also called: CPV in mixing



b) (direct// (D) vieletiere, 1000 (NIA 40 0 1/Te)/).

All CP violation processes result from quantum interference including three generations of fermions.

- **c) "mixing induced"** *CP* violation: 2001 (Belle & Babar):
- Also: *CPV in interference of mixing and decay* $sin 2\beta = 0.682 \pm 0.019$ (PDG)



Whisky: Three types of Flavour Violation...

3. "Mixing induced" 1. "In Mixing" 2. "Direct" **Blended** <u>"WTF?"</u> **Single Malt** Moonshine (Caol IIa) (Chivas Regal) CAOL ILA SADLER'S AGED 12 YEARS PEAKY BLINDER Moonshine lery Port Ashair Isle of Is LIMITED EDITION WHITE GRAIN SPIRIT 70cLe 40%vol

→ Interference experiments lead to interesting effects! (Constructive or destructive??)

<u>Type-1</u>: CP violation *in mixing*: $a_{SL}(B_d)$ en $a_{SL}(B_s)$

• Interfere *dispersive* and *absorptive* amplitudes ("indirect"):



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<u>Type-2</u>: CP violation in *decay*: $B_d^0 \to K\pi$ and $B_s^0 \to K\pi$



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A story on darts and penguins













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Flavor Oscillations

- Quantum mechanics with $\overline{B^0}$ and B^0 states: "What is a particle?"
 - Particle antiparticle transitions $\overline{B^0} \leftrightarrow \overline{B^0}$ mesons happen spontaneously.



Lecture Notes: Chapter 3

• Time evolution of B^0 and $\overline{B^0}$ described by an effective Hamiltonian

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Solving the Schrödinger Equation



 B^0 , $\overline{B^0}$: Flavour eigenstates

From the eigenvalue calculation:

$$q/p = -\sqrt{\left(M_{12}^* - \frac{i}{2}\Gamma_{12}^*\right)} / \left(M_{12} - \frac{i}{2}\Gamma_{12}\right)$$

Solution: (α and β are initial conditions):

 $\pm \frac{1}{2}\Delta\Gamma$

$$\Rightarrow \psi(t) = \alpha |B_H(t)\rangle + \beta |B_L(t)\rangle$$

Masses

$$\omega_{\pm} = m_{\pm} - \frac{i}{2}\Gamma_{\pm} \quad \left\{ \begin{array}{c} m_{\pm} = M \pm \frac{1}{2}\Delta m \\ \Gamma_{\pm} = \Gamma \pm \frac{1}{2}\Delta\Gamma \end{array} \right.$$

Lifetimes

weak Δm and $\Delta \Gamma$ follow from the Hamiltonian: $\Delta m = 2 \Re \sqrt{\left(M_{12} - \frac{i}{2}\Gamma_{12}\right) \left(M_{12}^* - \frac{i}{2}\Gamma_{12}^*\right)}$ $\Delta \Gamma = 4 \Im \left(M_{12} - \frac{i}{2} \Gamma_{12} \right) \left(M_{12}^* - \frac{i}{2} \Gamma_{12}^* \right)$ Examples $B^0: \Delta\Gamma \approx 0$, |q/p| = 1 B_s^0 : $\Delta\Gamma/\Delta m \ll 1$, |q/p| = 1 K^0 : $\Delta\Gamma/\Delta m \simeq 1$, $|q/p| - 1 \simeq 10^{-3}$

B^0 Oscillation Amplitudes

For an initially (t = 0) produced B^0 or a $\overline{B^0}$ it follows:

 $|\psi(t)
angle$:

$$B^{0}(t) \rangle = g_{+}(t) |B^{0}\rangle + \frac{q}{p} g_{-}(t) |\overline{B^{0}}\rangle$$
with
$$g_{\pm(t)} = \frac{e^{-i\omega_{+}t} \pm e^{-i\omega_{-}t}}{2}$$

$$g_{+}(t) = e^{-imt} e^{-\Gamma t/2} \cos \frac{\Delta m t}{2}$$

$$g_{-}(t) = e^{-imt} e^{-\Gamma t/2} i \sin \frac{\Delta m t}{2}$$

$$g_{\pm(t)} = e^{-imt} e^{-\Gamma t/2} i \sin \frac{\Delta m t}{2}$$

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 $|B^{0}\rangle = \frac{1}{2p}(|B_{H}\rangle + |B_{L}\rangle)$ $|\overline{B^{0}}\rangle = \frac{1}{2q}(|B_{H}\rangle - |B_{L}\rangle)$

using:

B^0 Oscillations



So far, so good...?







Hope not...



Observing *CP* Violation

• It's all about imaginary numbers...






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- Calculate the decay rate of a B-meson into a final state f: $\Gamma_{(B(t)\to f)} = |\langle f|B^0(t)\rangle|^2$
- From solving Schrodinger's equation we already had:



Master formula for neutral *B* decays

• Just by (tediously) writing it out...

$$\begin{split} \Gamma_{(B \to f)}(t) &= \left| A_f \right|^2 \left(1 + \left| \lambda_f \right|^2 \right) \frac{e^{-\Gamma t}}{2} \cdot \\ &\left(\cosh \frac{\Delta \Gamma t}{2} + D_f \sinh \frac{\Delta \Gamma t}{2} + C_f \cos \Delta m t - S_f \sin \Delta m t \right) \\ \Gamma_{(\overline{B} \to f)}(t) &= \left| A_f \right|^2 \left| \frac{q}{p} \right|^2 \left(1 + \left| \lambda_f \right|^2 \right) \frac{e^{-\Gamma t}}{2} \cdot \\ &\left(\cosh \frac{\Delta \Gamma t}{2} + D_f \sinh \frac{\Delta \Gamma t}{2} - C_f \cos \Delta m t + S_f \sin \Delta m t \right) \end{split}$$



• Coefficients D_f , C_f and S_f are measured by experiment → Measurement of CKM parameters via: $\lambda_f \equiv \frac{p}{q} \frac{A_f}{A_f} = \overline{B^0}$



 V_{cb}

 \bar{c} J/ψ

How does it give CP violation?

$$\underbrace{t = 0}_{q_{g}(t)} \underbrace{t}_{A_{f_{CP}}} A_{f_{CP}}(g_{+}(t) + \lambda g_{-}(t)) \\ g_{0}(t) = \frac{q}{p} \underbrace{\overline{A}_{f_{CP}}}_{f_{CP}} A_{f_{CP}}(g_{+}(t) + \lambda g_{-}(t)) \\ g_{0}(t) = \underbrace{f_{CP}}_{f_{CP}} \lambda_{f_{CP}} = \frac{q}{p} \underbrace{\overline{A}_{f_{CP}}}_{A_{f_{CP}}} g_{+}(t) = \frac{e^{-i(m-\Delta m/2)t} e^{-\Gamma t/2} + e^{-i(m+\Delta m/2)t} e^{-\Gamma t/2}}{2} \\ = e^{-imt} e^{-\Gamma t/2} \cos \frac{\Delta m t}{2} \\ g_{+}(t) = \underbrace{f_{CP}}_{q_{g}(t)} e^{-\Gamma t/2} - e^{-i(m+\Delta m/2)t} e^{-\Gamma t/2}}{2} \\ e^{-imt} e^{-\Gamma t/2} - e^{-i(m+\Delta m/2)t} e^{-\Gamma t/2}} \\ g_{-}(t) = \underbrace{f_{CP}}_{q_{g}(t)} e^{-\Gamma t/2} - e^{-i(m+\Delta m/2)t} e^{-\Gamma t/2}}{2} \\ e^{-imt} e^{-\Gamma t/2} i \sin \frac{\Delta m t}{2} \\ g_{+}(t) = \underbrace{f_{CP}}_{f_{CP}} \overline{A}_{f_{CP}} \left(g_{+}(t) + \frac{1}{\lambda}g_{-}(t)\right) \\ g_{0}(t) = \underbrace{f_{CP}}_{q_{g}(t)} e^{-\Gamma t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} \overline{A}_{f_{CP}} \left(g_{+}(t) + \frac{1}{\lambda}g_{-}(t)\right) \\ g_{0}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-\Gamma t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta m t}{2} \\ g_{-}(t) = \underbrace{f_{CP}}_{f_{CP}} e^{-T t/2} i \sin \frac{\Delta$$

Interfering Amplitudes

t = 0		t	Amplitude
B^0 $\overline{B^0}$	\rightarrow \rightarrow	fср fср	$A_{f_{CP}}\left(g_{+}(t) + \lambda g_{-}(t)\right)$ $\overline{A}_{f_{CP}}\left(g_{+}(t) + \frac{1}{\lambda}g_{-}(t)\right)$

$$g_{+} = e^{-imt} e^{-\Gamma t/2} \cos \frac{\Delta mt}{2}$$
$$g_{-} = e^{-imt} e^{-\Gamma t/2} i \sin \frac{\Delta mt}{2}$$
$$\lambda_{f_{CP}} = \frac{q}{p} \frac{\overline{A}_{f_{CP}}}{A_{f_{CP}}} = e^{-i\phi_{weak}} \quad (CKM)$$

Interfering Amplitudes

t = 0		t	Amplitude	Λmt
R^0	\rightarrow	fan	$A_{f_{CP}}(a_1 + a_2 e^{-i\phi_w} e^{i\pi/2})$	$g_+ = e^{-imt} e^{-\Gamma t/2} \cos \frac{2\pi t}{2}$
$\overline{B^0}$	\rightarrow	ГСР f _{CP}	$\overline{A}_{f_{CP}}(a_1 + a_2 e^{+i\phi_w} e^{i\pi/2})$	$g_{-} = e^{-imt} e^{-\Gamma t/2} \mathbf{i} \sin \frac{\Delta m t}{2}$
				$\lambda_{f_{CP}} = \frac{q}{p} \frac{\overline{A}_{f_{CP}}}{A_{f_{CP}}} = e^{-i\phi_{weak}} (CKM)$

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Interfering Amplitudes: CP violation!

 B^0

$$\frac{t = 0}{B^{0}} \xrightarrow{t} Amplitude} \qquad g_{+} = e^{-imt} e^{-\Gamma t/2} \cos \frac{\Delta m t}{2} \qquad g_{+} = e^{-imt} e^{-\Gamma t/2} \cos \frac{\Delta m t}{2} \qquad g_{-} = e^{-imt} e^{-\Gamma t/2} i \sin \frac{\Delta m t}{2} \qquad g_{-} = e^{-imt} e^{-\Gamma t/2} i \sin \frac{\Delta m t}{2} \qquad \lambda_{f_{CP}} = \frac{q}{p} \frac{\overline{A}_{f_{CP}}}{A_{f_{CP}}} = e^{-i\phi_{weak}} \quad (CKM)$$



Interfering Amplitudes: time dependent CP violation!



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From Amplitude to Decay rate

$$\frac{t = 0}{B^{0}} \xrightarrow{t} \frac{\text{Amplitude}}{A_{f_{CP}}} e^{-imt}e^{-i\Gamma t/2} \left(\cos\frac{\Delta mt}{2} + i\lambda \sin\frac{\Delta mt}{2}\right)$$

$$\overline{B^{0}} \xrightarrow{} f_{CP} \qquad \overline{A}_{f_{CP}} e^{-imt}e^{-i\Gamma t/2} \left(\cos\frac{\Delta mt}{2} + i\frac{1}{\lambda}\sin\frac{\Delta mt}{2}\right)$$

$$\lambda_{f_{CP}} = \frac{q}{p} \frac{\overline{A}_{f_{CP}}}{A_{f_{CP}}} = e^{-i\phi_{weak}}$$

• Decay rate is the *square* of the amplitude (work it out):

$$B^{0} \to f_{CP} : \left| \cos \frac{\Delta mt}{2} + i \lambda \sin \frac{\Delta mt}{2} \right|^{2} \propto 1 + \frac{(1-|\lambda|^{2})}{(1+|\lambda|^{2})} \cos \Delta mt - \frac{(2\Im\lambda)}{(1+|\lambda|^{2})} \sin \Delta mt$$
$$\overline{B^{0}} \to f_{CP} : \left| \cos \frac{\Delta mt}{2} + i \frac{1}{\lambda} \sin \frac{\Delta mt}{2} \right|^{2} \propto 1 - \frac{(1-|\lambda|^{2})}{(1+|\lambda|^{2})} \cos \Delta mt + \frac{(2\Im\lambda)}{(1+|\lambda|^{2})} \sin \Delta mt$$

Time Dependent CP violation

t = 0

 $\lambda_{f_{CP}} = \frac{q}{p} \, \frac{\overline{A}_{f_{CP}}}{A_{f_{CP}}} = e^{-i\phi_{weak}}$

t Amplitude

$$\begin{array}{lll}
B^{0} & \rightarrow & f_{CP} & A_{f_{CP}} e^{-imt} e^{-i\Gamma t/2} \left(\cos \frac{\Delta mt}{2} + i \ e^{-i\phi_{weak}} \ \sin \frac{\Delta mt}{2} \right) \\
\overline{B^{0}} & \rightarrow & f_{CP} & \overline{A}_{f_{CP}} \ e^{-imt} e^{-i\Gamma t/2} \left(\cos \frac{\Delta mt}{2} + i \ e^{+i\phi_{weak}} \ \sin \frac{\Delta mt}{2} \right)
\end{array}$$





Where were we?



"Mr. Osborne, may I be excused? My brain is full."

Time Dependent CP Asymmetry



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Similarly with this method of time dependent CP violation:

 \rightarrow B_s physics is mainly done at the LHC ...

How are you doing?



How are you doing?



How are you doing?



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- b) B-mixing and time dependent CP violation
- c) Experimental Aspects: LHC vs B-factory
- 3. Rare B-Decays
 - a) Effective Hamiltonian
 - b) Lepton Flavour Non-Universality





$B_s \rightarrow D_s K$: Quantum Interference Experiment @ LHCb



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$B_s \rightarrow D_s K$: Quantum Interference Experiment @ LHCb



$B_s \rightarrow D_s K$: Quantum Interference Experiment @ LHCb



$B_s \rightarrow D_s K$: Quantum Inter

CP violation

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$B_s \rightarrow D_s K$: Quantum Interference Experiment @ LHCb



The LHCb Detector? dOHJ



The LHCb Detector!



The LHCb Detector



Measure time dependent B and \overline{B} decay rates



B_s Physics at LHCb



Detector Requirements:

- Vertex reconstruction
- Momentum and mass reconstruction
- Particle identification (π, K, μ, e, γ)
- Trigger (Online reconstruction)

Physics Requirements:

- Signal selection and background suppression
- Flavour tagging: B or \overline{B} at production
- Decay time measurement: t = md/p



B_s Physics at LHCb - Vertex reconstruction



B_s Physics at LHCb - Vertex reconstruction


B_s Physics at LHCb



B_s Physics at LHCb – momentum and mass determination 59



B_{s} Physics at LHCb – momentum and mass determination



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B_s Physics at LHCb



B_s Physics at LHCb – Particle Identification with RICH



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B_s Physics at LHCb – Particle Identification with RICH



B_s Physics at LHCb



B_s Physics at LHCb – Trigger/Tag with Calorimeters and Muon⁶³



B_s Physics at LHCb – Trigger/Tag with Calorimeters and Muon⁶³



Measuring $B_s - B_s$ Oscillations

(Self tagging $B_s \rightarrow D_s \pi$)



Experimental Situation: Ideal measurement (no dilutions)





<u>Experimental Situation:</u> Ideal measurement (no dilutions) + Realistic flavour tagging dilution





Experimental Situation: Ideal measurement (no dilutions) + Realistic flavour tagging dilution + Realistic decay time resolution





Experimental Situation: Ideal measurement (no dilutions) + Realistic flavour tagging dilution + Realistic decay time resolution + Background events

Proper-time dependent decay rate: Perfect reconstruction 1000 + flavour tagging + proper time resolution + background 800 Events 600 $B_s \to D_s^- \pi^+$ (2 fb⁻¹) 400 200 0 5 0 3 Proper time (ps)



Experimental Situation:

Ideal measurement (no dilutions)

- + Realistic flavour tagging dilution
- + Realistic decay time resolution
- + Background events
- + Trigger and selection acceptance



Meson mixing in LHCb: does is actually work?



Meson mixing in LHCb: does is actually work?





B meson production in e^+e^- Collisions

.

10.54

) (4S)

10.58

10.62

• Electron-Positron collider:

 $e^+e^- \rightarrow \Upsilon(4s) \rightarrow B^0 \overline{B^0}$

14-6

10.00 10.02

r(1s)

9.46

9.44

r(2S)

25

20

10

 \rightarrow Hadrons)(nb)

σ (e⁺e

- Only 4S resonance or higher produces B meson pair
- Low B production cross-section: ~1 nb

Babar, Belle

- Clean environment, coherent $B^0\overline{B^0}$ production

Y(3S)

10.37

Mass (GeV/c⁻)

10.34



= 0.28

 $\sigma(hadr)$

• e⁺

(4 GeV)

$\Upsilon(4S)$: Coherent *B* - \overline{B} production

• Production at $\Upsilon(4S) J^{PC} = 1^{--}$:

 $B^0\overline{B^0}$ system evolves coherently until one *B* decays (EPR!)

$$\left| \left(B^0 \overline{B^0} \right)_{P=-} (t) \right\rangle = e^{-\Gamma_B t/2} \frac{1}{\sqrt{2}} \left| B^0 \left(\vec{k} \right) \overline{B^0} \left(-\vec{k} \right) \right\rangle - \left| B^0 \left(-\vec{k} \right) \overline{B^0} \left(\vec{k} \right) \right\rangle$$

- P = -1: Wave function is odd under particle exchange.
- The first decay of the two B's "starts the clock".
- Instead of flavour tag at production, *B* mesons have opposite flavour at the time the first meson decays.
 - Work with Δt
 - Half of the time the signal *B* decays first ($\Delta t < 0$)
- Coherent production improves flavour tagging performance



$\Upsilon(4S)$: Coherent *B* - \overline{B} production (Babar & Belle)





 $A_{CP}(t) = \sin 2\beta \sin \Delta m t$

Babar: $\sin 2\beta = 0.657 \pm 0.036 \text{ (stat)} \pm 0.012 \text{ (syst)}$ Belle: $\sin 2\beta = 0.670 \pm 0.029 \text{ (stat)} \pm 0.013 \text{ (syst)}$

Babar & Belle







Decay time dependent *CP* violation





 \mathbf{R}^0 decays

CKM triangle: putting all measurements together

	Measured	CKMfitter prediction	UTfit prediction
β	22.7 ± 0.7	23.7 ^{+1.1} _{-1.0}	23.8 ± 1.4
γ	70.0 ± 4.2	65.3 ^{+1.0} _{-2.5}	65.8 ± 2.2
α	93.1 ± 5.6	92.1 ^{+1.5} -1.1	90.1 ± 2.2





CPV in Kaons (K) and Beauty (B): How about Charm (D)?





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• Look at: $\Delta A_{CP} = A_{raw}(KK) - A_{raw}(\pi\pi) = A_{CP}(KK) - A_{CP}(\pi\pi)$ \Rightarrow All detection and production asymmetries cancel \Rightarrow Directly observe CP asymmetry!

2019: Discovery of CP violation in charm mesons!



- Which type of machine would you use?
 - e^+e^- or pp, pp or $p\overline{p}$ collider or fixed target? Why?
- At which energy do you want to run this machine?
- You will measure *CP* asymmetry in $B_s \rightarrow D_s^{\mp} K^{\pm}$ with BR=10⁻⁴
 - Estimate how many collisions you need for a precision of $\gamma {=} 1^{\circ}$
- You measure $B_s \to D_s^{\mp} K^{\pm}$ and $\overline{B_s} \to D_s^{\mp} K^{\pm}$
 - How do you determine the flavour of the B_s at production?
 - Are there intrinsic limits to this precision?
 - How would you calibrate the wrong tag fraction?
- There is a potential large background from another B_s -decay.
 - Do you know which it could be?
 - With which detector technology would you remove this background?
- What is the formula to reconstruct the B_s meson decay time in an event in observable quantities?
 - Which subdetectors would you require to measure it?

- Which type of machine would you use?
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Points to consider:

- e^+e^- at $\Upsilon(4S)$: electromagnetic production, clean, no B_S , coherent production: B^0 only time dependent CPV, requires asymmetric beams, good flavor tagging.
- e^+e^- at $\Upsilon(5S)$: B_s , lower cross section, no resolution for time dependent *CPV*.
- e^+e^- at Z-peak. Weak production, not coherent, interesting...?
- *pp* collisions: Strong production and lots of stat's, "messy" events, large backgrounds requiring excellent detectors.
- Fixed target vs collider: low cross section vs long decay distance.
 - b-quark cross section increases with high energy
- $pp \text{ vs } p\overline{p}$: "colour drag" asymmetry. Extra cross check for pp.

- You will measure *CP* asymmetry in $B_s \rightarrow D_s^{\mp} K^{\pm}$ with BR=10⁻⁴.
 - Estimate how many collisions you need for a precision of γ =1°
 - B_s mesons: Let's assume pp collisions at LHC using LHCb
- For ~1% measurement precision (0.01) on asymmetry:
 - Number of perfectly measured $B_s \rightarrow D_s^{\mp} K^{\pm}$ events:
 - Fraction of collisions that produce *b*-quarks:
 - Fraction of events where B_s meson is produced from b-quark:
 - Fraction of B_s that decay into $B_s \rightarrow D_s^{\mp} K^{\pm}$ channel
- → So in total

perfectly reconstructed events required

- Next, assumed measured by the LHCb experiment:
 - Acceptance x Reconstruction (background, resolution):
 - Trigger:
 - Tagging Power:
- In total

$pp\ {\rm collisions}\ {\rm must}\ {\rm be}\ {\rm collected}$

• Assume ~10 MHz collisions, 3 x 10⁶ s/year running time: ⁶ of running.

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Contents:

- 1. CP Violation
 - a) Discrete Symmetries
 - b) CP Violation in the Standard Model
 - c) Jarlskog Invariant and Baryogenesis

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