



QCDNUM 17-01-13

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Fast interpolation in QCDNUM-17-01-13

- The interpolation algorithm is split in three parts:
 1. Set-up an interpolation mesh and store weights for each interpolation point
 2. Store function value for all the mesh points (take mesh overlaps into account)
 3. Interpolate by computing a weighted sum of function values over each mesh
- Efficient when more than one function is interpolated for a given point or list of points (set-up the interpolation only once for all functions)
- Efficient when meshes of a list of points do overlap (no redundant function calls in the overlaps)
- Gain speed by very fast addressing of pdf tables
- Steps 1.2.3 above are packed inside each of the present routines
- A future version of the toolbox will make steps 1.2.3 separately available for fast interpolation of any user-defined function

NB: an interpolation mesh is an $n_x \times n_q$ subgrid around the interpolation point e.g. 3×3 for quadratic interpolation

The new interpolation routines

Old Name	New Name
FSNSXQ	BVALXQ(<i>iset</i> , <i>id</i> , <i>x</i> , <i>q</i> , <i>ichk</i>)
FVALXQ	FVALXQ(<i>iset</i> , <i>id</i> , <i>x</i> , <i>q</i> , <i>ichk</i>)
FPDFXQ	ALLFXQ(<i>iset</i> , <i>x</i> , <i>q</i> , <i>f</i> , <i>n</i> , <i>ichk</i>)
FSUMXQ	SUMFXQ(<i>iset</i> , <i>c</i> , <i>isel</i> , <i>x</i> , <i>q</i> , <i>ichk</i>)
PDFLST	FFLIST(<i>iset</i> , <i>c</i> , <i>isel</i> , <i>x</i> , <i>q</i> , <i>f</i> , <i>n</i> , <i>ichk</i>)
PDFTAB	FTABLE(<i>iset</i> , <i>c</i> , <i>isel</i> , <i>x</i> , <i>nx</i> , <i>q</i> , <i>nq</i> , <i>tbl</i> , <i>ichk</i>)

- ✓ Most routines are (much) faster than before
- ✓ All routines can access extra pdfs (if present in the pdf set)
- ✓ Singlet-nonsinglet selection via the *isel* flag (see later)
- ✓ Speed-up by optionally switching-off checks (see later)

Calculate weighted sum $\sum_i^{n_f} e_i^2 x(q_i + \bar{q}_i)$ for 2400 x-Q² points

PDF accessed in one call	Subroutine	Speed gain wrt 01-12	CPU (arbitrary units)
Single basis pdf	BVALIJ	6	
Single flavour pdf	FVALIJ	9	
All flavour pdfs	ALLFIJ	6	
Linear combination	SUMFIJ	11	
Single basis pdf	BVALXQ	2	
Single flavour pdf	FVALXQ	4	
All flavour pdfs	ALLFXQ	2	
Linear combination	SUMFXQ	19	
List	FFLIST	1	
Table (here 60x40)	FTABLE	2	

NB: Timing profile depends much on what you calculate

Singlet-nonsinglet selection (1)

```
SUMFXQ( iset, c, isel, x, q, ichk )  
FFLIST( iset, c, isel, x, q, f, n, ichk )  
FTABLE( iset, c, isel, x, nx, q, nq, tbl, ichk )
```


- **c** (-6:6) array with quark and antiquark coefficients
- **isel** selection flag that defines what is returned

isel = 0 Gluon
 1 Quark linear combination defined by **c**
 2-8 Singlet-nonsinglet selection (next slides)
 12+i Extra pdf xf_i if present in **iset**

Singlet-nonsinglet selection (2)

Reminder QCDNUM basis pdfs

$$q_i^\pm \equiv q_i \pm \bar{q}_i$$

	$ e_1^+\rangle = \sum_{i=1}^{n_f} (q_i + \bar{q}_i)$	singlet
	$ e_1^-\rangle = \sum_{i=1}^{n_f} (q_i - \bar{q}_i)$	valence
 nonsinglet	$ e_2^\pm\rangle = u^\pm - d^\pm$	$n_f \geq 3$
	$ e_3^\pm\rangle = u^\pm + d^\pm - 2s^\pm$	$n_f \geq 3$
	$ e_4^\pm\rangle = u^\pm + d^\pm + s^\pm - 3c^\pm$	$n_f \geq 4$
	$ e_5^\pm\rangle = u^\pm + d^\pm + s^\pm + c^\pm - 4b^\pm$	$n_f \geq 5$
	$ e_6^\pm\rangle = u^\pm + d^\pm + s^\pm + c^\pm + b^\pm - 5t^\pm$	$n_f \geq 6$

Singlet-nonsinglet selection (3)

- The linear combination **c (-6 : 6)** in terms of basis pdfs:

$$|xq\rangle = \overbrace{d_1^+ |xe_1^+\rangle}^{\text{si}} + \overbrace{\sum_{i=2}^{n_f} d_i^+ |xe_i^+\rangle}^{\text{ns}^+} + \overbrace{d_1^- |xe_1^-\rangle}^{\text{va}} + \overbrace{\sum_{i=2}^{n_f} d_i^- |xe_i^-\rangle}^{\text{ns}^-}$$

- isel**: Select combination of singlet and nonsinglet terms

$$\begin{array}{llll} |1\rangle = \text{all terms} & |2\rangle = \text{si} & |3\rangle = \text{all ns} & |4\rangle = \text{ns}^+ \\ |5\rangle = \text{va} + \text{ns}^- & |6\rangle = \text{ns}^- & |7\rangle = \text{va} & |8\rangle = d_1^+ |xg\rangle \end{array}$$

- Useful for structure function calculations e.g.:

$$\begin{array}{ll} F_2^{\text{LO}} & = |1\rangle \\ F_2^{\text{NLO}} & = C_g \otimes |8\rangle + C_s \otimes |2\rangle + C_{\text{ns}} \otimes |3\rangle \\ F_2^{\text{NNLO}} & = C_g \otimes |8\rangle + C_s \otimes |2\rangle + C_+ \otimes |4\rangle + C_- \otimes |5\rangle \end{array}$$

Speed-up goody: switch-off checks

```
BVALXQ|IJ( iset, id, x|ix, q|iq, ichk )  
FVALXQ|IJ( iset, id, x|ix, q|iq, ichk )  
ALLFXQ|IJ( iset, x|ix, q|iq, f, n, ichk )  
SUMFXQ|IJ( iset, c, isel, x|ix, q|iq, ichk )
```

- The **ichk** flag controls the error checking:

0 Return a null when x or qmu2 are outside the grid
+1 Fatal error when x or qmu2 are outside the grid
-1 As above, but do not check the input iset and id

NEW

- Useful to speed-up loops (most effective for **BVALIJ**)

```
pdf(1) = BVALIJ( iset, id, ix(1), iq(1), +1 )  
do k = 2,n  
  pdf(k) = BVALIJ( iset, id, ix(k), iq(k), -1 )  
enddo
```


Restricted access to pdfs (1)

- QCDNUM can have pdf sets with different evolution parameters in memory

```
iset = 0      Current (active) parameters that steer QCDNUM
      = 1-24   Parameters stored with a pdf set
```

- You can only access pdf sets evolved with the current parameters
- So you may have to first activate the parameters of your favourite pdf set
- Looks clumsy but protects against using incompatible pdfs in a calculation
- There are four routines to manage sets of evolution parameters

```
USEPAR( iset )   Activate parameter set (make them current parameters)
KEYPAR( iset )   Get key of parameter set (equal key = equal parameters)
PUSHCP          Push current parameters on a stack
PULLCP          Pull current parameters from a stack
```

Restricted access to pdfs (2)

- The routines `USEPAR` and `PULLCP` are slow because they re-initialise QCDUM
- Always calling `USEPAR` is therefore not a very good idea ...

```
call USEPAR(iset)
call ALLFXQ(iset, ... )
```

- Use keys to first check if a pdf set is evolved with the current parameters
 - Parameter keys are (un)equal when parameter sets are (un)equal

```
if( KEYPAR(iset) .eq. KEYPAR(0) ) then
  call ALLFXQ(iset, ...) !get pdfs directly
else
  call PUSHCP           !store current parameters
  call USEPAR(iset)     !activate parameters of iset
  call ALLFXQ(iset, ...) !get pdfs
  call PULLCP           !restore current parameters
endif
```

- If your pdf sets have the same parameters you don't need all this of course!

Progress on the C++ interface

- Valerio sent me yesterday a [17-01-13](#) version with a C++ interface and test-jobs that worked out-of-the-box
- Presently I am setting-up the Autotool part of the release script to handle the C++ code correctly
- For the moment there exists an interface to QCDNUM [out-of-the-box routines](#), and the add-ons [ZMSTF](#) and [HQSTF](#)
- Waiting for Renats [QCD-QED stand-alone code](#) to turn it into an add-on package, also with a C++ interface
- Interface to the QCDNUM [toolbox](#) will come later
- Will soon start testing all existing C++ routines one-by-one

QCDNUM joblist beyond 17-01-13

- C++ interface coming soon (my thanks to Valerio Bertone)
- Cleanup code to have one evolution routine (now there are two)
- VFNS evolution starting above charm threshold (intrinsic charm)
- Re-enable cuts
- Toolbox improvements (make it more user-function driven)
- Upgrade polarised and time-like evolution to NNLO
- ...

You are welcome to add to this list or
make suggestions to prioritise it