



# SIGHTSEEING IN THE LANDSCAPE

# CONTENTS

- ✿ Landscape remarks  
(physics/06041340, Dutch version 1998)
- ✿ RCFT orientifolds  
(with Huiszoon,Fuchs, Schweigert,Walcher)
- ✿ 2003-2004 results  
(with Dijkstra,Huiszoon)
- ✿ 2005-2006 results  
(with Anastasopoulos,Dijkstra,Kiritsis, hep-th/0605226)

# 1984-2006: A SLOW REVOLUTION

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A.N. Schellekens, “The landscape *avant la lettre*” (physics/06041340, Dutch version 1998)

# SO WHAT CAN WE STILL DO?

- ✿ Explore unknown regions of the landscape
- ✿ Establish the likelihood of standard model features  
(gauge group, three families, ....)
- ✿ Convince ourselves that standard model is a plausible vacuum
- ✿ Understand vacuum statistics
- ✿ Understand cosmological likelihood
- ✿ Understand “anthropicity”



ORIENTIFOLDS  
OF  
GEPNER MODELS

# EARLIER FOOTPRINTS

- C. Angelantonj, M. Bianchi, G. Pradisi, A. Sagnotti and Y. S. Stanev, Phys. Lett. B **387** (1996) 743 [arXiv:hep-th/9607229].
- R. Blumenhagen and A. Wisskirchen, Phys. Lett. B **438**, 52 (1998) [arXiv:hep-th/9806131].
- G. Aldazabal, E. C. Andres, M. Leston and C. Nunez, JHEP **0309**, 067 (2003) [arXiv:hep-th/0307183].
- I. Brunner, K. Hori, K. Hosomichi and J. Walcher, arXiv:hep-th/0401137.
- R. Blumenhagen and T. Weigand, JHEP **0402** (2004) 041 [arXiv:hep-th/0401148].
- G. Aldazabal, E. C. Andres and J. E. Juknevich, JHEP **0405**, 054 (2004) [arXiv:hep-th/0403262].

# THE LONG ROAD TO THE CHIRAL SSM

- ⌘ Angelantonj, Bianchi, Pradisi, Sagnotti, Stanev (1996)  
*Chiral spectra from Orbifold-Orientifolds*
- ⌘ Aldazabal, Franco, Ibanez, Rabadan, Uranga (2000)  
Blumenhagen, Görlich, Körs, Lüst (2000)  
Ibanez, Marchesano, Rabadan (2001)  
*Non-supersymmetric SM-Spectra with RR tadpole cancellation*
- ⌘ Cvetic, Shiu, Uranga (2001)  
*Supersymmetric SM-Spectra with chiral exotics*
- ⌘ Blumenhagen, Görlich, Ott (2002)  
Honecker (2003)  
*Supersymmetric Pati-Salam Spectra with brane recombination*
- ⌘ Dijkstra, Huiszoon, Schellekens (2004)  
*Supersymmetric Standard Model (Gepner Orientifolds)*
- ⌘ Honecker, Ott (2004)  
*Supersymmetric Standard Model ( $Z_6$  orbifold/orientifold)*

# GEPNER MODELS

Building Blocks:  
Minimal N=2 CFT

$$c = \frac{3k}{k+2}, \quad k = 1, \dots, \infty$$

168 ways of solving  $\sum_i c_{k_i} = 9$

Spectrum:

$$h_{l,m} = \frac{l(l+2) - m^2}{4(k+2)} + \frac{s^2}{8}$$

$$(l = 0, \dots, k; \quad q = -k, \dots, k+2; \quad s = -1, 0, 1, 2)$$

(plus field identification)

4( $k+2$ ) simple currents

# TENSORING

- ✿ Preserve world-sheet susy
- ✿ Preserve space-time susy (GSO)
- ✿ Use surviving simple currents to build MIPFs
- ✿ This yields one point in the moduli space of a Calabi-Yau manifold

# SELECTING MIPFs AND ORIENTIFOLDS

Each tensor product has a discrete group  $\mathcal{G}$   
of simple currents:  $J \cdot a = b$

Choose:

- {
  - ✿ A subgroup  $\mathcal{H}$  of  $\mathcal{G}$
  - ✿ A rational matrix  $X_{\alpha\beta}$  defined on  $\mathcal{H}$
  
- {
  - ✿ An element  $K$  of  $\mathcal{G}$
  - ✿ A set of signs  $\beta_K(J)$  defined on  $\mathcal{H}$

# A MIPF

$$\begin{aligned} & (0+2)^2 + (1+3)^2 + (4+6)*(13+15) + (5+7)*(12+14) \\ & + (8+10)^2 + (9+11)^2 + (12+14)*(5+7) + (13+15)*(4+6) \\ & + (16+18)*(25+27) + (17+19)*(24+26) + (20+22)^2 + (21+23)^2 \\ & + (24+26)*(17+19) + (25+27)*(16+18) + (28+30)^2 + (29+31)^2 \\ & + (32+34)^2 + (33+35)^2 + (36+38)*(45+47) + (37+39)*(44+46) \\ & + (40+42)^2 + (41+43)^2 + (44+46)*(37+39) + (45+47)*(36+38) \\ & + (48+50)*(57+59) + (49+51)*(56+58) + (52+54)^2 + (53+55)^2 \\ & + (56+58)*(49+51) + (57+59)*(48+50) + (60+62)^2 + (61+63)^2 \end{aligned}$$

....

$$\begin{aligned} & + 2*(2913)*(2915) + 2*(2914)*(2912) + 2*(2915)*(2913) \\ & + 2*(2916)^2 + 2*(2917)^2 + 2*(2918)^2 + 2*(2919)^2 \\ & + 2*(2920)^2 + 2*(2921)^2 + 2*(2922)^2 + 2*(2923)^2 \\ & + 2*(2924)*(2926) + 2*(2925)*(2927) + 2*(2926)*(2924) \\ & + 2*(2927)*(2925) + 2*(2928)^2 + 2*(2929)^2 + 2*(2930)^2 \\ & + 2*(2931)^2 + 2*(2932)*(2934) + 2*(2933)*(2935) \\ & + 2*(2934)*(2932) + 2*(2935)*(2933) + 2*(2936)*(2938) \\ & + 2*(2937)*(2939) + 2*(2938)*(2936) + 2*(2939)*(2937) \\ & + 2*(2940)^2 + 2*(2941)^2 + 2*(2942)^2 + 2*(2943)^2 \end{aligned}$$

# BOUNDARIES AND CROSSCAPS\*

## ✿ Boundary coefficients

$$R_{[a,\psi_a](m,J)} = \sqrt{\frac{|\mathcal{H}|}{|\mathcal{C}_a||\mathcal{S}_a|}} \psi_a^*(J) S_{am}^J$$

## ✿ Crosscap coefficients

$$U_{(m,J)} = \frac{1}{\sqrt{|\mathcal{H}|}} \sum_{L \in \mathcal{H}} e^{\pi i (h_K - h_{KL})} \beta_K(L) P_{LK,m} \delta_{J,0}$$

\**Huiszoon, Fuchs, Schellekens, Schweigert, Walcher (2000)*

# COEFFICIENTS

✿ Klein bottle

$$K^i = \sum_{m,J,J'} \frac{S^i{}_m U_{(m,J)} g_{J,J'}^{\Omega,m} U_{(m,J')}}{S_{0m}}$$

✿ Annulus

$$A^i_{[a,\psi_a][b,\psi_b]} = \sum_{m,J,J'} \frac{S^i{}_m R_{[a,\psi_a](m,J)} g_{J,J'}^{\Omega,m} R_{[b,\psi_b](m,J')}}{S_{0m}}$$

✿ Moebius

$$M^i_{[a,\psi_a]} = \sum_{m,J,J'} \frac{P^i{}_m R_{[a,\psi_a](m,J)} g_{J,J'}^{\Omega,m} U_{(m,J')}}{S_{0m}}$$

$$g_{J,J'}^{\Omega,m} = \frac{S_{m0}}{S_{mK}} \beta_K(J) \delta_{J',J^c}$$

# PARTITION FUNCTIONS

✿ Closed

$$\frac{1}{2} \left[ \sum_{ij} \chi_i(\tau) Z_{ij} \chi_i(\bar{\tau}) + \sum_i K_i \chi_i(2\tau) \right]$$

✿ Open

$$\frac{1}{2} \left[ \sum_{i,a,n} N_a N_b A^i{}_{ab} \chi_i\left(\frac{\tau}{2}\right) + \sum_{i,a} N_a M^i{}_a \hat{\chi}_i\left(\frac{\tau}{2} + \frac{1}{2}\right) \right]$$

$N_a$ : Chan-Paton multiplicity

# TADPOLES & ANOMALIES

- ✿ Tadpole cancellation condition:

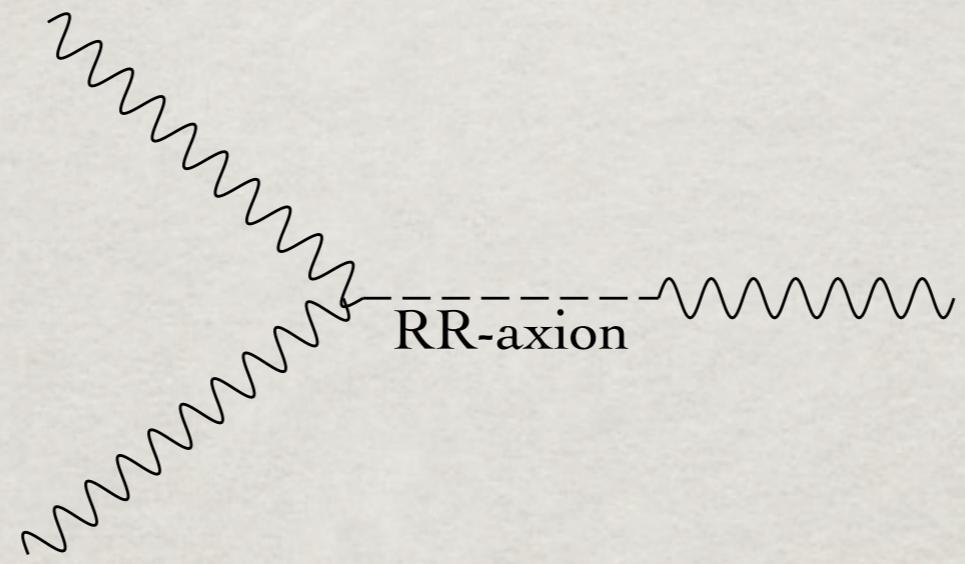
$$\sum_b N_b R_{b(m,J)} = 4\eta_m U_{(m,J)}$$

- ✿ Cubic  $\text{Tr}F^3$  anomalies cancel
- ✿ Remaining anomalies by Green-Schwarz mechanism
- ✿ In rare cases, additional conditions for global anomaly cancellation\*

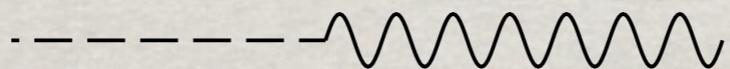
\**Gato-Rivera, Schellekens (2005)*

# ABELIAN MASSES

Green-Schwarz mechanism



Axion-Vector boson vertex



Generates mass vector bosons of anomalous symmetries

(e.g.  $B + L$ )

But may also generate mass for non-anomalous ones

$(Y, B - L)$

# SCOPE OF THE SEARCH

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- ✿ 168 Gepner models

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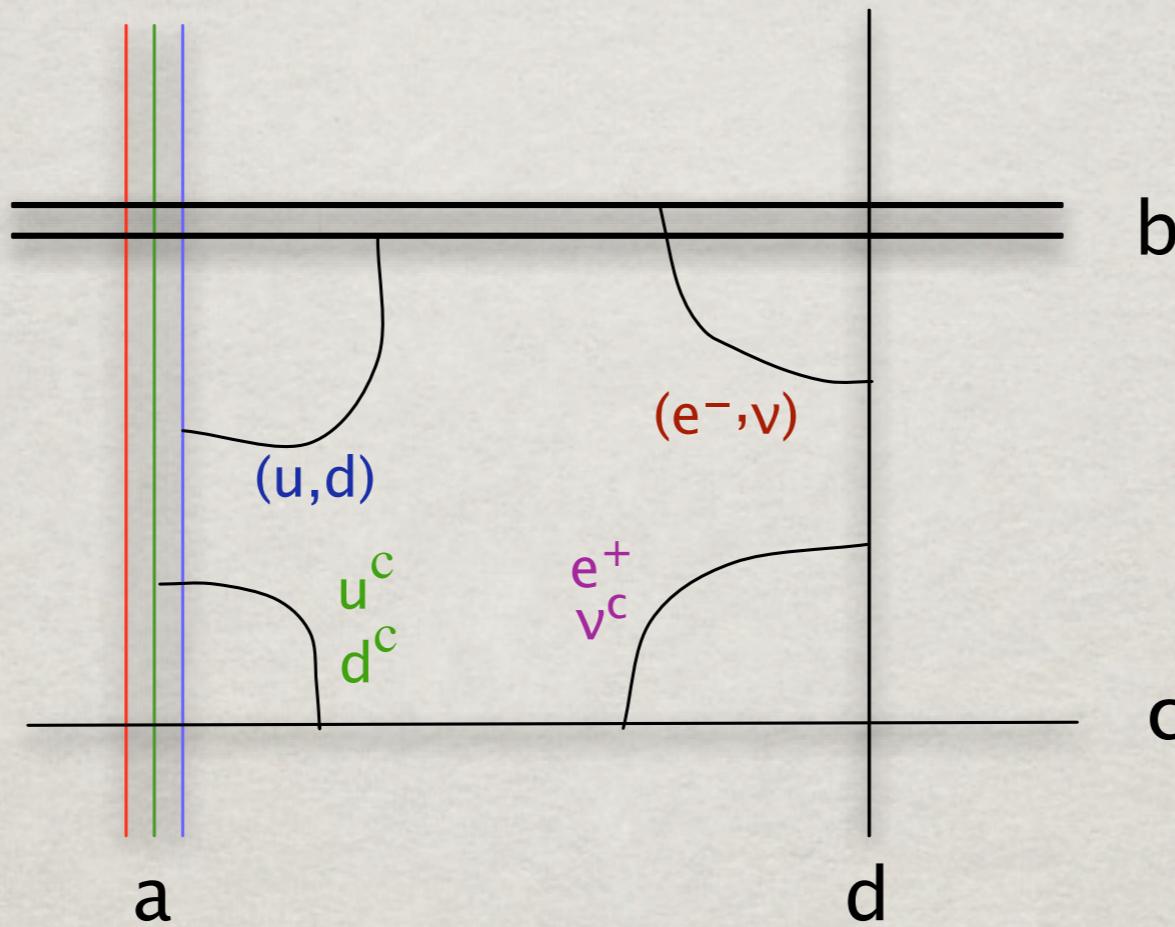
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**Essential to decide what to search for!**

# WHAT TO SEARCH FOR

## The Madrid model



Chiral  $SU(3) \times SU(2) \times U(1)$  spectrum:

$$3(u, d)_L + 3u_L^c + 3d_L^c + 3(e^-, \nu)_L + 3e_L^+$$

Y massless

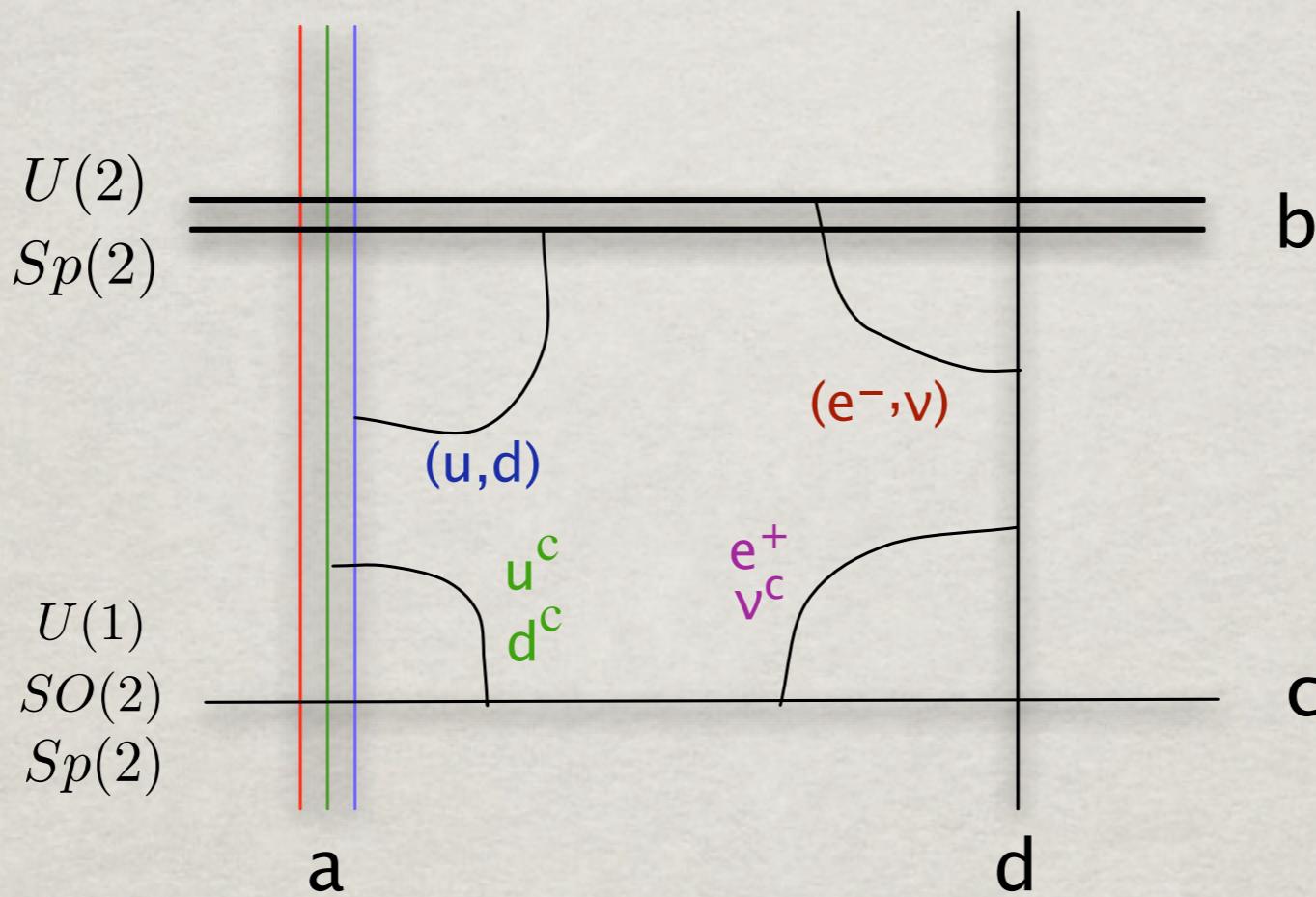
$$Y = \frac{1}{6}Q_a - \frac{1}{2}Q_c - \frac{1}{2}Q_d$$

N=1 Supersymmetry

No tadpoles, global anomalies

# WHAT TO SEARCH FOR

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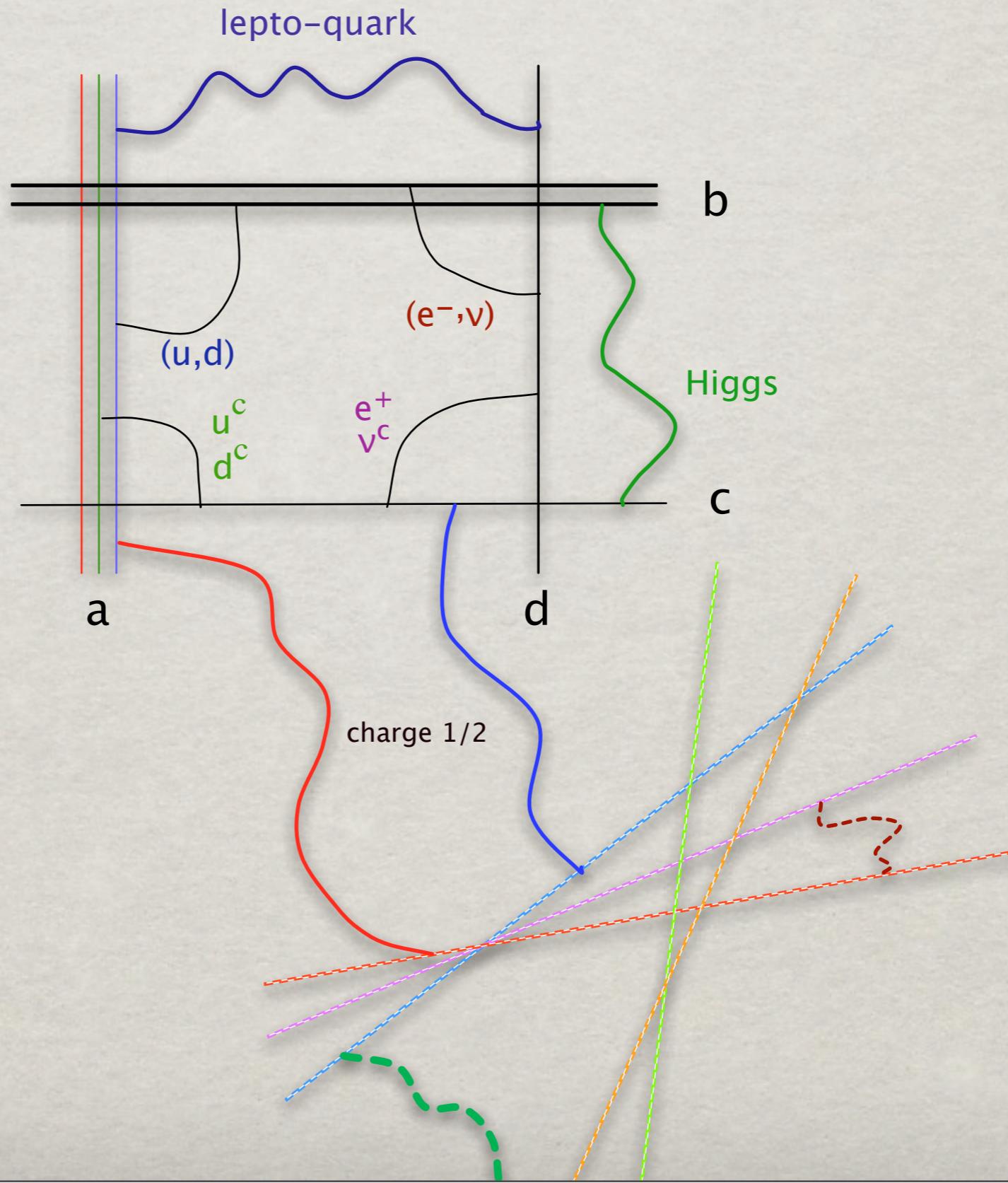
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# THE HIDDEN SECTOR



# STATISTICS

Total number of 4-stack configurations	45761187347637742772 ( $45.7 \times 10^{18}$ )
Total number scanned	4.37522E+19
Total number of SM configurations	45051902 fraction: $1.0 \times 10^{-12}$
Total number of tadpole solutions	1649642 fraction: $3.8 \times 10^{-14}$ (*)
Total number of distinct solutions	211634

(\*) cf. Gmeiner, Blumenhagen, Honecker, Lüst, Weigand: “One in a Billion”

# RCFT orientifolds with Standard Model Spectrum

Tim Dijkstra, Lennaert Huiszoon and Bert Schellekens

On this page you can search through all our supersymmetric, tadpole-free  $D=4$ ,  $N=1$  orientifold vacua with a three family chiral fermion spectrum identical to that of the Standard Model. They were constructed in a semi-systematic way by considering orientifolds of all Gepner Models (see [Phys.Lett.B609:408-417](#) and [Nucl.Phys.B710:3-57](#) for more information). Since the publication of these papers all spectra have been re-analysed and checked for the presence of global (Witten) anomalies. A few cases (less than 1%) needed correction. All spectra in this database are now free from global anomalies, and the total number is 210,782, slightly more than reported in these papers.

As explained in referenced articles the standard model gauge group can be realized in different ways (which we call *types*). In addition to these factors, the gauge group usually has extra *hidden* gauge group factors. Chiral states with one leg in the standard model gauge group are not permitted.

All these models of course have the same *chiral* spectrum for the standard model gauge group, except for the higgs-sector of which we do not know how it is realized in nature.

These models then differ in multiplicities of the non-chiral particles, hidden gauge group, higgs sector coupling constants on the string scale, and others.

To search for your favorite realization you can use the form below to filter our set with an condition. Example:

```
type==0 && nrHidden<2
```

You can consult a [list of valid field names](#). Also much more complicated expressions are possible, see the [syntax description](#).

## Filter form

Two output formats are provided. The first only gives the number of answers, the second lists all the spectra satisfying the search criteria. Be warned that output can be very large and take up to a minute to compile; at the moment we have

Gauge group: U(3) x Sp(2) x Sp(2) x U(1) x Sp(6) x Sp(4) x Sp(2)

Number of representations: 19

```

3 x (V ,V ,0 ,0 ,0 ,0 ,0 ) chirality 3
3 x (V ,0 ,V ,0 ,0 ,0 ,0 ) chirality -3
3 x (0 ,V ,0 ,V ,0 ,0 ,0 ) chirality 3
3 x (0 ,0 ,V ,V ,0 ,0 ,0 ) chirality -3
2 x (V ,0 ,0 ,V ,0 ,0 ,0 )
2 x (0 ,V ,V ,0 ,0 ,0 ,0 )
2 x (V ,0 ,0 ,0 ,V ,0 ,0 )
2 x (V ,0 ,0 ,0 ,0 ,V ,0 )
2 x (V ,0 ,0 ,0 ,0 ,0 ,V )
1 x (0 ,V ,0 ,0 ,V ,0 ,0 )
1 x (0 ,0 ,V ,0 ,V ,0 ,0 )
2 x (0 ,0 ,0 ,V ,0 ,V ,0 )
1 x (0 ,0 ,0 ,0 ,V ,0 ,V )
2 x (0 ,0 ,0 ,0 ,0 ,V ,V )
2 x (0 ,0 ,0 ,0 ,A ,0 ,0 )
1 x (0 ,0 ,0 ,0 ,S ,0 ,0 )
5 x (0 ,0 ,0 ,0 ,0 ,A ,0 )
5 x (0 ,0 ,0 ,0 ,0 ,S ,0 )
1 x (0 ,0 ,0 ,0 ,0 ,0 ,S )

```

#### Summary:

Higgs:	(2,1/2)+(2*,1/2)	2
Non-chiral SM matter (Q,U,D,L,E,N):	0 0 0 0 0 0	0
Adjoints:	0 0 0 0	0
Symmetric Tensors:	0 0 0 0	0
Anti-Symmetric Tensors:	0 0 0 0	0
Lepto-quarks: (3,-1/3),(3,2/3)	1 0	0
Non-SM (a,b,c,d)	12 6 6 4	0
Hidden (Total dimension)	162 (chirality 0)	0

$$\sin^2(\theta_w) = .3610368$$

$$\frac{\alpha_3}{\alpha_2} = .8660246$$

Standard model type: 6  
 Number of factors in hidden gauge group: 0  
 Gauge group: U(3) x Sp(2) x U(1) x U(1)

Number of representations: 19

3 x	(V ,V ,0 ,0 )	chirality 3
3 x	(V ,0 ,V ,0 )	chirality -3
3 x	(V ,0 ,V*,0 )	chirality -3
9 x	(0 ,V ,0 ,V )	chirality 3
5 x	(0 ,0 ,V ,V )	chirality -3
3 x	(0 ,0 ,V ,V*)	chirality -3
2 x	(V ,0 ,0 ,V )	
10 x	(0 ,V ,V ,0 )	
2 x	(Ad,0 ,0 ,0 )	
2 x	(A ,0 ,0 ,0 )	

•••••

Higgs:	(2,1/2)+	2*,1/2)	5				
Non-chiral SM matter	(Q,U,D,L,E,N):	0	0	0	3	1	0
Adjoints:		2	0	9	3		
Symmetric Tensors:		1	10	7	3		
Anti-Symmetric Tensors:		1	14	3	2		
Lepto-quarks:	3,-1/3),	3,2/3)	1	0			
Non-SM	a,b,c,d)	0	0	0	0		
Hidden	Total dimension)	0		(chirality 0)			

$$\sin^2(\theta_w) = .5271853$$

$$\frac{\alpha_3}{\alpha_2} = 3.2320501$$

# UNBIASED SEARCH

Require only:

- ✿ U(3) from a single brane
- ✿ U(2) from a single brane
- ✿ Quarks and leptons, Y from at most four branes
- ✿  $G_{CP} \supset SU(3) \times SU(2) \times U(1)$
- ✿ Chiral  $G_{CP}$  fermions reduce to quarks, leptons  
(plus non-chiral particles) but
- ✿ No fractionally charged mirror pairs
- ✿ Massless Y

# ALLOWED FEATURES

- ✿ (Anti)-quarks from anti-symmetric tensors
- ✿ leptons from anti-symmetric tensors
- ✿ family symmetries
- ✿ non-standard Y-charge assignments
- ✿ Unification (Pati-Salam, (flipped) SU(5), trinification)\*
- ✿ Baryon and/or lepton number violation
- ✿ ....

\*a,b,c,d may be identical

# Chan-Paton gauge group

$$G_{CP} = U(3)_a \times \left\{ \begin{array}{c} U(2)_b \\ Sp(2)_b \end{array} \right\} \times G_c \quad (\times G_d)$$

Embedding of Y:

$$Y = \alpha Q_a + \beta Q_b + \gamma Q_c + \delta Q_d + W_c + W_d$$

Q: Brane charges (for unitary branes)

W: Traceless generators

# CLASSIFICATION

$$Y = \left(x - \frac{1}{3}\right)Q_a + \left(x - \frac{1}{2}\right)Q_b + xQ_C + (x - 1)Q_D$$


Distributed over  
c and d

Allowed values for  $x$

1/2	Madrid model, Pati-Salam, Flipped SU(5)
0	(broken) SU(5)
1	Antoniadis, Kirsits, Tomaras
-1/2, 3/2	
any	Trinification ( $x = 1/3$ ) (orientable)

# RESULTS

- ✿ Searched all MIPFs with  $< 1750$  boundaries  
(4557 of 5403 MIPFs)
- ✿ 19345 chirally different SM embeddings found
- ✿ Tadpole conditions solved in 1900 cases  
(18 “old” ones)

# STATISTICS

Value of x	Total
0	21303612
1/2	124006839*
1	12912
-1/2, 3/2	0
any	1250080

\*Previous search: 45051902

# REALIZATIONS

- ✿ Bottom-Up configuration: any brane configuration that yields 3 chiral families
- ✿ Top-Down configuration: any such configuration realized with boundary states
- ✿ String Vacuum: Top-down configuration with tadpole cancellation (with or without hidden sector)

# BOTTOM-UP vs TOP-DOWN (1)

$x$	Config.	stack <b>c</b>	stack <b>d</b>	Bottom-up	Top-down	Occurrences	Solved
1/2	UUUU	C,D	C,D	27	9	5194	1
1/2	UUUU	C	C,D	103441	434	1056708	31
1/2	UUUU	C	C	10717308	156	428799	24
1/2	UUUU	C	F	351	0	0	0
1/2	UUU	C,D	-	4	1	24	0
1/2	UUU	C	-	215	5	13310	2
1/2	UUUR	C,D	C,D	34	5	3888	1
1/2	UUUR	C	C,D	185520	221	2560681	31
1/2	USUU	C,D	C,D	72	7	6473	2
1/2	USUU	C	C,D	153436	283	3420508	33
1/2	USUU	C	C	10441784	125	4464095	27
1/2	USUU	C	F	184	0	0	0

Continued on next page

$\leq 3$  CP-chiral mirror pairs

$\leq 3$  CP-chiral Susy Higgs pairs

$\leq 6$  CP-chiral singlets (right-handed neutrinos)

# MOST FREQUENT MODELS

nr	Total occ.	MIPFs	Chan-Paton Group	spectrum	x	Solved
1	9801844	648	$U(3) \times Sp(2) \times Sp(6) \times U(1)$	VVVV	1/2	Y!
2	8479808(16227372)	675	$U(3) \times Sp(2) \times Sp(2) \times U(1)$	VVVV	1/2	Y!
3	5775296	821	$U(4) \times Sp(2) \times Sp(6)$	VVV	1/2	Y!
4	4810698	868	$U(4) \times Sp(2) \times Sp(2)$	VVV	1/2	Y!
5	4751603	554	$U(3) \times Sp(2) \times O(6) \times U(1)$	VVVV	1/2	Y!
6	4584392	751	$U(4) \times Sp(2) \times O(6)$	VVV	1/2	Y
7	4509752(9474494)	513	$U(3) \times Sp(2) \times O(2) \times U(1)$	VVVV	1/2	Y!
8	3744864	690	$U(4) \times Sp(2) \times O(2)$	VVV	1/2	Y!
9	3606292	467	$U(3) \times Sp(2) \times Sp(6) \times U(3)$	VVVV	1/2	Y
10	3093933	623	$U(6) \times Sp(2) \times Sp(6)$	VVV	1/2	Y
11	2717632	461	$U(3) \times Sp(2) \times Sp(2) \times U(3)$	VVVV	1/2	Y!
12	2384626	560	$U(6) \times Sp(2) \times O(6)$	VVV	1/2	Y
13	2253928	669	$U(6) \times Sp(2) \times Sp(2)$	VVV	1/2	Y!
14	1803909	519	$U(6) \times Sp(2) \times O(2)$	VVV	1/2	Y!
15	1676493	517	$U(8) \times Sp(2) \times Sp(6)$	VVV	1/2	Y
16	1674416	384	$U(3) \times Sp(2) \times O(6) \times U(3)$	VVVV	1/2	Y
17	1654086	340	$U(3) \times Sp(2) \times U(3) \times U(1)$	VVVV	1/2	Y
18	1654086	340	$U(3) \times Sp(2) \times U(3) \times U(1)$	VVVV	1/2	Y
19	1642669	360	$U(3) \times Sp(2) \times Sp(6) \times U(5)$	VVVV	1/2	Y
20	1486664	346	$U(3) \times Sp(2) \times O(2) \times U(3)$	VVVV	1/2	Y!
21	1323363	476	$U(8) \times Sp(2) \times O(6)$	VVV	1/2	Y
22	1135702	350	$U(3) \times Sp(2) \times Sp(2) \times U(5)$	VVVV	1/2	Y!
23	1050764	532	$U(8) \times Sp(2) \times Sp(2)$	VVV	1/2	Y
24	956980	421	$U(8) \times Sp(2) \times O(2)$	VVV	1/2	Y
25	950003	449	$U(10) \times Sp(2) \times Sp(6)$	VVV	1/2	Y
26	910132	51	$U(3) \times U(2) \times Sp(2) \times O(1)$	AAVV	0	Y
...						
34	869428(1096682)	246	$U(3) \times Sp(2) \times U(1) \times U(1)$	VVVV	1/2	Y!
153	115466	335	$U(4) \times U(2) \times U(2)$	VVV	1/2	Y
225	71328	167	$U(3) \times U(3) \times U(3)$	VVV	1/3	

# MOST FREQUENT MODELS

nr	Total occ.	MIPFs	Chan-Paton Group	spectrum	x	Solved
1	9801844	648	$U(3) \times Sp(2) \times Sp(6) \times U(1)$	VVVV	1/2	Y!
2	8479808(16227372)	675	$U(3) \times Sp(2) \times Sp(2) \times U(1)$	VVVV	1/2	Y!
3	5775296	821	$U(4) \times Sp(2) \times Sp(6)$	VVV	1/2	Y!
4	4810698	868	$U(4) \times Sp(2) \times Sp(2)$	VVV	1/2	Y!
5	4751603	554	$U(3) \times Sp(2) \times O(6) \times U(1)$	VVVV	1/2	Y!
6	4584392	751	$U(4) \times Sp(2) \times O(6)$	VVV	1/2	Y
7	4509752(9474494)	513	$U(3) \times Sp(2) \times O(2) \times U(1)$	VVVV	1/2	Y!
8	3744864	690	$U(4) \times Sp(2) \times O(2)$	VVV	1/2	Y!
9	3606292	467	$U(3) \times Sp(2) \times Sp(6) \times U(3)$	VVVV	1/2	Y
10	3093933	623	$U(6) \times Sp(2) \times Sp(6)$	VVV	1/2	Y
11	2717632	461	$U(3) \times Sp(2) \times Sp(2) \times U(3)$	VVVV	1/2	Y!
12	2384626	560	$U(6) \times Sp(2) \times O(6)$	VVV	1/2	Y
13	2253928	669	$U(6) \times Sp(2) \times Sp(2)$	VVV	1/2	Y!
14	1803909	519	$U(6) \times Sp(2) \times O(2)$	VVV	1/2	Y!
15	1676493	517	$U(8) \times Sp(2) \times Sp(6)$	VVV	1/2	Y
16	1674416	384	$U(3) \times Sp(2) \times O(6) \times U(3)$	VVVV	1/2	Y
17	1654086	340	$U(3) \times Sp(2) \times U(3) \times U(1)$	VVVV	1/2	Y
18	1654086	340	$U(3) \times Sp(2) \times U(3) \times U(1)$	VVVV	1/2	Y
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# PATI-SALAM

Type:	U	S	S
Dimension	4	2	2
5 x ( V , 0 , V )	chirality	-3	
3 x ( V , V , 0 )	chirality	3	
2 x ( Ad , 0 , 0 )	chirality	0	
2 x ( 0 , A , 0 )	chirality	0	
7 x ( 0 , 0 , A )	chirality	0	
4 x ( A , 0 , 0 )	chirality	0	
2 x ( 0 , S , 0 )	chirality	0	
5 x ( 0 , 0 , S )	chirality	0	
7 x ( 0 , V , V )	chirality	0	

# SU(5)

Type:	U	O	O	
Dimension	5	1	1	
3 x	(A , 0 , 0 )	chirality	3	
11 x	(V , V , 0 )	chirality	-3	
8 x	(S , 0 , 0 )	chirality	0	
3 x	(Ad, 0 , 0 )	chirality	0	
1 x	(0 , A , 0 )	chirality	0	
3 x	(0 , V , V )	chirality	0	
8 x	(V , 0 , V )	chirality	0	
2 x	(0 , S , 0 )	chirality	0	
4 x	(0 , 0 , S )	chirality	0	
4 x	(0 , 0 , A )	chirality	0	

*Note: gauge group is just SU(5)!*

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- ✿ Very clean SU(5)'s....
- ✿ ....But are they good for anything?



**IT'S JUST ONE SMALL STEP:  
874 HODGE NUMBERS SCANNED  
AT LEAST 30000 KNOWN (M. KREUZER)**