

Why three generations of particles?

Why is there no antimatter?

Why is an atom electric neutral?

Introducing the lecturers

Lecturer:

Marcel Merk



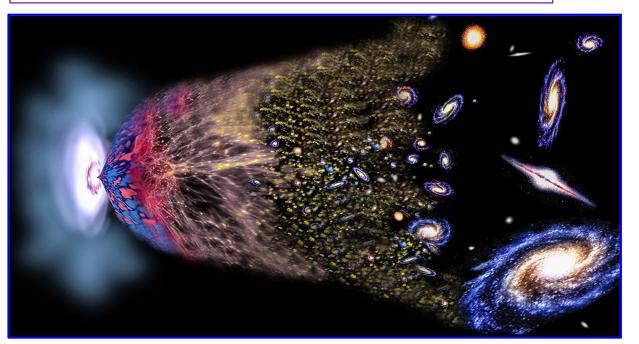
Tutors:

- Silvia Ferreres
- Miriam Lucio Martinez



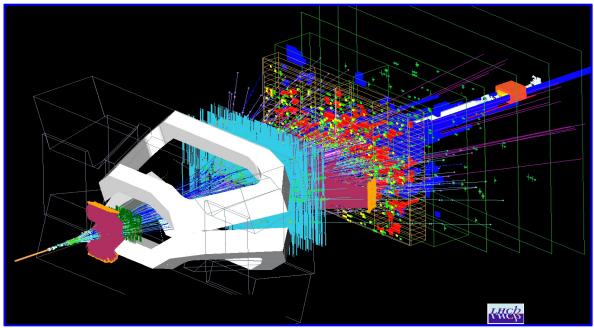
Research (theoretical):

- Why a *matter-vs-antimatter asymmetry* in nature?
- Why do we have *three generations* of particles?



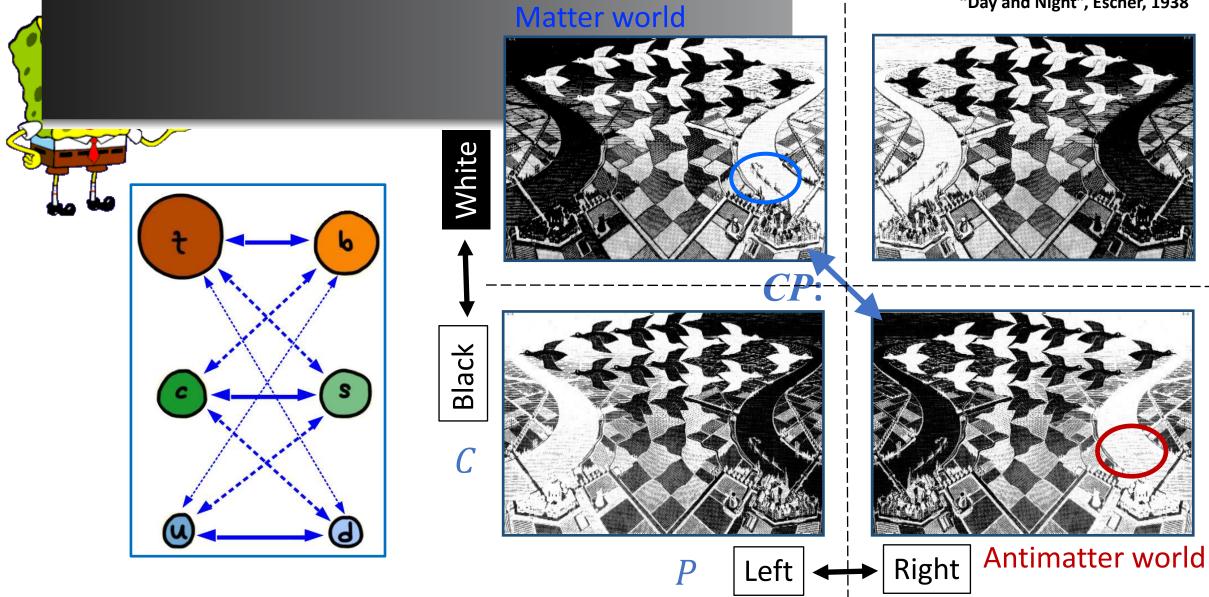
Research (experimental):

- Detector technology at the Large Hadron Collider.
- Measurements of CP violation rare decays



The Antimatter Mystery





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"Day and Night", Escher, 1938

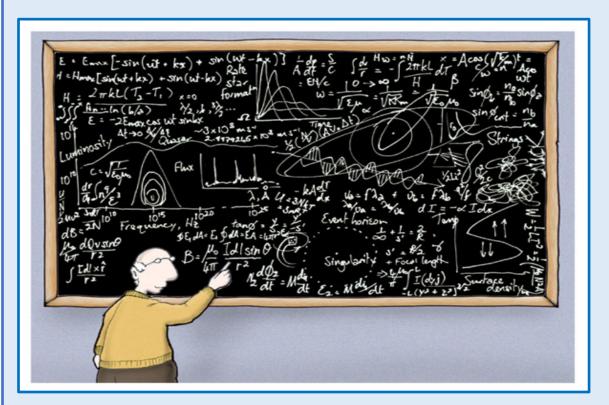
- 1. CP Violation
 - a) Discrete Symmetries
 - b) CP Violation in the Standard Model
 - c) Jarlskog Invariant and Baryogenesis

2. B-Mixing

- a) CP violation and Interference
- b) B-mixing and time dependent CP violation
- c) Experimental Aspects: LHC vs B-factory

3. B-Decays

- a) Effective Hamiltonian
- b) Lepton Flavour Non-Universality



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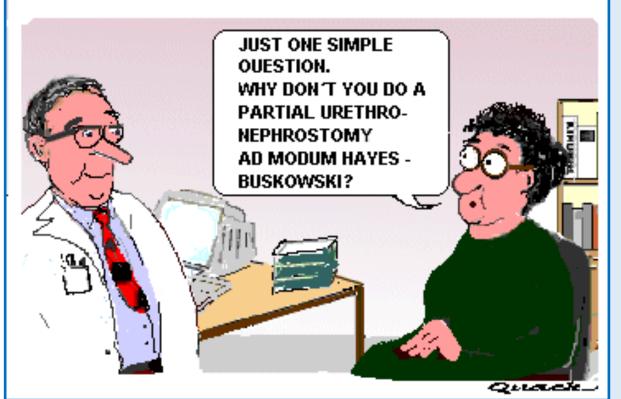
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Don't be afraid to ask questions...



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Symmetry and non-Observables

T.D.Lee: "The root to all *symmetry* principles lies in the assumption that it is impossible to observe certain basic quantities; the *non-observables*"

- There are four main types of symmetry:
- Permutation symmetry:
 - Bose-Einstein and Fermi-Dirac Statistics
- Continuous space-time symmetries:

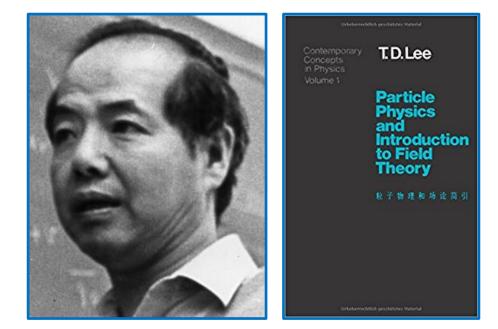
translation, rotation, velocity, acceleration,...

• Discrete symmetries:

space inversion, time reversal, charge conjugation,...

• Unitary symmetries: gauge invariances:

U₁(charge), SU₂(isospin), SU₃(color),...



- \Rightarrow If a quantity is fundamentally non-observable it is related to an *exact* symmetry
- ⇒ If it could in principle be observed by an improved measurement; the symmetry is said to be broken

Noether Theorem: symmetry

conservation law

Symmetry and non-observables

Non-observables	Symmetry Transformations	Conservation Laws or Selection Rule
Difference between identical particles	Permutation	BE. or FD. statistics
Absolute spatial position	Space translation: $\vec{r} \rightarrow \vec{r} + \vec{\Delta}$	momentum
Absolute time	Time translation: $t \rightarrow t + \tau$	energy
Absolute spatial direction	Rotation: $\vec{r} \rightarrow \vec{r}'$	angular momentum
Absolute velocity	Lorentz transformation	generators of the Lorentz group
Absolute right (or left)	$\vec{r} \rightarrow -\vec{r}$	parity
Absolute sign of electric charge	$e \rightarrow -e$	charge conjugation
Relative phase between states of different charge Q	$\psi ightarrow e^{i\theta Q}\psi$	charge
Relative phase between states of different baryon number B	$\psi \to e^{i\theta N}\psi$	baryon number
Relative phase between states of different lepton number L	$\psi ightarrow e^{i heta L} \psi$	lepton number
Difference between different coherent mixture of p and n states	$\binom{p}{n} \to U\binom{p}{n}$	isospin

C, P, T Symmetries

• Parity, P:

- Reflects a system through the origin. Converts right-handed to left-handed.
 - $\vec{x} \to -\vec{x}$, $\vec{p} \to -\vec{p}$ (vectors) but $\vec{L} = \vec{x} \times \vec{p}$ (axial vectors)
- Charge Conjugation, C: unobservable: (absolute charge)
 - Turns internal charges to opposite sign.
 - $e^+
 ightarrow e^-$, $K^-
 ightarrow K^+$

• Time Reversal, T: unobservable: (direction of time)

- Changes direction of motion of particles
 - $t \rightarrow -t$

• *CPT* Theorem:

- All interactions are invariant under combined C, P and T operation
- A particle *is* an antiparticle travelling backward in time
- Implies e.g. particle and anti-particle have equal masses and lifetimes

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Classical Mirror Worlds \rightarrow Invariant!

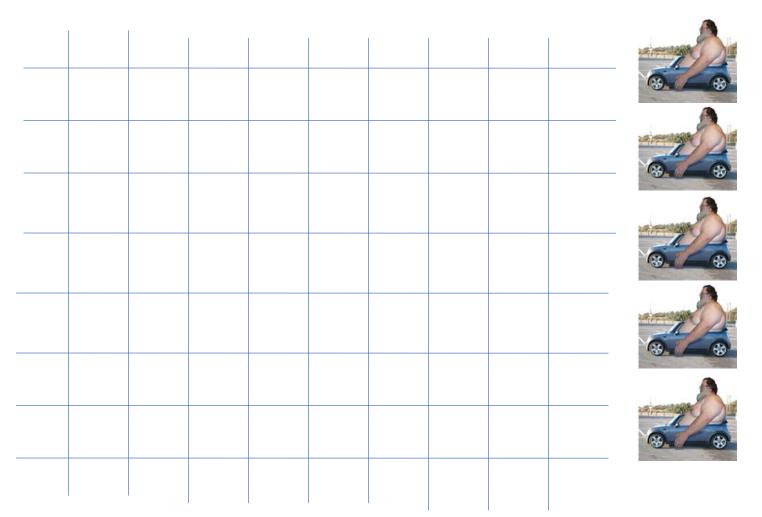
- Parity: $\vec{x} \rightarrow -\vec{x}$
 - Mass mP m = m: scalar- Force \vec{F} ($\vec{F} = d\vec{p}/dt$) $P \vec{F} = P d\vec{p}/dt = -d\vec{p}/dt = -\vec{F}$: vector- Acceleration \vec{a} ($\vec{a} = d^2\vec{x}/dt^2$) $P \vec{a} = -d^2x/dt^2 = -\vec{a}$: vector- Angular momentum $\vec{L}, \vec{S}, \vec{J}$ ($\vec{L} = \vec{x} \times \vec{p}$) $P \vec{L} = -\vec{x} \times -\vec{p} = \vec{L}$: axial vector
- <u>Parity</u>: Newton's law is *invariant* under *P*-operation (i.e. the same in the mirror world): $\vec{F} = m \vec{a} \xrightarrow{P} - \vec{F} = -m \vec{a} \iff \vec{F} = m \vec{a}$
- <u>Charge</u>: Lorentz Force in the *C*-mirror world is *invariant*: $\vec{F} = q [\vec{E} + \vec{v} \times \vec{B}] \xrightarrow{C} \vec{F} = -q [-\vec{E} + \vec{v} \times -\vec{B}]$
- <u>Time</u>: laws of physics are also *invariant* unchanged under *T*-reversal, since:

$$\vec{F} = m \, \vec{a} = m \, \frac{d^2 \vec{x}}{dt^2} \xrightarrow{T} \vec{F} = m \frac{d^2 \vec{x}}{d(-t)^2} \iff \vec{F} = m \overline{d}$$
• QM: Consider Schrodinger's equation $(t \to -t)$: $ih \frac{\partial \psi}{\partial t} = -\frac{\vec{\nabla}^2 \psi}{2m}$
Complex conjugation is required to stay invariant: $\psi \xrightarrow{T} \psi^*$

C-, *P*-, *T*- Symmetry

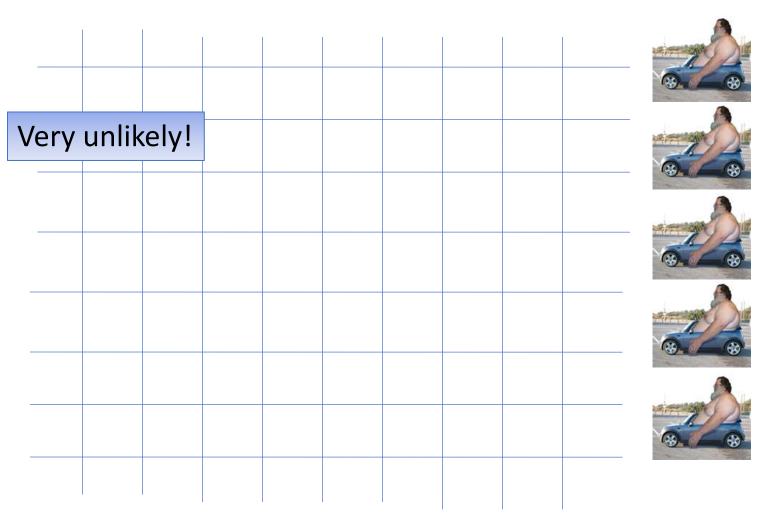
- Classical Theory is invariant under *C*, *P*, *T* operations; i.e. they conserve *C*, *P*, *T* symmetry
 - Newton mechanics, Maxwell electrodynamics.
- Suppose we watch some physical event. Can we determine unambiguously whether:
 - We are watching the event where all *charges are reversed* or not?
 - We are watching the event *in a mirror* or not?
 - Macroscopic biological asymmetries are considered *accidents of evolution* rather than fundamental asymmetry in the laws of physics.
 - We are watching the event in a *film running backwards* or not?
 - The arrow of time is due to thermodynamics: i.e. the realization of a macroscopic final state is *statistically more probable* than the initial state

Macroscopic time reversal (T.D. Lee)



- At each crossing: 50% 50% choice to go left or right
- After many decisions: reverse the velocity of the final state and return
- Do we end up with the initial state?

Macroscopic time reversal (T.D. Lee)



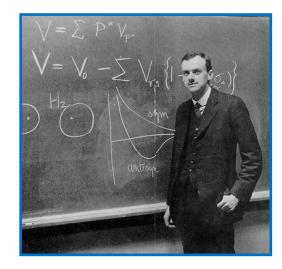
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Macroscopic time reversal

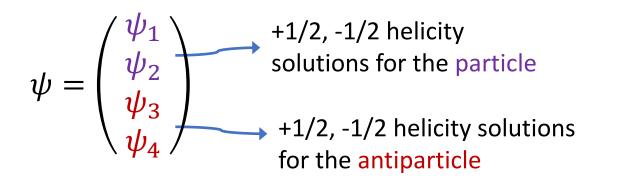


about entropy until much later...

C, P operations and Dirac theory (QED)



In Dirac theory particles are represented as spinors





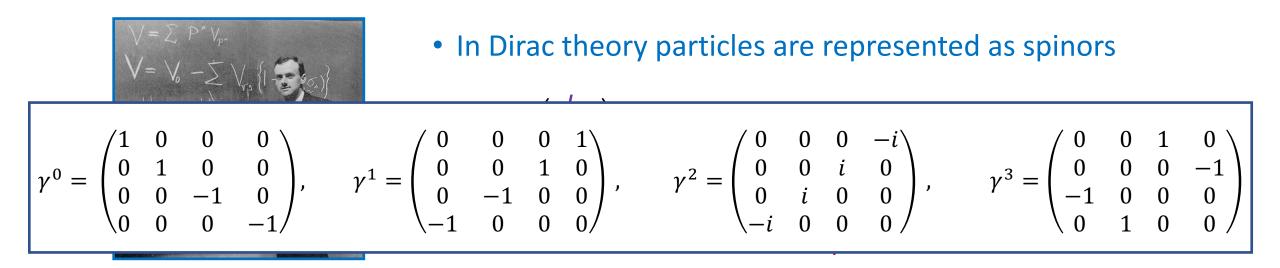
• Implementation of *P* and *C* operators in Dirac theory:

$$P: \psi \to \psi' = \gamma^0 \psi(-\vec{x}, t) \qquad C: \psi \to \psi' = i\gamma^2 \psi^*(\vec{x}, t)$$

$$\begin{pmatrix} [(i\gamma^0\partial_0 - i\gamma^i\partial_{x_i}) - m]\psi(\vec{x}, t) = 0 \\ \gamma^0[(i\gamma^0\partial_0 + i\gamma^i\partial_{x_i}) - m]\psi'(-\vec{x}, t) = 0 \end{pmatrix} \qquad \left(\begin{array}{cc} \text{Elect. } \psi : [\gamma^\mu(i\partial_\mu + eA_\mu) - m]\psi = 0 \\ \text{Posit. } \psi' : [\gamma^\mu(i\partial_\mu - eA_\mu) - m]\psi' = 0 \end{array} \right)$$

• QED (Dirac theory) is symmetric under *C*, *P* conjugation. Reversing electric charges keeps electrodynamics invariant. See lecture notes for more details.

C, P operations and Dirac theory (QED)



• Implementation of *P* and *C* operators in Dirac theory:

$$P: \psi \to \psi' = \gamma^{0}\psi(-\vec{x},t) \qquad C: \psi \to \psi' = i\gamma^{2}\psi^{*}(\vec{x},t)$$

$$\begin{pmatrix} [(i\gamma^{0}\partial_{0} - i\gamma^{i}\partial_{x_{i}}) - m]\psi(\vec{x},t) = 0 \\ \gamma^{0}[(i\gamma^{0}\partial_{0} + i\gamma^{i}\partial_{x_{i}}) - m]\psi'(-\vec{x},t) = 0 \end{pmatrix} \qquad \begin{pmatrix} \text{Elect. } \psi : [\gamma^{\mu}(i\partial_{\mu} + eA_{\mu}) - m]\psi = 0 \\ \text{Posit. } \psi' : [\gamma^{\mu}(i\partial_{\mu} - eA_{\mu}) - m]\psi' = 0 \end{pmatrix}$$

• QED (Dirac theory) is symmetric under C, P conjugation. Reversing electric charges keeps electrodynamics invariant. See lecture notes for more details.

C, P operations and Dirac theory (QED)

$$\gamma^{0} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}, \qquad \gamma^{1} = \begin{pmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & -1 & 0 & 0 \\ -1 & 0 & 0 & 0 \end{pmatrix}, \qquad \gamma^{2} = \begin{pmatrix} 0 & 0 & 0 & -i \\ 0 & 0 & i & 0 \\ 0 & i & 0 & 0 \\ -i & 0 & 0 & 0 \end{pmatrix}, \qquad \gamma^{3} = \begin{pmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \\ -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}$$

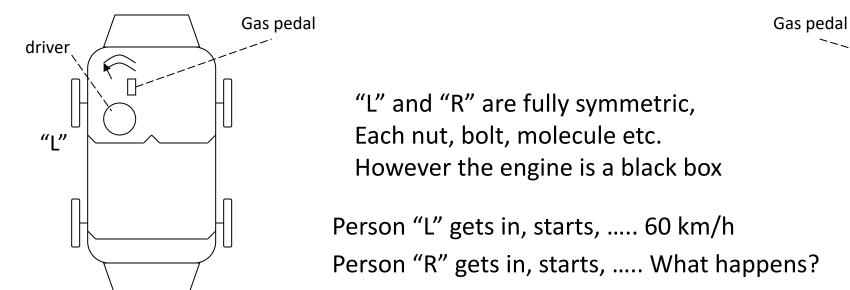
- In Dirac equation: $[(i\gamma^0\partial_0 i\gamma^i\partial_{x_i}) m]\psi(\vec{x},t) = 0$
- Implementation of *P* operator in Dirac: $\vec{x} \to -\vec{x}$; $\partial x_i \to -\partial x_i$ $P: \psi \to \psi' = \psi(-\vec{x}, t) \qquad [(i\gamma^0\partial_0 + i\gamma^i\partial_{x_i}) - m]\psi(-\vec{x}, t) = 0$ Does not work! Instead: $\psi \to \psi' = \gamma^0\psi(-\vec{x}, t) \qquad [(i\gamma^0\partial_0 + i\gamma^i\partial_{x_i}) - m]\gamma^0\psi(-\vec{x}, t) = 0$

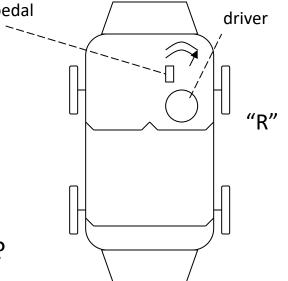
$$\gamma^0 [(i\gamma^0\partial_0 - i\gamma^i\partial_{x_i}) - m]\psi'(-\vec{x}, t) = 0 \qquad \text{OK}$$

- Implementation of *C* operator in Dirac: $C : q \to -q$; $\psi \to \psi' = i\gamma^2 \psi^*(\vec{x}, t)$
- $\psi : [\gamma^{\mu}(i\partial_{\mu} qA_{\mu}) m]\psi = 0 \qquad \psi' : [\gamma^{\mu*}(-i\partial_{\mu} + qA_{\mu}) m]i\gamma^{2}\psi^{*} = 0$ $\psi' : [\gamma^{\mu}(i\partial_{\mu} + qA_{\mu}) - m]^{*}\psi' = 0 \qquad \psi' : i\gamma^{2}[\gamma^{\mu}(i\partial_{\mu} + qA_{\mu}) - m]\psi^{*} = 0 \quad \text{OK}$

Parity Violation Before 1956 physicists were <u>convinced</u> that the laws of nature were left-right symmetric. Strange?

A "gedanken" experiment: consider two perfectly mirror symmetric cars:



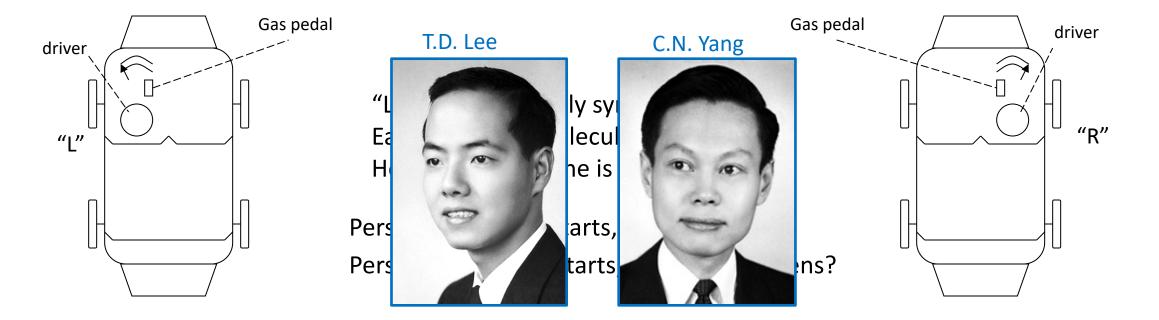


What happens in case the ignition mechanism uses, say, $Co^{60} \beta$ decay?



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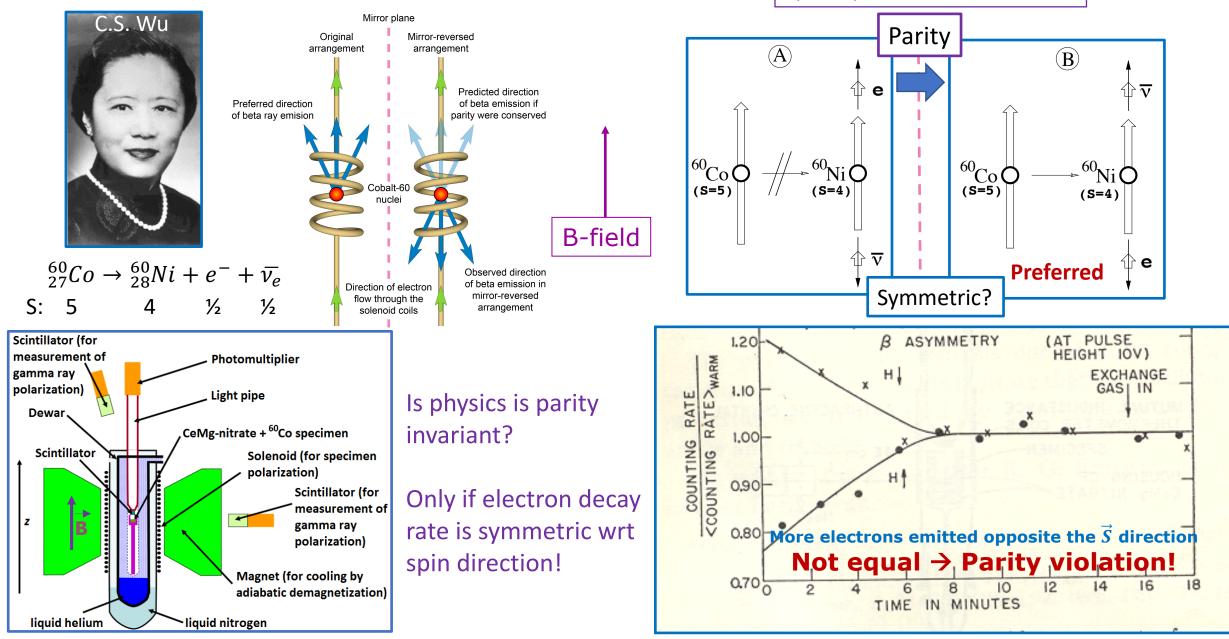
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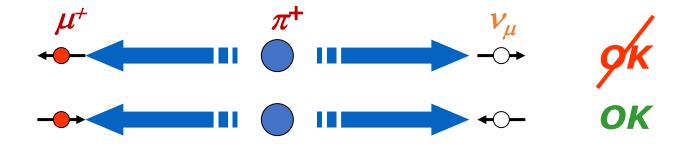
Discovery of Parity Violation

Spin is pseudoscalar, P: $\vec{S} \rightarrow \vec{S}$



So P is violated, what's next?

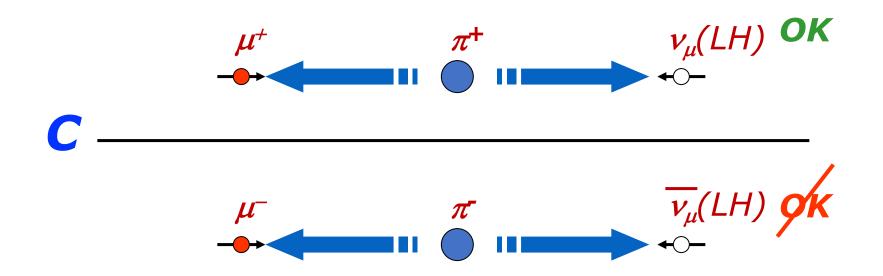
- Wu's experiment was shortly followed by another clever experiment by L. Lederman: Look at decay $\pi^+ \rightarrow \mu^+ \nu_{\mu}$
 - Pion has spin 0, μ , ν_{μ} both have spin $\frac{1}{2}$
 - \rightarrow spin of decay products must be oppositely aligned
 - \rightarrow Helicity of muon is same as that of neutrino.



• Ledermans result: All neutrinos are left-handed and all anti-neutrinos are right-handed

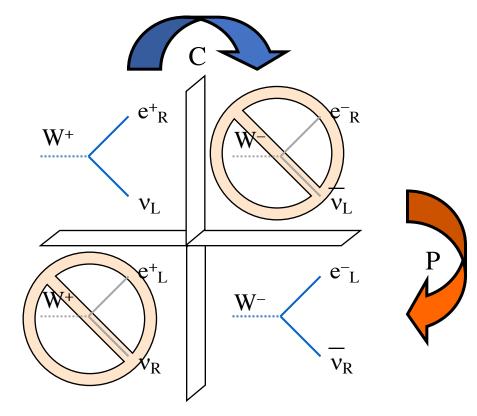
Charge conjugation symmetry?

- Introducing *C*-symmetry
 - The C(harge) conjugation is the operation which exchanges **particles and anti-particles** (not just electric charge)
 - It is a discrete symmetry, just like P, i.e. $C^2 = 1$



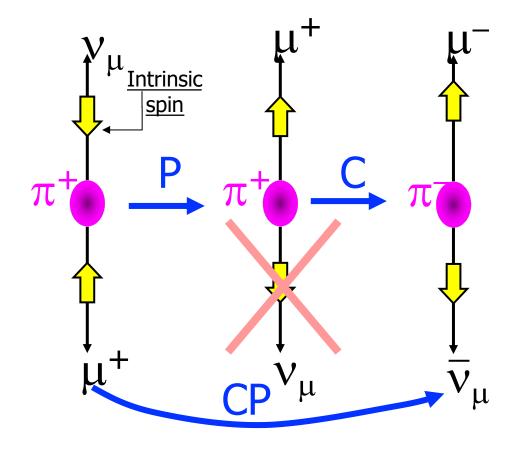
- C symmetry is broken by the weak interaction
 - Just like P

Weak Force breaks C and P, is CP really OK?



- Weak interaction breaks *C* and *P* symmetry maximally!
 - Nature is left-handed for matter and righthanded for antimatter.
- Despite *maximal* violation of *C* and *P*, combined *CP* seems *conserved*.
- Is combined **CP** really exactly conserved?

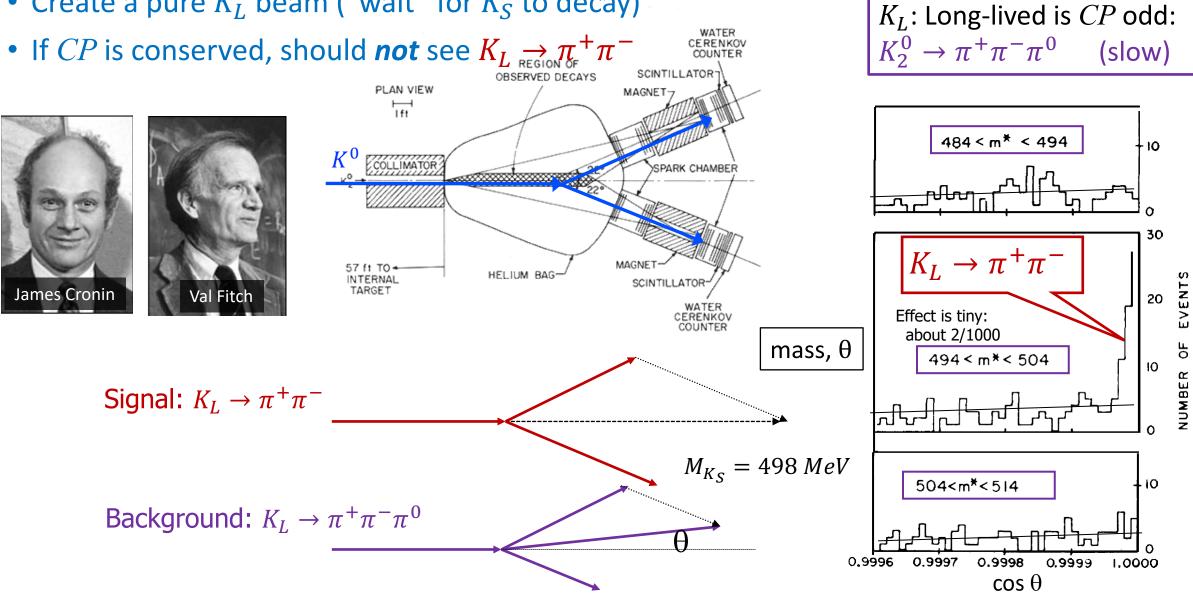
The Weak force and *CP* violation



- Combined *C* + *P* = *CP* symmetry?
 - **CP** symmetry is parity conjugation: $(x, y, z \rightarrow -x, -y, -z)$ followed by charge conjugation: $(\psi \rightarrow \overline{\psi})$
- **CP** symmetry *appears* to be preserved in the weak interaction
- But in 1964, Christenson, Cronin, Fitch and Turlay observed *CP* violation in decays of neutral kaons...

Discovery of *CP*-Violation with K^0 decays

• Create a pure K_L beam ("wait" for K_S to decay)



 K_{S} : Short-lived is *CP* even:

 $K_1^0 \rightarrow \pi^+ \pi^-$ (fast)

Discovery of *CP*-Violation with K^0 decays

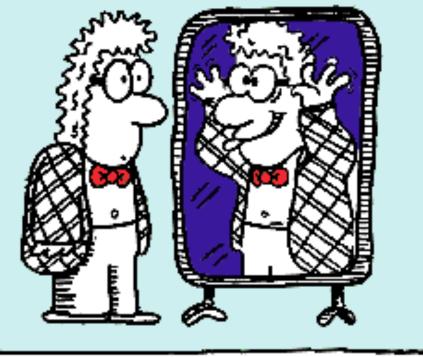
- Create a pure K_L be a function of the descent of the descent
- If CP is conserved,

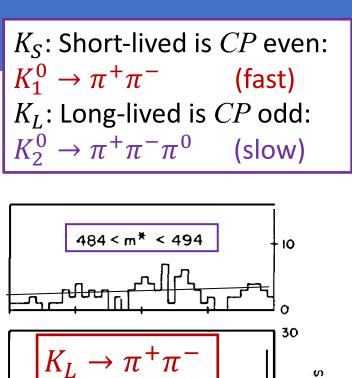


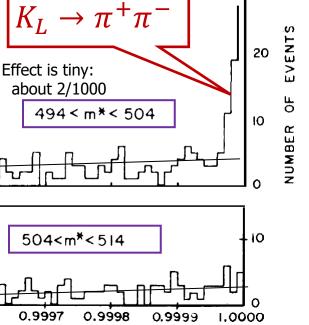
Signal: $K_1^0 \rightarrow \pi$

Background: K

THE MIRROR DID NOT SEEM TO BE OPERATING PROPERLY.



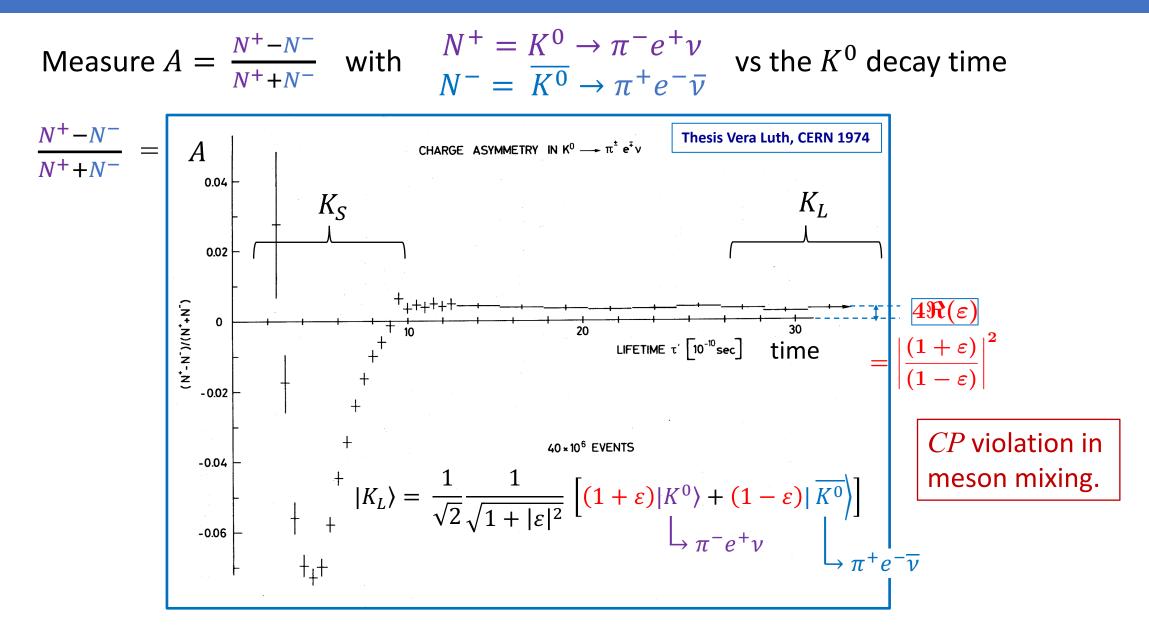




 $\cos \theta$

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Alternative: Charge Asymmetry in K^0 decays



Contact with Aliens !

Compare $K_L^0 \to \pi^+ e^- \bar{\nu}$ to $K_L^0 \to \pi^- e^+ \nu$

Compare the charge of the most abundantly produced electron with that of the electrons in your body: If opposite: matter If equal: anti-matter

Are they made of matter or anti-matter?

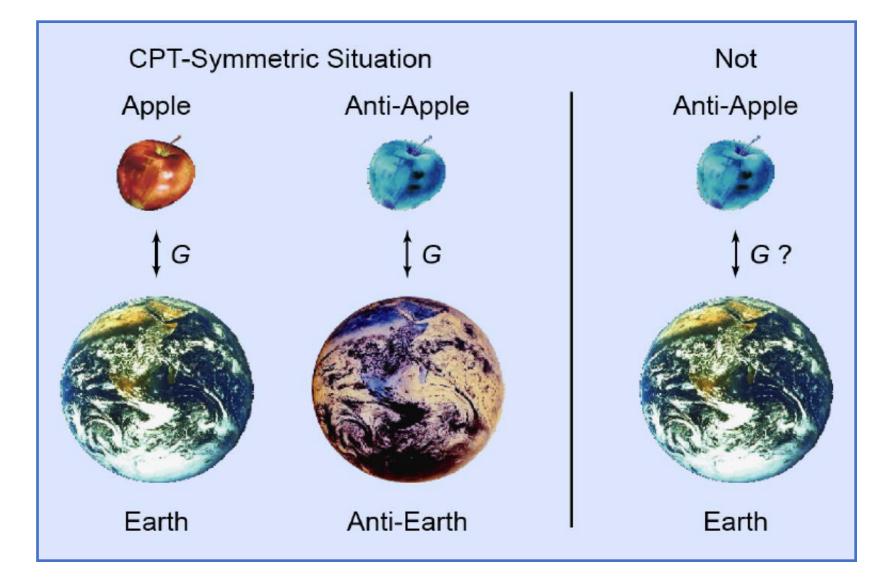


CPT Violation...



CPT symmetry implies that an antiparticle is *identical* to a particle travelling backwards in time.

CPT is conserved, but does anti-matter fall down?



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Weak interaction in three Flavour Generations

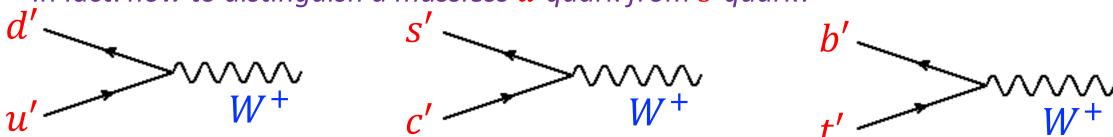
- Weak Interaction is 100% parity violating.
 - Wolfgang Pauli: "I cannot believe God is a weak left-hander."
- Implement an SU(2)_L symmetry for *massless* particles:

 $\mathcal{L}_W = \frac{g}{\sqrt{2}} u'_L \gamma_\mu W^\mu d'_L \qquad x3!$



• Flavour universality: *identical interactions* in three generations.

• In fact: how to distinguish a massless d'quark from s'quark?



- There is no CP violation in these massless interactions
 - What happens when particles acquire mass?

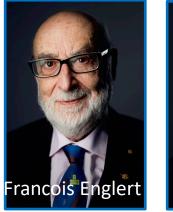
Spontaneous Symmetry Breaking→ Origin of Mass

• Yukawa couplings to massless particles:

$$\mathcal{L}_{Y} = Y_{ij}^{d} \left(\overline{u'_{i}}, \overline{d'_{i}} \right)_{L} \left(\begin{array}{c} \phi^{+} \\ \phi^{0} \end{array} \right) d'_{jR} + Y_{ij}^{u} \left(\overline{u'_{i}}, \overline{d'_{i}} \right)_{L} \left(\begin{array}{c} \phi^{0} \\ \phi^{-} \end{array} \right) u'_{jR}$$

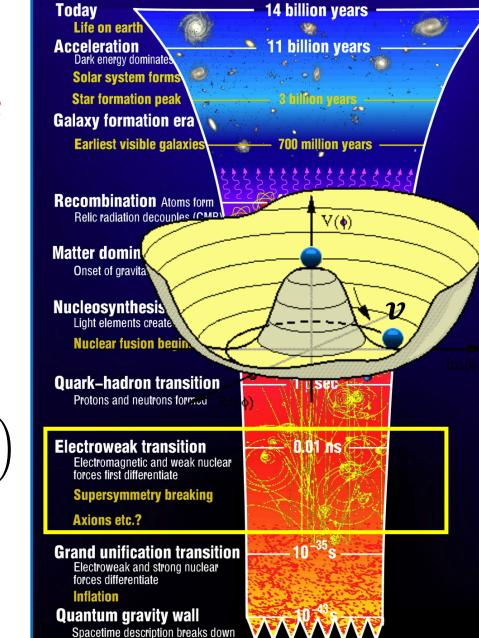
- Yukawa interaction is *not* flavour universal!
- →Unknown origin of Yukawa matrix acting on generations "i" and "j"
- SSB: B-E-H Mechanism:







➔ Massive W- and Z- bosons



Spontaneous Symmetry Breaking→ Origin of Mass

• Yukawa couplings to massless particles (Weinberg):

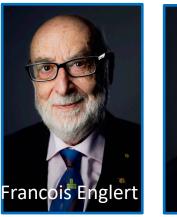
$$\mathcal{L}_{Y} = Y_{ij}^{d} \left(\overline{u_{i}'}, \overline{d_{i}'}\right)_{L} \begin{pmatrix} 0 \\ \nu/\sqrt{2} \end{pmatrix} d_{jR}' + Y_{ij}^{u} \left(\overline{u_{i}'}, \overline{d_{i}'}\right)_{L} \begin{pmatrix} \nu/\sqrt{2} \\ 0 \end{pmatrix} u_{jR}'$$

- Yukawa interaction is *not* flavour universal!
- →Unknown origin of Yukawa matrix acting on generations "i" and "j"

→Massive fermions

• SSB: B-E-H Mechanism:

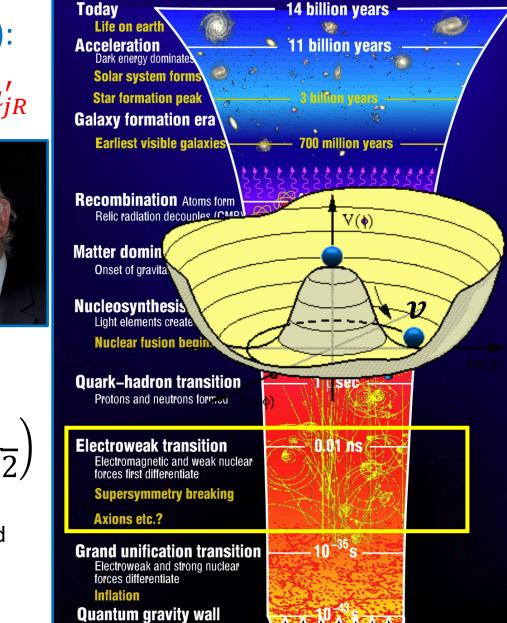






 $\begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} \rightarrow \begin{pmatrix} 0 \\ \nu/\sqrt{2} \end{pmatrix}$

➔ Massive W- and Z- bosons



Spacetime description breaks down

Spontaneous Symmetry Breaking→ Origin of Mass

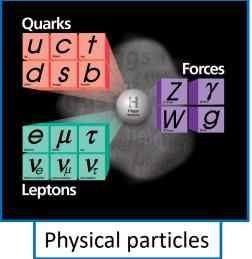
• Yukawa couplings to massless particles:

$$\mathcal{L}_{Y} = Y_{ij}^{d} \left(\overline{u_{i}'}, \overline{d_{i}'}\right)_{L} \begin{pmatrix} 0 \\ v/\sqrt{2} \end{pmatrix} d_{jR}' + Y_{ij}^{u} \left(\overline{u_{i}'}, \overline{d_{i}'}\right)_{L} \begin{pmatrix} v/\sqrt{2} \\ 0 \end{pmatrix} u_{jR}'$$

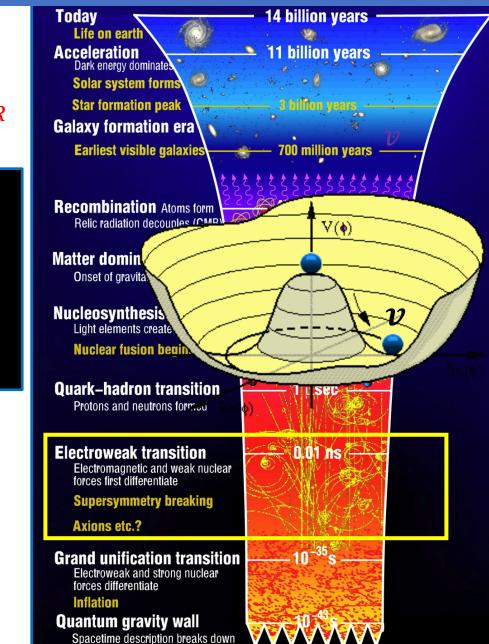
• Diagonalize Y_{ij} : $u_i = (V^u)_{ij} u'_j$ and $d_i = (V^d)_{ij} d'_j$ \rightarrow mass and flavour eigenstates

• Mass terms:
$$M_{ij} = Y_{ij} v/\sqrt{2}$$

 $\mathcal{L}_Y \rightarrow \mathcal{L}_H = m_d d_L d_R + m_u u_L u_R$



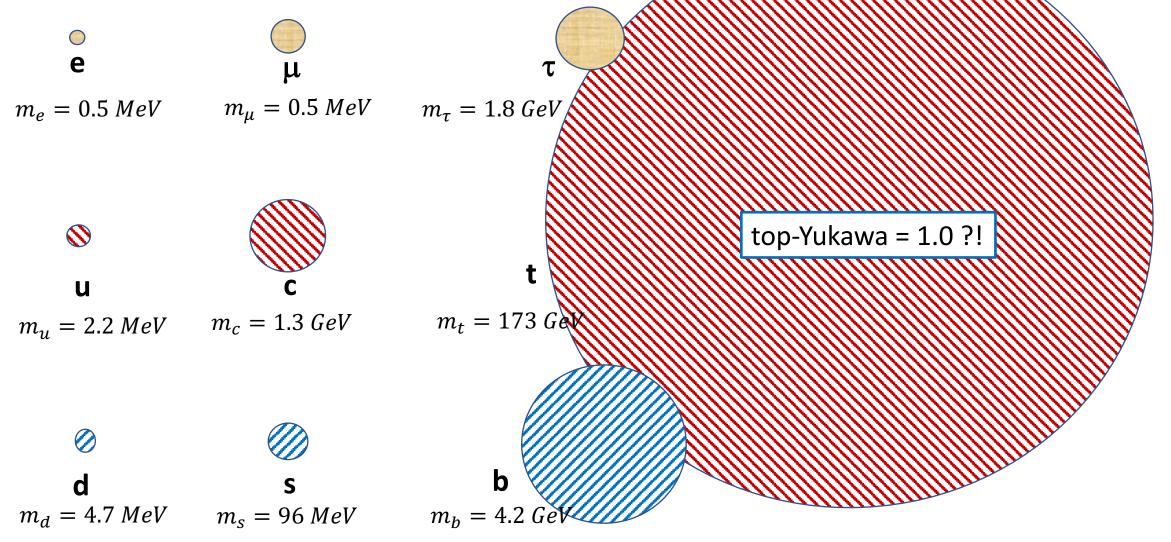
- Top quark mass: $m_{top} = 1.0 \ v/\sqrt{2}$
 - To first order Higgs couples only to top with coupling strength 1.0 !
 - Very flavour non-universal



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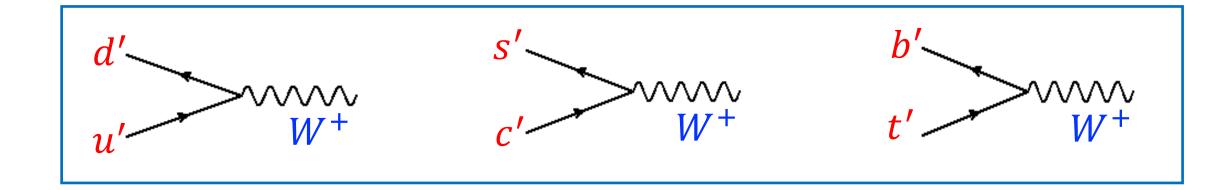
Flavour Puzzle: particle masses? Origin Yukawa couplings? 28

- Weak interaction flavour universal
- Higgs interaction almost purely 3rd generation.



The Weak Interaction \rightarrow Flavour Mixing

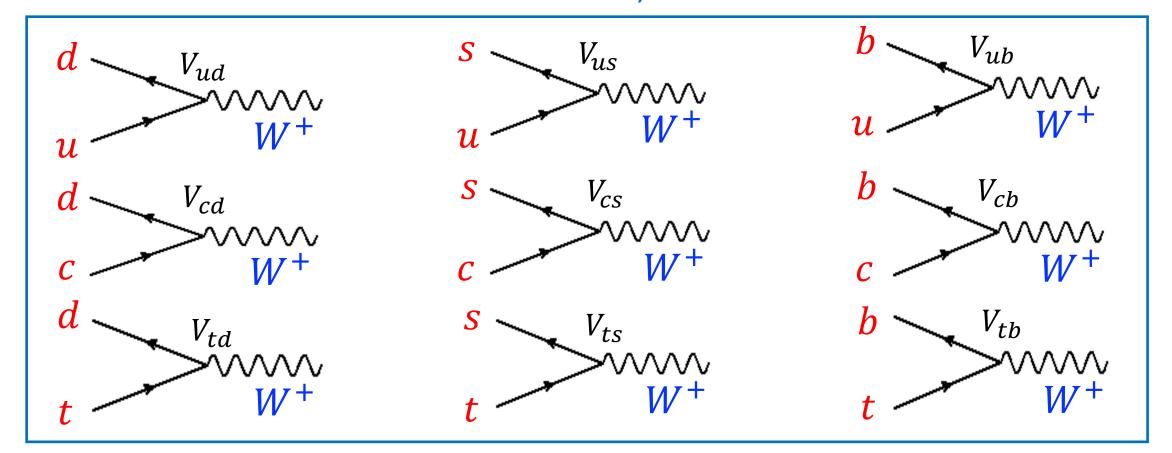
$$\mathcal{L}_W = \frac{g}{\sqrt{2}} u'_L \gamma_\mu W^\mu d'_L$$



Redefine:
$$u'_i = (V^u)_{ij} u_i$$
 and: $d'_i = (V^d)^{\dagger}_{ij} d_i$, such that: $V_{CKM} = (V^u V^{d\dagger})_{ij}$...

The Weak Interaction \rightarrow Flavour Mixing

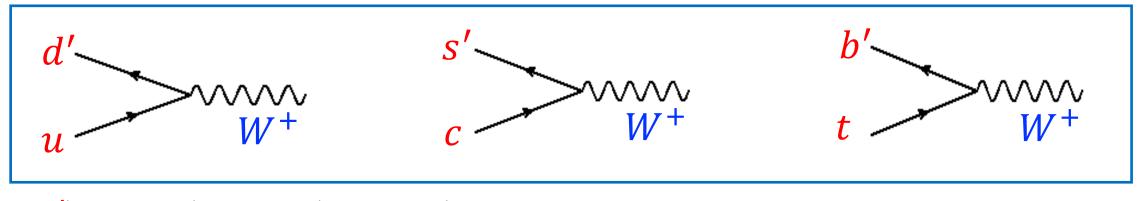
$$\mathcal{L}_{W} = \frac{g}{\sqrt{2}} u'_{L} \gamma_{\mu} W^{\mu} d'_{L} \longrightarrow \mathcal{L}_{W} = \frac{g}{\sqrt{2}} V_{CKM} u_{L} \gamma_{\mu} W^{\mu} d_{L}$$
Redefine: $u'_{i} = (V^{u})_{ij} u_{i}$ and: $d'_{i} = (V^{d})^{\dagger}_{ij} d_{i}$, such that: $V_{CKM} = (V^{u}V^{d\dagger})_{ij}$...
Generation structure of weak interaction, now includes CP violation



The Weak Interaction \rightarrow Flavour Mixing

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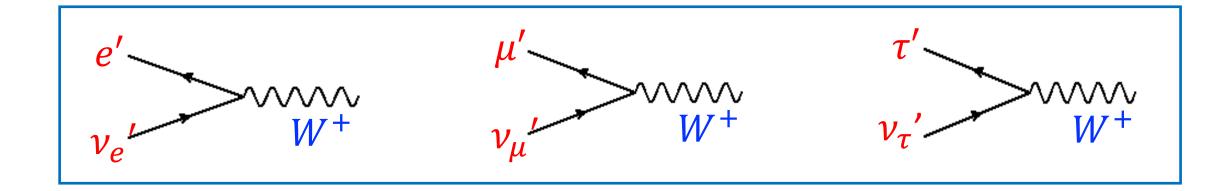
<u>Convention</u>: instead, we do as if: $u'_i = u_i$ and $d'_i = (V_{CKM})_{ij} d_j$



 $|\mathbf{d}'\rangle = V_{ud} |\mathbf{d}\rangle + V_{us} |\mathbf{s}\rangle + V_{ub} |\mathbf{b}\rangle$

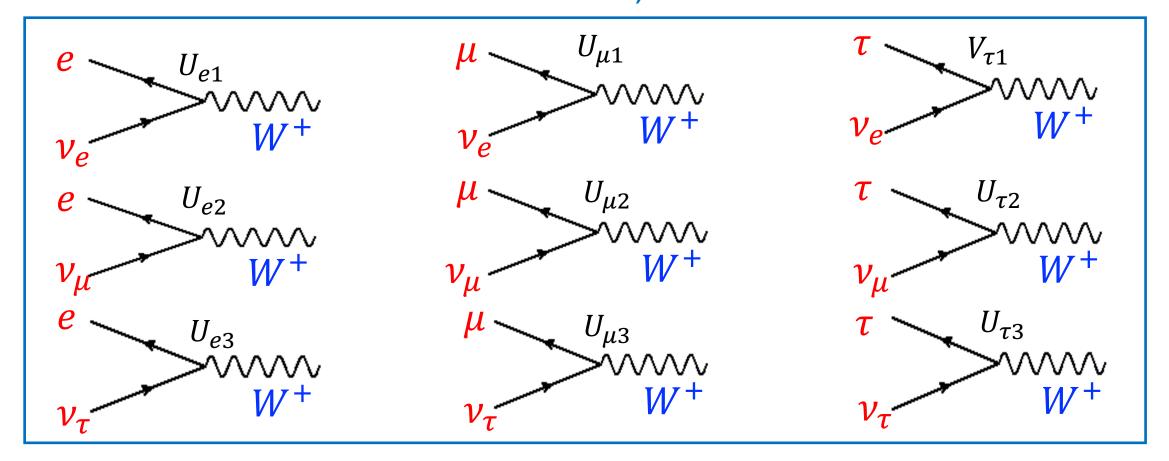
 $|s'\rangle = V_{cd} |d\rangle + V_{cs} |s\rangle + V_{cb} |b\rangle$ $|b'\rangle = V_{td} |d\rangle + V_{ts} |s\rangle + V_{tb} |b\rangle$

$$\mathcal{L}_W = \frac{g}{\sqrt{2}} \nu'_{e_L} \gamma_\mu W^\mu e'_L$$



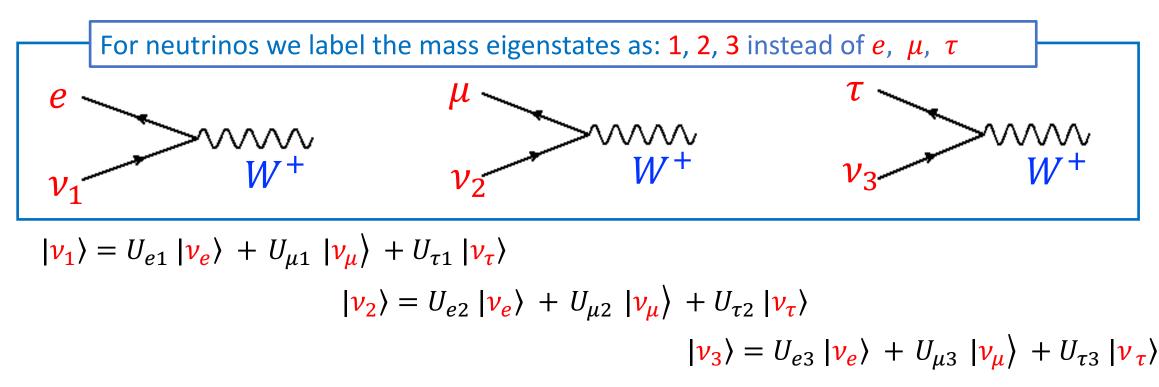
Redefine:
$$\mathbf{v}_{i}' = (U^{\nu})_{ij} \mathbf{v}_{i}$$
 and: $\mathbf{l}_{i}' = (U^{l})_{ij}^{\dagger} \mathbf{l}_{i}$, such that: $U_{MNS} = (U^{\nu} U^{l\dagger})_{ij}$...

$$\mathcal{L}_{W} = \frac{g}{\sqrt{2}} \mathbf{v}'_{L} \gamma_{\mu} W^{\mu} \mathbf{e}'_{L} \longrightarrow \mathcal{L}_{W} = \frac{g}{\sqrt{2}} U_{MNS} \mathbf{v}_{L} \gamma_{\mu} W^{\mu} \mathbf{e}_{L}$$
Redefine: $\mathbf{v}'_{i} = (U)_{ij} \mathbf{v}_{i}$ and: $\mathbf{l}'_{i} = (U^{d})^{\dagger}_{ij} \mathbf{l}_{i}$, such that: $U_{MNS} = (U^{u}U^{d\dagger})_{ij}$...
Generation structure of weak interaction, now includes CP violation



 $\mathcal{L}_{W} = \frac{g}{\sqrt{2}} v'_{L} \gamma_{\mu} W^{\mu} e'_{L} \longrightarrow \mathcal{L}_{W} = \frac{g}{\sqrt{2}} U_{MNS} v_{L} \gamma_{\mu} W^{\mu} e_{L}$ Redefine: $v'_{i} = (U)_{ij} v_{i}$ and: $l'_{i} = (U^{d})^{\dagger}_{ij} l_{i}$, such that: $U_{MNS} = (U^{u}U^{d\dagger})_{ij}$... Generation structure of weak interaction, now includes CP violation.

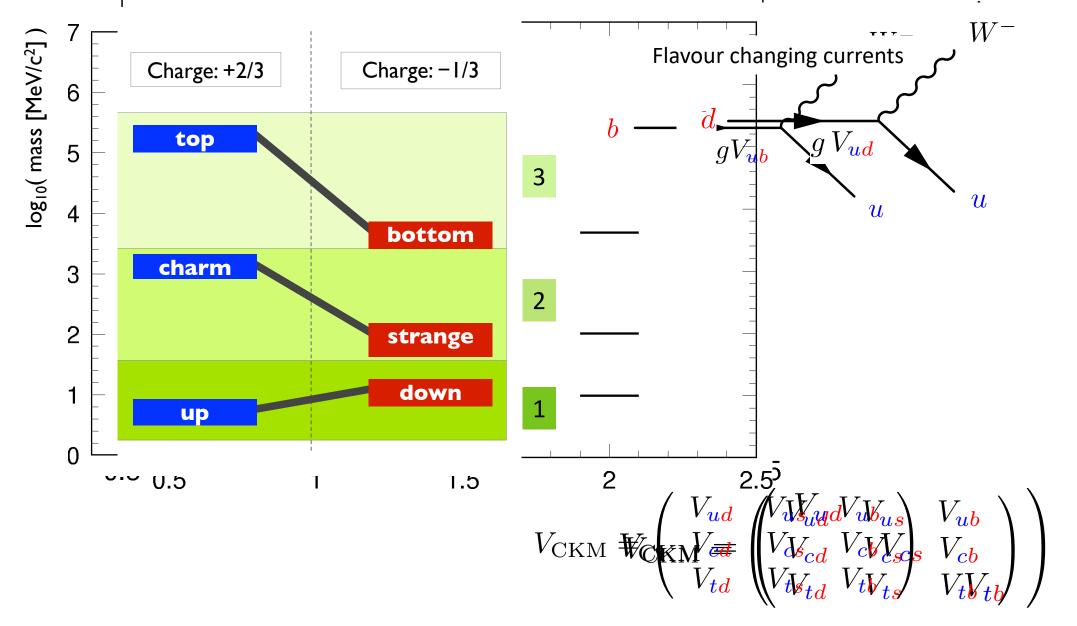
<u>Convention</u>: instead we do as if: $v_{1,2,3} = (U_{MNS})_{ij} v_{e,\mu,\tau}$ and $l_i' = l_i$



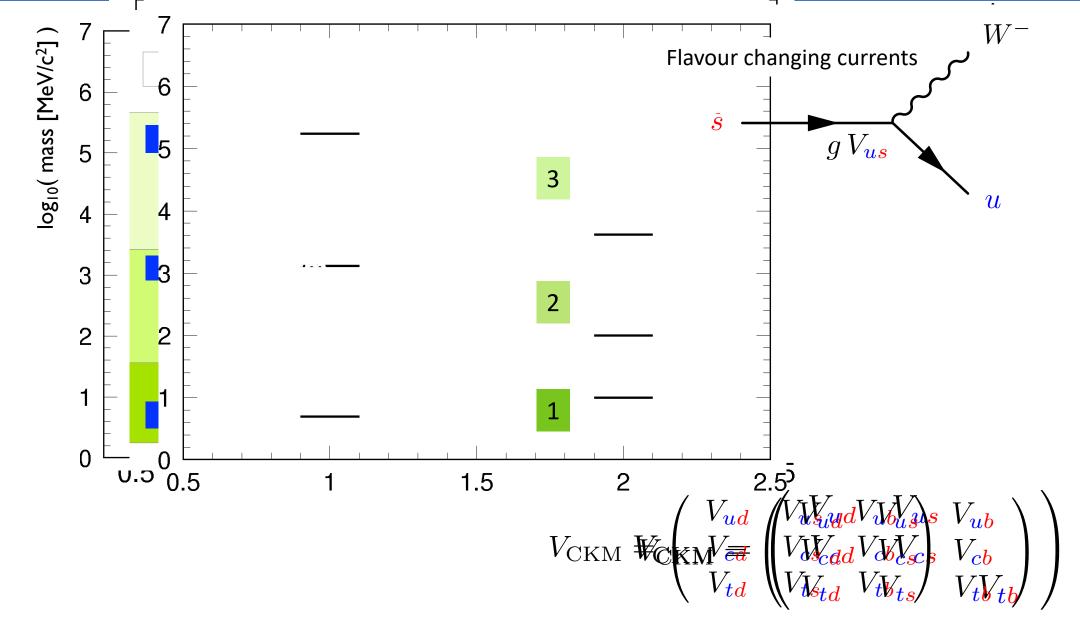
Food for thought: which states mix?

- Quarks: $\binom{u}{d'} = \binom{u}{V_{ud} d + V_{us} s + V_{ub} b}$; We say "the down-type quarks mix".
- Leptons: $\binom{v_1}{e} = \binom{U_{e1} v_e + U_{\mu 1} v_{\mu} + U_{\tau 1} v_{\tau}}{e}$; We say "the neutrinos mix."
- Why the "down-types" in one case and the "up-types" in another?
- Answer: it is convention! Both mix individually (in an unknown way).
 - The interaction is always: $\mathcal{L}_W = \frac{g}{\sqrt{2}} V_{CKM} u_L \gamma_\mu W^\mu d_L$
 - i.e up and down-type combined!
- Paradox question: does this mean neutrino mixing is unphysical??

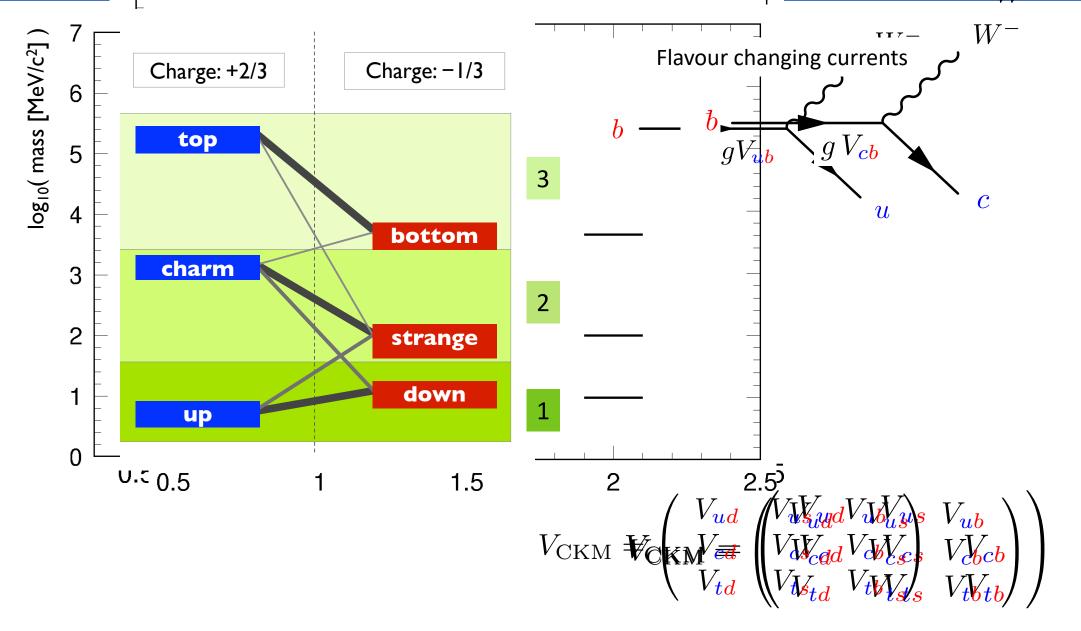
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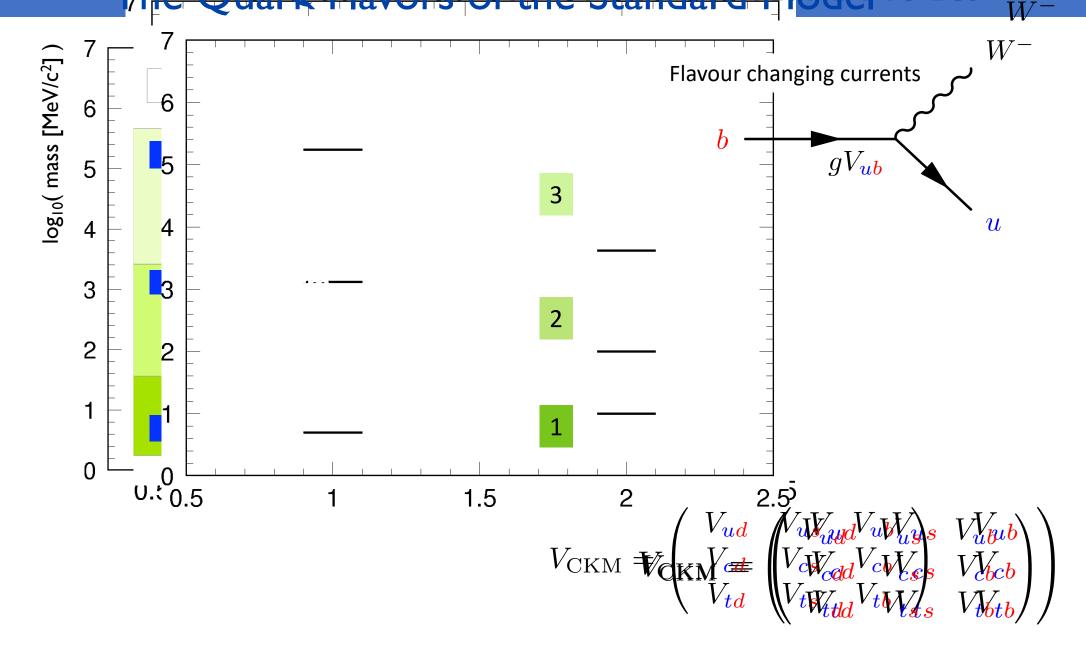
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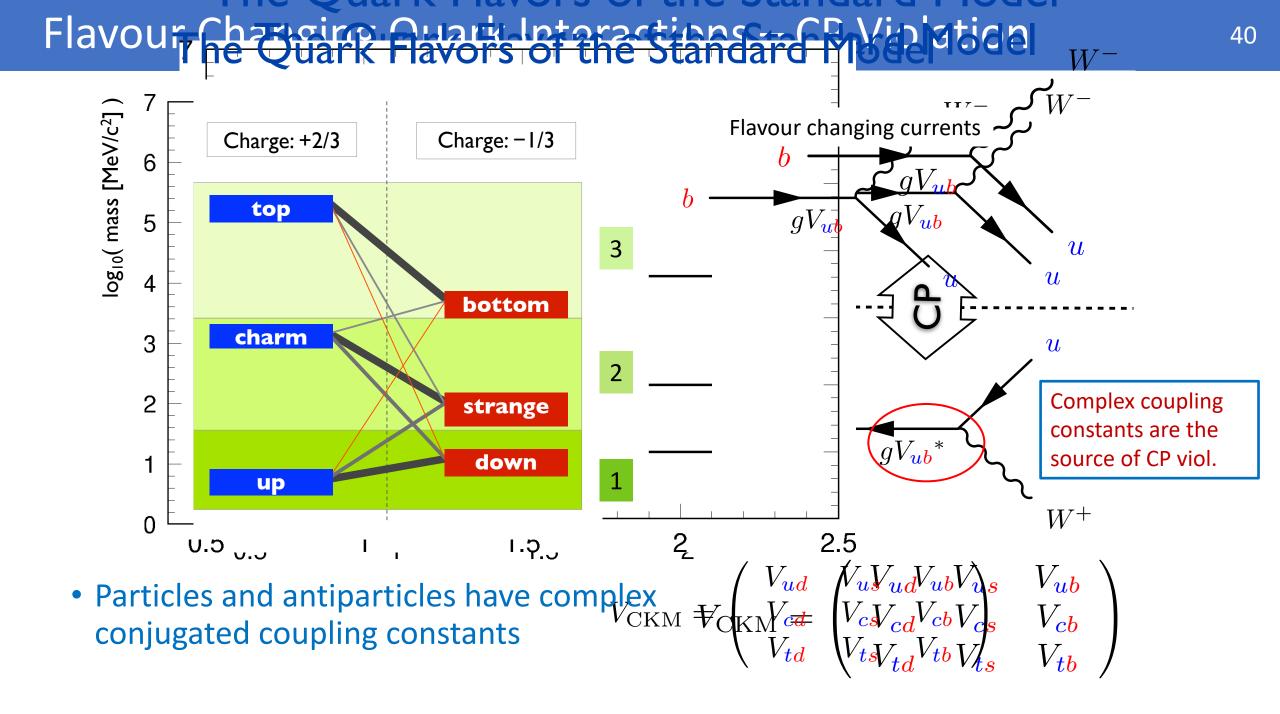


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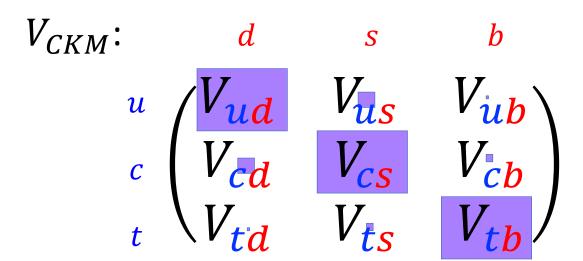


Flavour chameiro Auartanteration Standarde Model





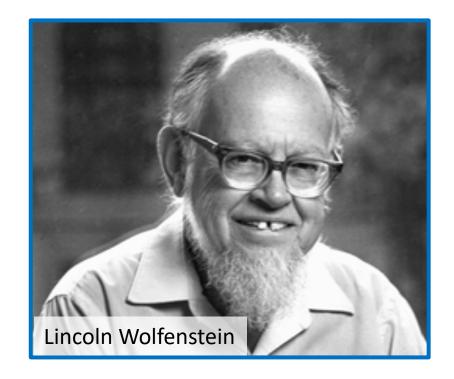
The CKM matrix V_{CKM} - 3 Generations



• Wolfenstein parametrization: V_{CKM} =

$$\begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

1 complex degree of freedom
CP violating phase



• It follows from unitarity: $V_{CKM}^{\dagger} V_{CKM} = 1$

The CKM matrix and unitarity triangle

- The CKM is a mixing matrix, ie. a complex rotation in 3x3 flavour space
 - This implies that the matrix is unitary: $V_{CKM}^{\dagger} V_{CKM} = 1$

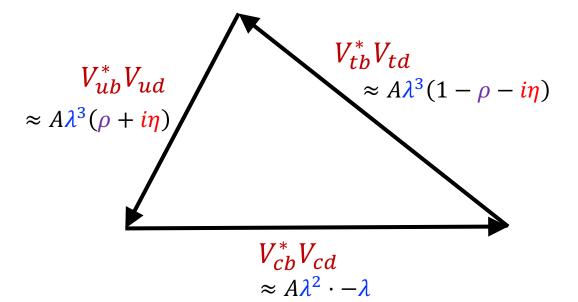
$$\begin{pmatrix} V_{ud}^* & V_{cd}^* & V_{td}^* \\ V_{us}^* & V_{cs}^* & V_{ts}^* \\ V_{ub}^* & V_{cb}^* & V_{tb}^* \end{pmatrix} \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Triangle in the complex plane:

- There are 9 orthonormality equations
 - Example: $V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0$

• Wolfenstein parametrization:

$$V_{CKM} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$



The CKM matrix and unitarity triangle

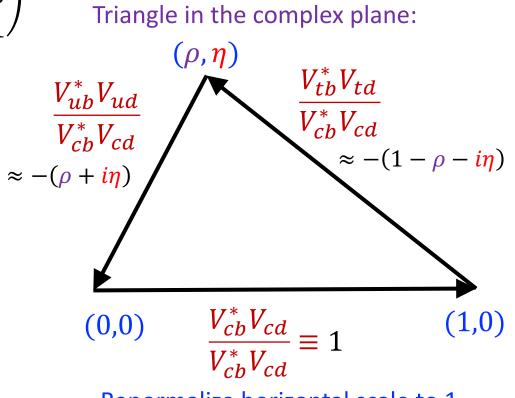
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Renormalize horizontal scale to 1

• CKM in terms of *phases*:

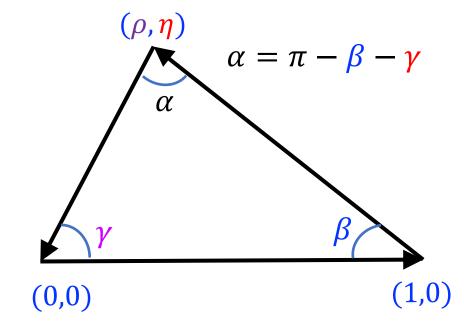
$$V_{CKM} = \begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ -|V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}|e^{-i\beta} & -|V_{ts}|e^{i\beta_s} & |V_{tb}| \end{pmatrix}$$

- There are 9 orthonormality equations
 - 9 complex numbers: 9 real + 9 imaginary
 - 5 unobservable *relative* quark phases: $\psi'_i \rightarrow e^{\phi_i} \psi_i$
 - 18 9 5 = 4 degrees of freedom
- Wolfenstein parametrization:

$$V_{CKM} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

$$V_{CKM}^{\dagger} V_{CKM} = 1$$

Triangle in the complex plane:



- There are 4 degrees of freedom:
 - 3 real (Euler angles) and one phase

• CKM in terms of *phases*:

$$V_{CKM} = \begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ -|V_{cd}| & |V_{cs}| & |V_{cb}| \end{pmatrix}$$

$$V_{CKM} = \begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}|e^{-i\gamma} \\ |V_{cd}|e^{-i\beta} & -|V_{ts}|e^{i\beta_s} & |V_{tb}| \end{pmatrix}$$

$$V_{tb} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

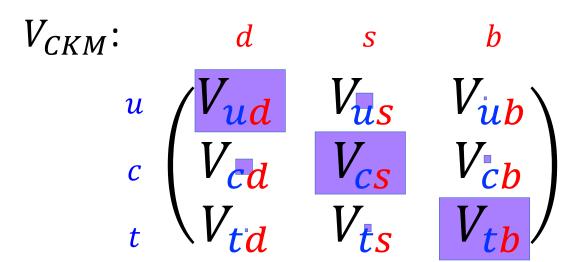
Triangle in the complex plane:

$$V_{CKM} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

Triangle in the complex plane:

$$V_{CKM} = \begin{pmatrix} V_{tb} & V_{cKM} & = 1 \\ V_{tb} & V_{tb} &$$

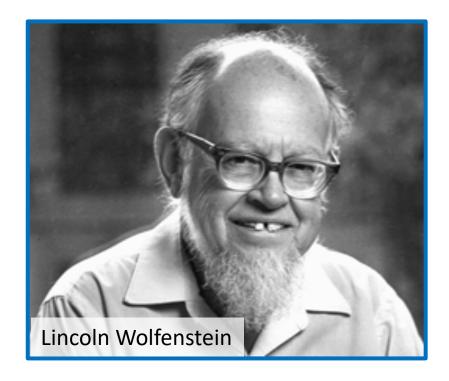
The CKM matrix V_{CKM} - 3 Generations



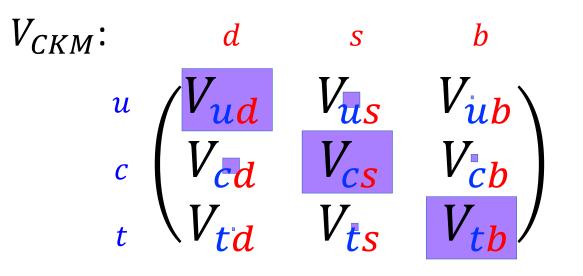
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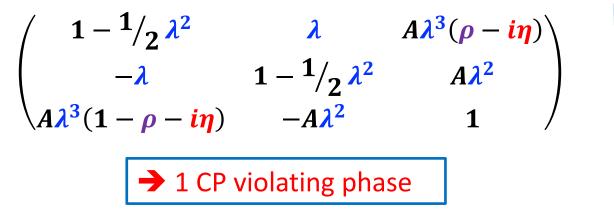
➔ 1 CP violating phase

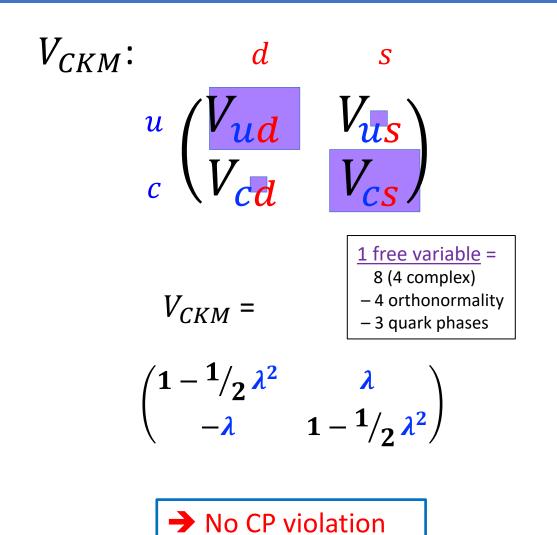


The CKM matrix V_{CKM} - 3 vs 2 Generations



Wolfenstein parametrization: V_{CKM} =

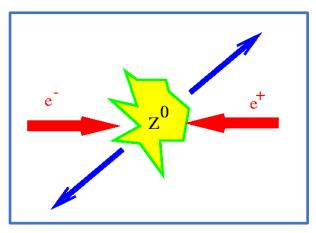


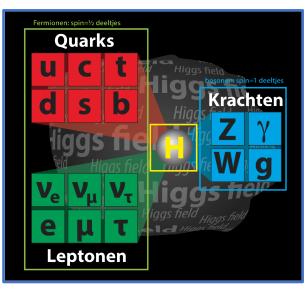


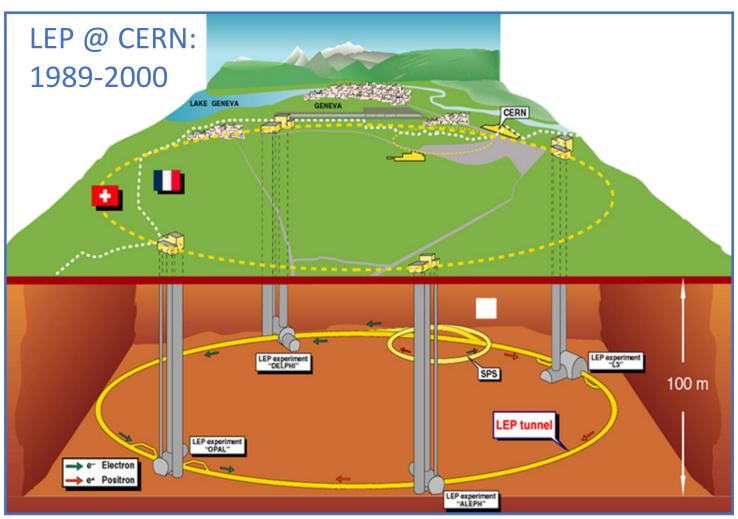
• 3 generations is the minimal particle content to generate CP violation (In Standard Model).

3 Generations of particles – How do we know?

LEP: The heavy Z boson decays into 3 light neutrino types.



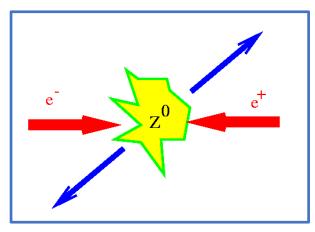


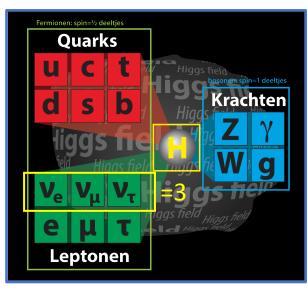


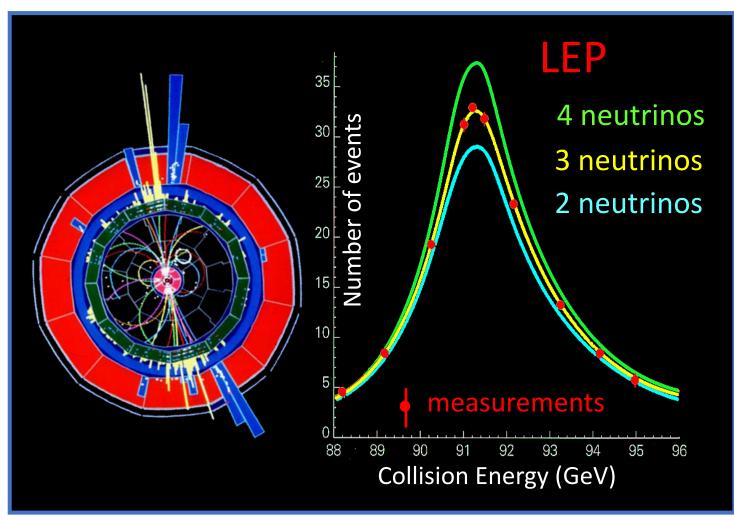
• No additional weakly interacting light fermion generations.

3 Generations of particles – How do we know?

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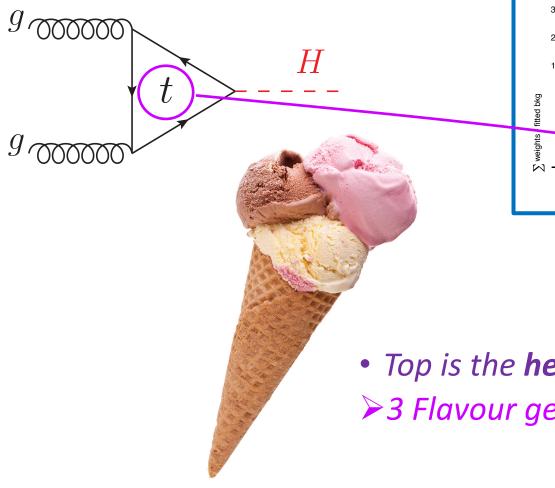


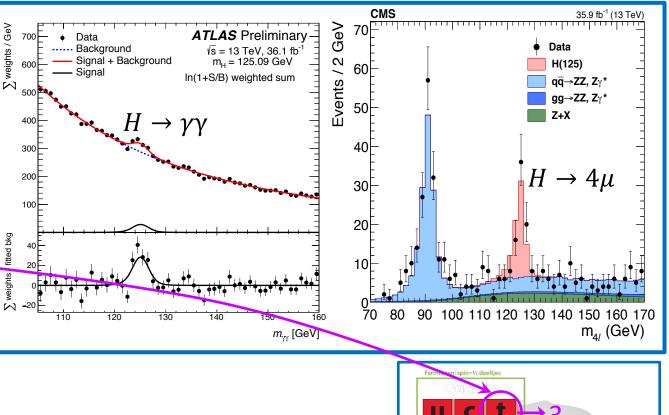
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3 Generations of particles – How do we know?

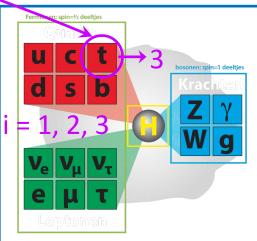
LHC: Higgs production:

Loop diagram is proportional to the mass of the heaviest fermion.

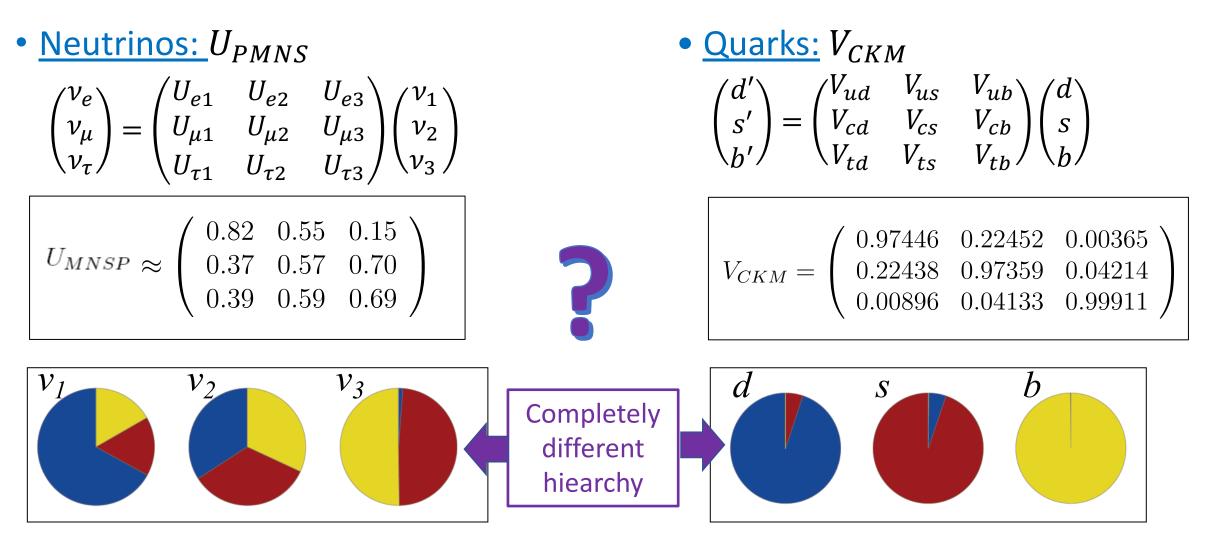


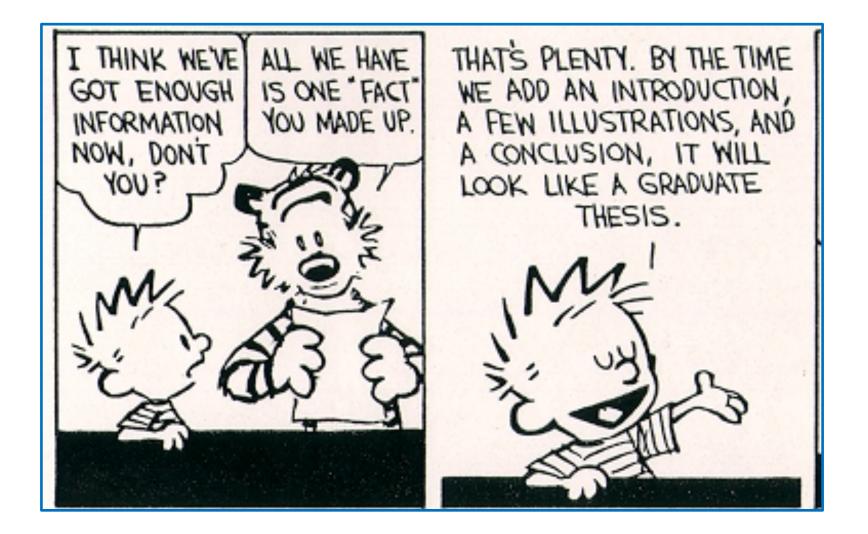


Top is the *heaviest fermion* flavour.
▶3 Flavour generations



- Equivalent of CKM-Matrix V_{CKM} for leptons is PMNS-Matrix
 - Pontecorvo-Maki-Nakagawa-Sakata matrix: U_{PMNS}





Contents per Week:

- 1. CP Violation
 - a) Discrete Symmetries
 - b) CP Violation in the Standard Model
 - c) Jarlskog Invariant and Baryogenesis

2. B-Mixing

- a) CP violation and Interference
- b) B-mixing and time dependent CP violation
- c) Experimental Aspects: LHC vs B-factory

3. B-Decays

- a) Effective Hamiltonian
- b) Lepton Flavour Non-Universality



Flavour Physics and CP Violation

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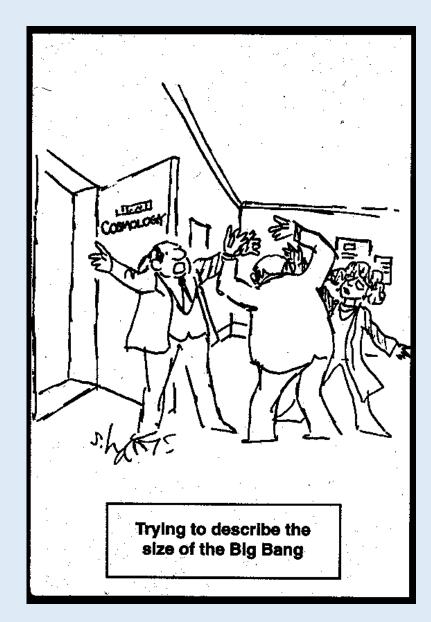
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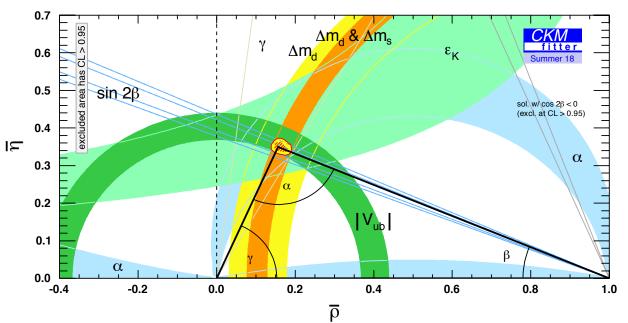
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How large is CP violation?

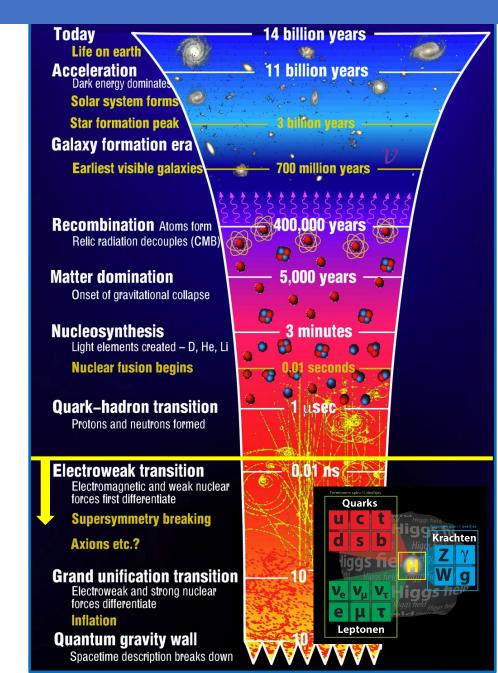
- Large CP violation requires *large mixing* and *large phases* in the CKM matrix.
 - Surface of unitarity triangle
 - Jarlskog invariant: $J = 3 \times 10^{-5}$
- CP violation also requires three generations with non-zero quark masses
 - In fact, *different* masses are required:
 - $m_u \neq m_c$; $m_c \neq m_t$; $m_t \neq m_u$
 - $m_d \neq m_s$; $m_s \neq m_b$; $m_b \neq m_d$
- Jarlskog criterion (1987) for amount of CP violation:

 $\frac{-\det[M_u M_u^{\dagger}, M_d M_d^{\dagger}] = 2 \, i \, J \, (m_t^2 - m_c^2) (m_c^2 - m_u^2) (m_u^2 - m_t^2) }{\times (m_b^2 - m_s^2) (m_s^2 - m_d^2) (m_d^2 - m_b^2) } \times (m_b^2 - m_s^2) (m_s^2 - m_d^2) (m_d^2 - m_b^2) }$





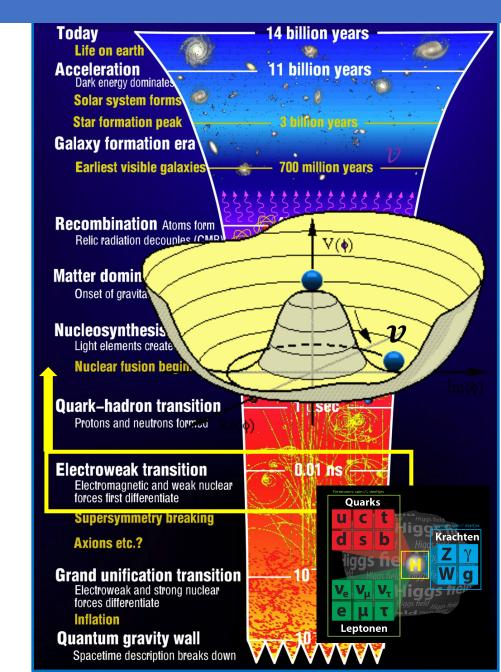
• W interaction flavour universal $\mathcal{L}_W = \frac{g}{\sqrt{2}} u'_L \gamma_\mu W^\mu d'_L$



$SU(2) \rightarrow Higgs vev$

- W interaction flavour universal $\mathcal{L}_W = \frac{g}{\sqrt{2}} u'_L \gamma_\mu W^\mu d'_L$
- Higgs interaction not flavour universal

 $\mathcal{L}_{H} = Y_{ij}^{d} \left(\overline{u'_{i}}, \overline{d'_{i}} \right)_{L} \begin{pmatrix} 0 \\ v \end{pmatrix} d'_{jR} + Y_{ij}^{u} \left(\overline{u'_{i}}, \overline{d'_{i}} \right)_{L} \begin{pmatrix} v \\ 0 \end{pmatrix} u'_{jR}$



$SU(2) \rightarrow Higgs vev \rightarrow Origin of Mass$

- W interaction flavour universal $\mathcal{L}_W = \frac{g}{\sqrt{2}} u'_L \gamma_\mu W^\mu d'_L$
- Higgs interaction not flavour universal

$$\mathcal{L}_{H} = Y_{ij}^{d} \left(\overline{u'_{i}}, \overline{d'_{i}} \right)_{L} \begin{pmatrix} 0 \\ v \end{pmatrix} d'_{jR} + Y_{ij}^{u} \left(\overline{u'_{i}}, \overline{d'_{i}} \right)_{L} \begin{pmatrix} v \\ 0 \end{pmatrix} u'_{jR}$$

• Mass vs Interaction states:

$$u_i = (V^u)_{ij} u'_j \qquad d_i = (V^d)_{ij} d'_j$$

• Amount of CP violation:

$$det[M_u M_u^{\dagger}, M_d M_d^{\dagger}] = 2 i J (m_t^2 - m_c^2) (m_c^2 - m_u^2) (m_u^2 - m_t^2) \times (m_b^2 - m_s^2) (m_s^2 - m_d^2) (m_d^2 - m_b^2)$$

$SU(2) \rightarrow Higgs vev \rightarrow Origin of Mass \rightarrow Origin of CP violation?$

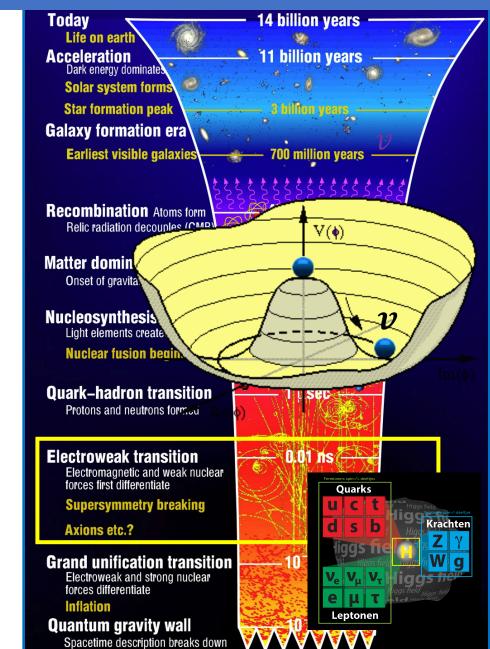
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 - $\mathcal{L}_{H} = Y_{ij}^{d} \left(\overline{u'_{i}}, \overline{d'_{i}} \right)_{L} \begin{pmatrix} 0 \\ v \end{pmatrix} d'_{jR} + Y_{ij}^{u} \left(\overline{u'_{i}}, \overline{d'_{i}} \right)_{L} \begin{pmatrix} v \\ 0 \end{pmatrix} u'_{jR}$
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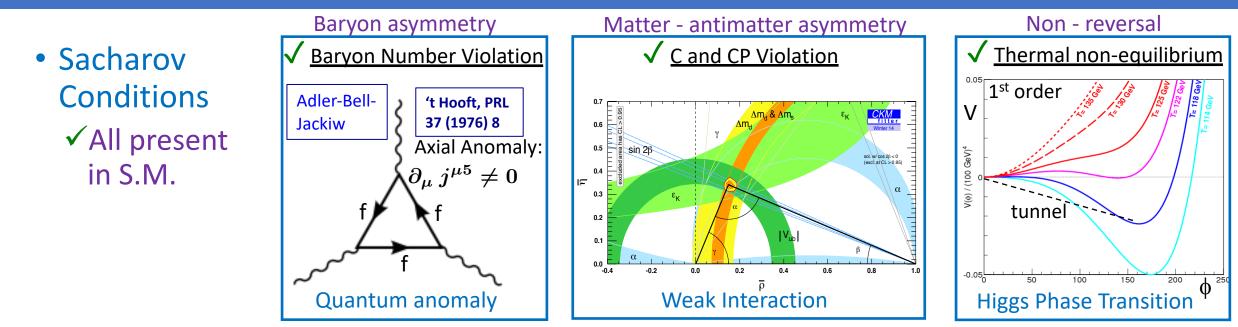
• Amount of CP violation:

 $det[M_u M_u^{\dagger}, M_d M_d^{\dagger}] = 2 i J (m_t^2 - m_c^2)(m_c^2 - m_u^2)(m_u^2 - m_t^2)$ $\times (m_b^2 - m_s^2)(m_s^2 - m_d^2)(m_d^2 - m_b^2)$

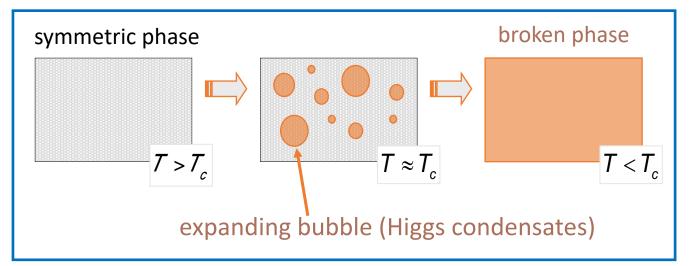
- Does the Standard Model include CP violation before symmetry breaking?
 - Is CP violation perhaps an emergent phenomenon?

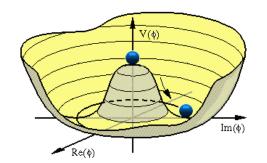


The Baryogenesis Puzzle – Electroweak Baryogenesis?

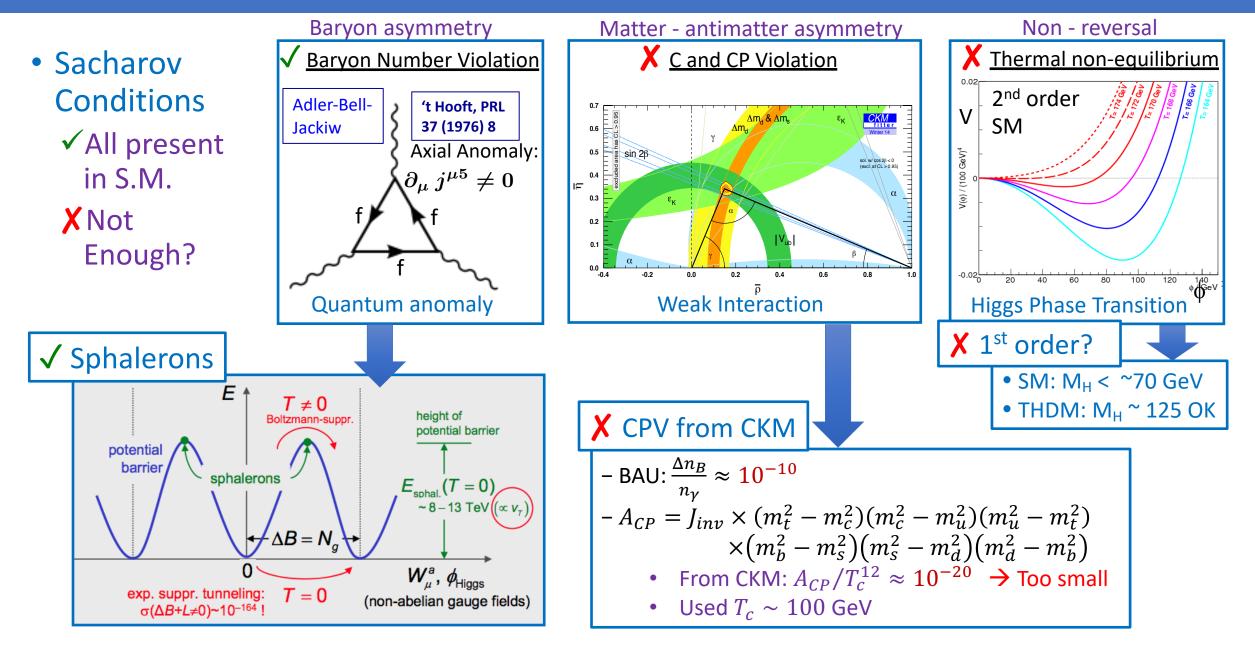


• Baryogenesis from Higgs symmetry breaking?



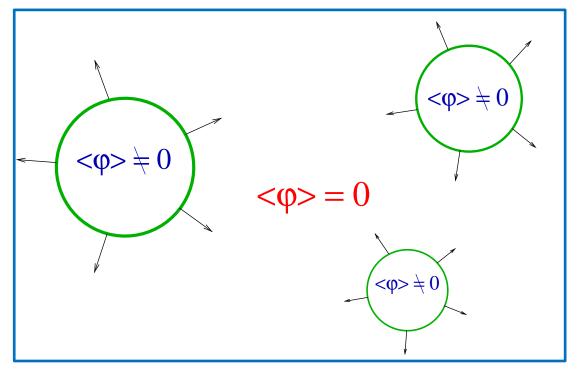


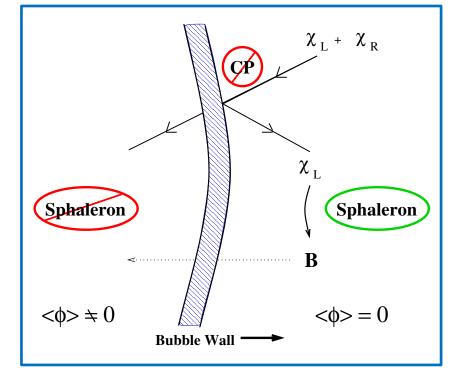
The Baryogenesis Puzzle – Electroweak Baryogenesis?



The Baryogenesis Puzzle – Electroweak Baryogenesis?

Baryon production in Expanding bubbles of broken phase In a medium of opposite to in physice to Deutsche Physika figente of estimate in the physical in the physical in the physical interval interval interval interval interval in the physical interval i





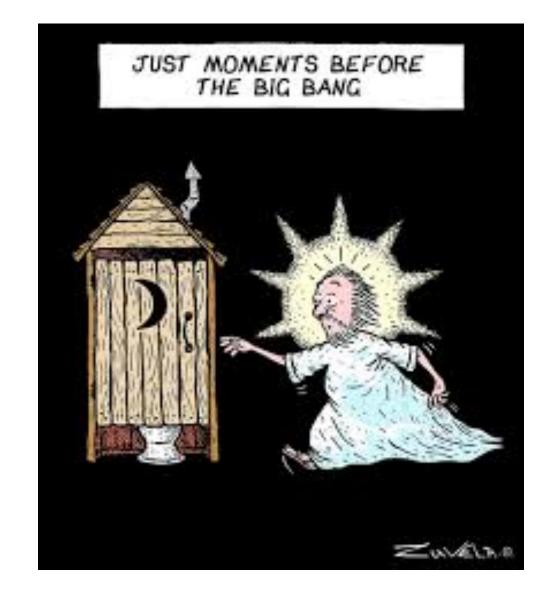
→ Was the phase transition in the early universe of 1st order?

CP

→ Higgs potential?

- → If new physics is abundant in thermal plasma of early universe: → Likely to be of TeV energy scale.

Alternative Explanation...



Flavour Physics and CP Violation

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