

The Emperor's Last Clothes?



Overlooking the String Theory Landscape



THE EMPEROR'S NEW CLOTHES



Hans Christian Andersen

Many years ago, there lived an emperor who cared much about his clothes. One day he heard from two swindlers named Guido and Luigi Farabutto that they could make the finest suit of clothes from the most beautiful cloth. This cloth, they said, also had the special capability that it was invisible to anyone who was either stupid or not fit for his position.

The emperor allowed himself to be dressed in the clothes for a procession through town, never admitting that he was too unfit and stupid to see what he was wearing.

Of course, all the townspeople wildly praised the magnificent clothes of the emperor, afraid to admit that they could not see them, until a small child said:

"But he has nothing on!"

Based on:

The Emperor's Last Clothes?
Overlooking the String Theory Landscape.

Rept. Prog. Phys. 71:072201,2008. (20 pages)

Extended version: [arXiv:0807.3249](https://arxiv.org/abs/0807.3249) (87 pages)

The Fairy Tale

Early String Theory Expectations: (\approx 1985)

“The hope is that the constraints imposed on such theories solely by the need for mathematical consistency are so strong that they essentially determine a single possible theory uniquely, and that by working out the consequences of the theory in detail one might eventually be able to show that there must be particles with precisely the masses, interactions, and so on, of the known elementary particles: in other words, that the world we live in is the only possible one.”

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From “The Problems of Physics” by Antony Legget (1987)

A.N. Schellekens,

Contribution to the proceedings of the EPS conference, Uppsala, June 1987

The prevailing attitude seems to be that "non-perturbative string effects" will somehow select a unique vacuum. This is unreasonable and unnecessary wishful thinking. We do not know at present how to discuss such effects, and have no idea whether they impose any restrictions at all. One cannot reasonably expect that a mathematical condition will have a unique solution corresponding to the standard model with three generations and a bizarre mass matrix. It is important to realize that this quest for uniqueness is based on philosophy, not on physics. There is no logical reason why the "theory of everything" should have a unique vacuum.

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A. Strominger (1986)

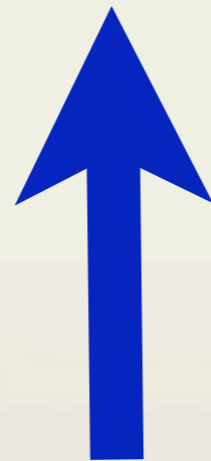
All of this points to the overwhelming need to find a dynamical principle for determining the ground state, which now appears more imperative than ever.

String Theory



Standard Model

String Theory



Standard Model

“Theory of almost everything”

~~“Theory of almost everything”~~
String Theory



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String Theory



Anthropic Principle



Standard Model
“Theory of almost everything”

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Anthropic Principle

David Gross (Strings 2008):
“We all know that it is wrong”



Standard Model

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Anthropic Principle

What we observe is biased by
our own existence.

BRIEF HISTORY

1973: Brandon Carter

Carter proposed the “Anthropic Principle” in Krakow, Poland in 1973, during a special two-week series of lectures commemorating Copernicus's 500th birthday. He proclaimed that humanity does indeed hold a special place in the Universe, an assertion that is the exact opposite of Copernicus's now universally accepted theory. His statement that day is now referred to as the Weak Anthropic Principle (WAP) and runs like this: “The observed values of all physical and cosmological quantities are not equally probable, but they take on the values restricted by the requirement that there exist sites where carbon-based life can evolve and by the requirement that the Universe be old enough for it to have already done so.” Later, Carter also proposed the Strong Anthropic Principle (SAP), which states that the Universe had to bring humanity into being. The SAP states that “the Universe must have those properties which allow life to develop within it at some stage in its history.”

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1987: Barrow and Tipler

“The Anthropic Cosmic Principle”

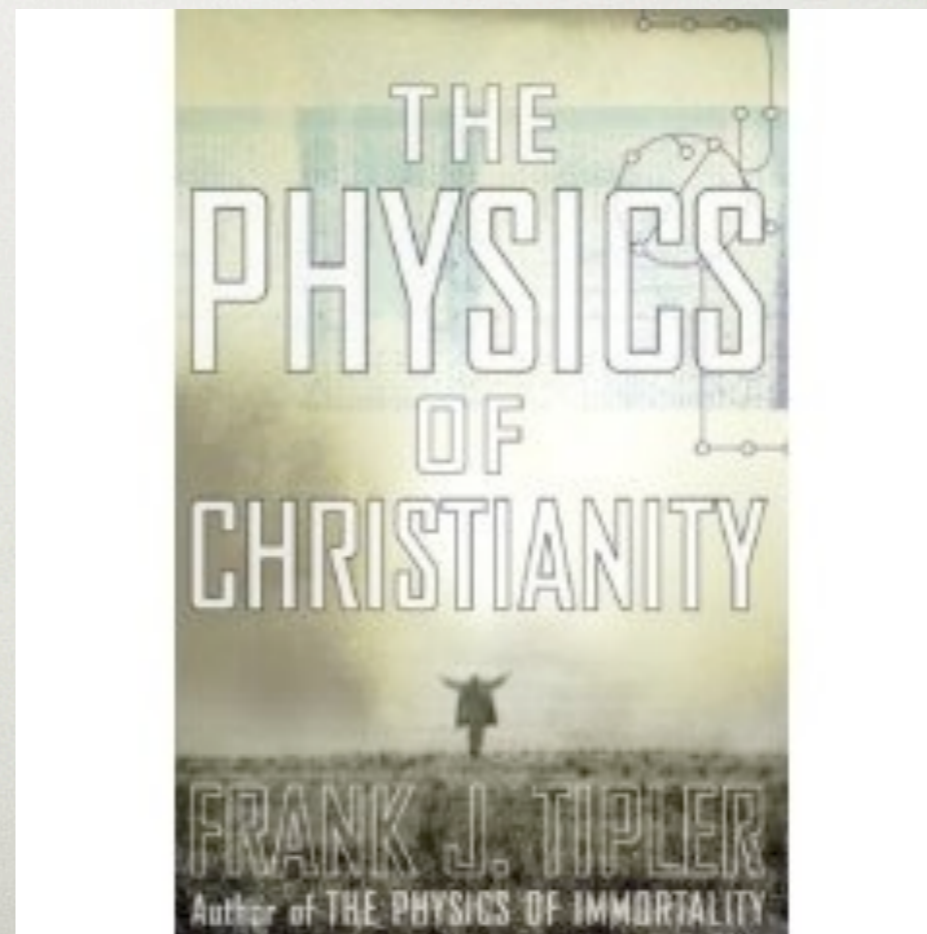
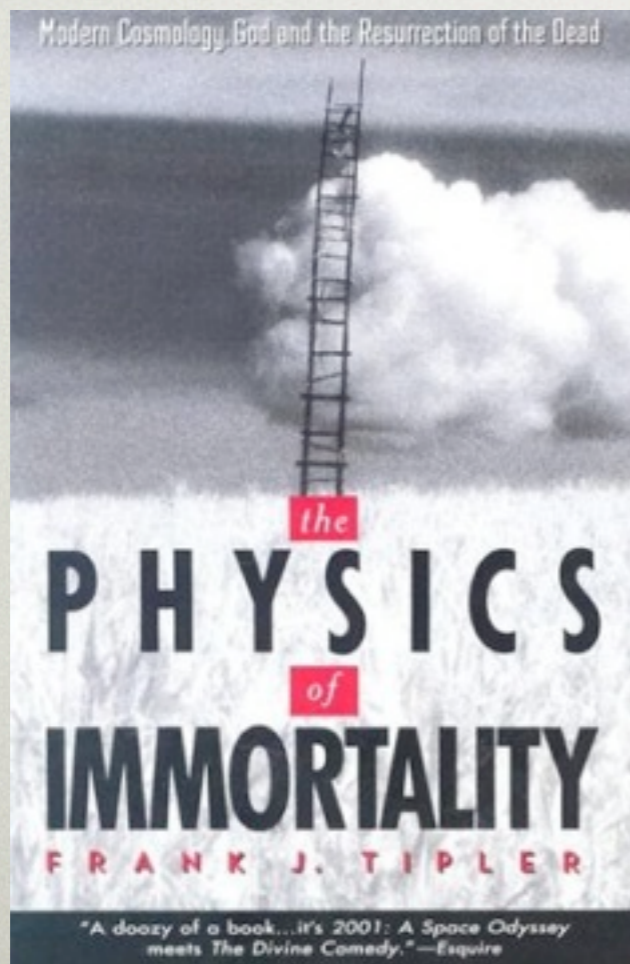
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Other work by F. Tipler



From a book review
by Larry Krauss:

“I was first tempted to describe Tipler’s new book as nonsense, but I soon realized that that would be unfair to the concept of nonsense.”

Criticisms

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- * It is assumed that some things could be different than what we observe. But what can vary, and what do you keep fixed when you vary it?

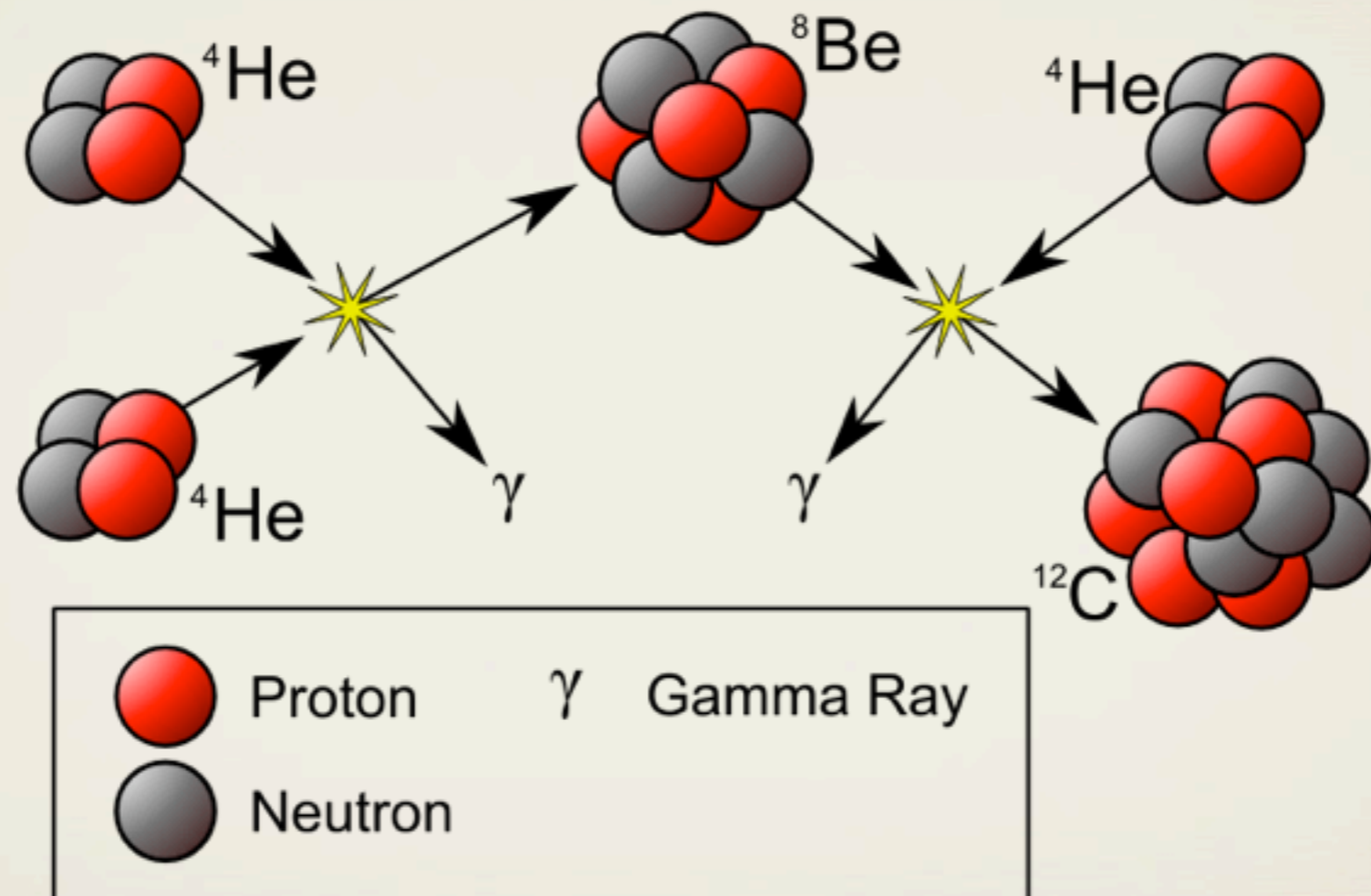
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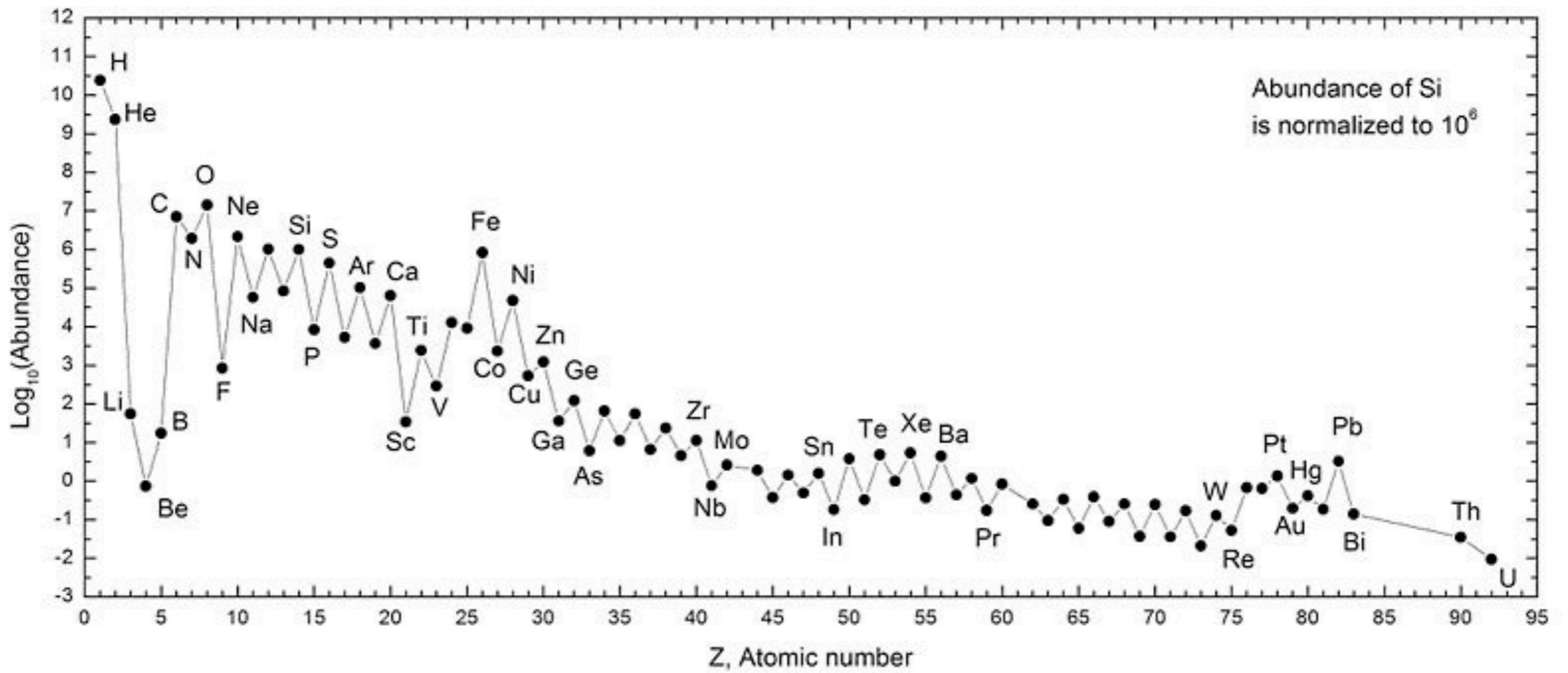
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- * So what?

Example: The Beryllium Bottleneck



Hoyle: there should exist a carbon-12 resonance near 7.65 MeV.

This prediction was confirmed!



- * One cannot vary a level of Carbon while keeping everything else fixed.
- * Carbon is essential for our kind of life. But the relevant question is: is it essential for any kind of intelligent life? (Some anthropic arguments rely on special properties of water or DNA.)
- * So what?
Hoyle: *“A common sense interpretation of the facts suggests that a superintellect has monkeyed with physics, as well as with chemistry and biology”*

The Standard Model

Theory of quarks and leptons and their electromagnetic, strong and weak interactions.

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Discrete choices:

Lie-algebra: $SU(3) \times SU(2) \times U(1)$

Quark and lepton Representation:

$$3 \times \left\{ (3, 2, \frac{1}{6}) + (\bar{3}, 1, -\frac{2}{3}) + (\bar{3}, 1, \frac{1}{3}) + (1, 2, -\frac{1}{2}) + (1, 1, 1) + (1, 1, 0) \right\}$$

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Continuous choices: 28 real parameters
(coupling constants, quark and lepton masses, mixing angles)

Feynman about α

There is a most profound and beautiful question associated with the observed coupling constant, e the amplitude for a real electron to emit or absorb a real photon. It is a simple number that has been experimentally determined to be close to $1/137.03597$. It has been a mystery ever since it was discovered more than fifty years ago, and all good theoretical physicists put this number up on their wall and worry about it.

....

*We know what kind of a dance to do experimentally to measure this number very accurately, but **we don't know what kind of dance to do on the computer to make this number come out**, without putting it in secretly!*

FORMULAS FOR α

$$\alpha = 2^{-4}3^{-3}\pi$$

Heisenberg

$$\alpha = \frac{9}{8\pi^4} \left(\frac{\pi^5}{2^{45}} \right)^{1/4}$$

Wyler

$$\alpha = \frac{29}{\pi} \cos\left(\frac{\pi}{137}\right) \tan\left(\frac{\pi}{(137 \times 29)}\right)$$

Gilson

Most variations in Nuclear Physics are invalid.

By now we know what really can be varied:

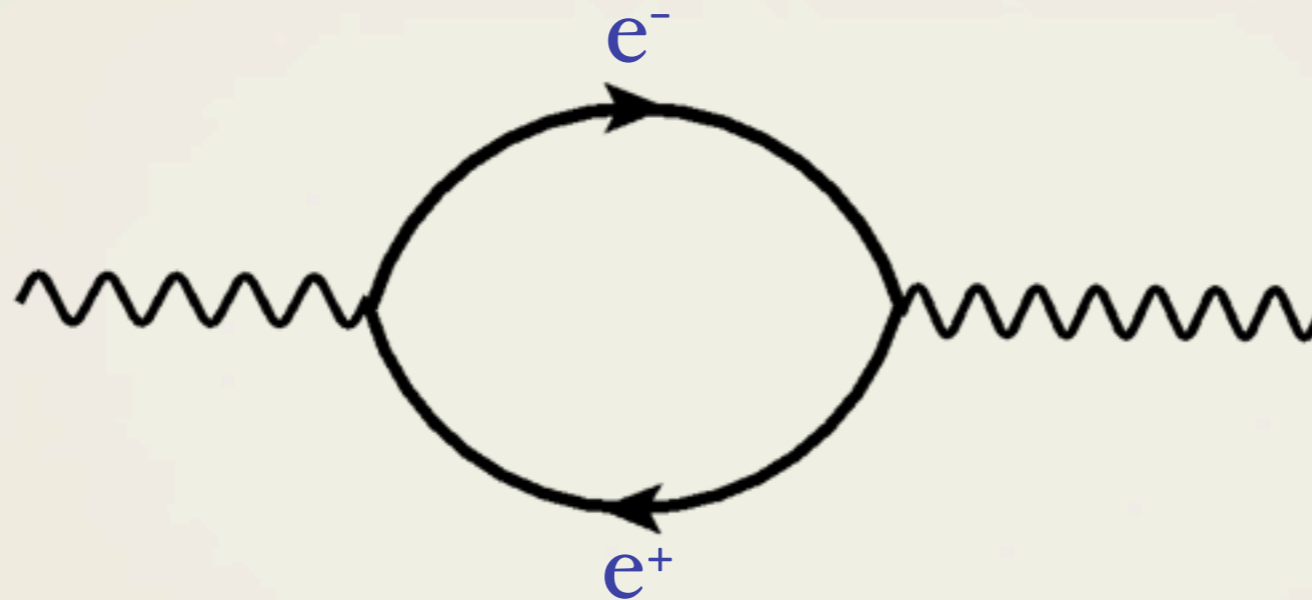
The QCD coupling constant and the quark masses.

You can't draw anthropic conclusions if you move "out of physics".

But how can a theory ever be immune to what we do not know yet?

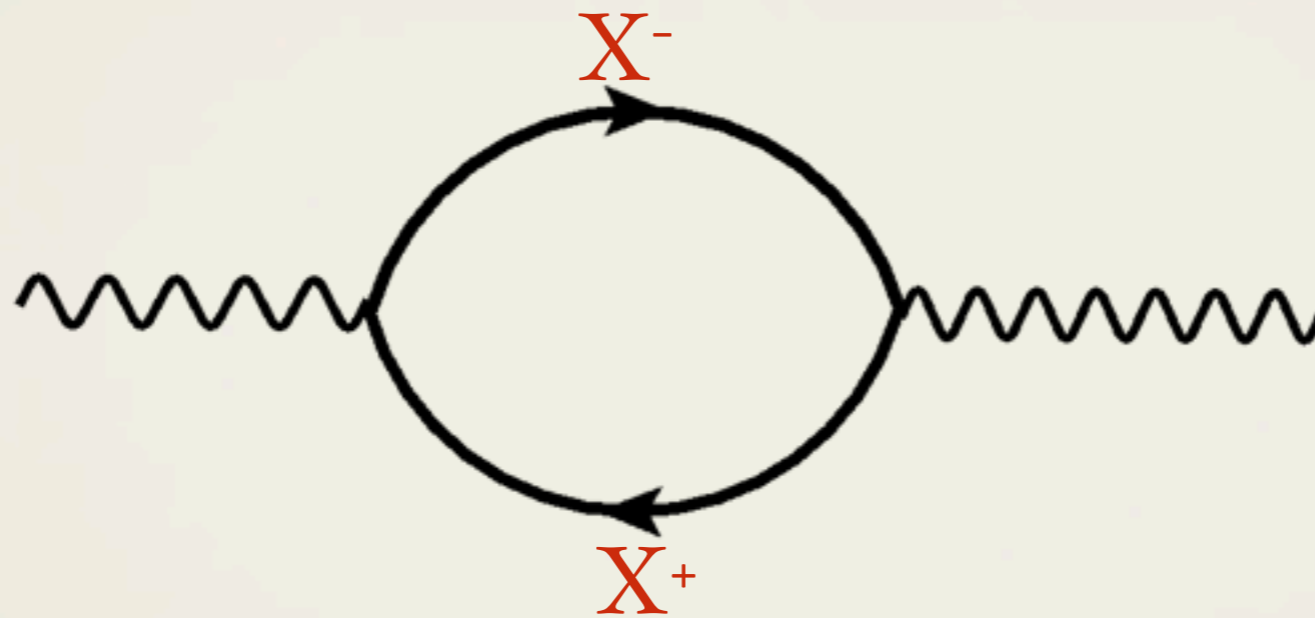
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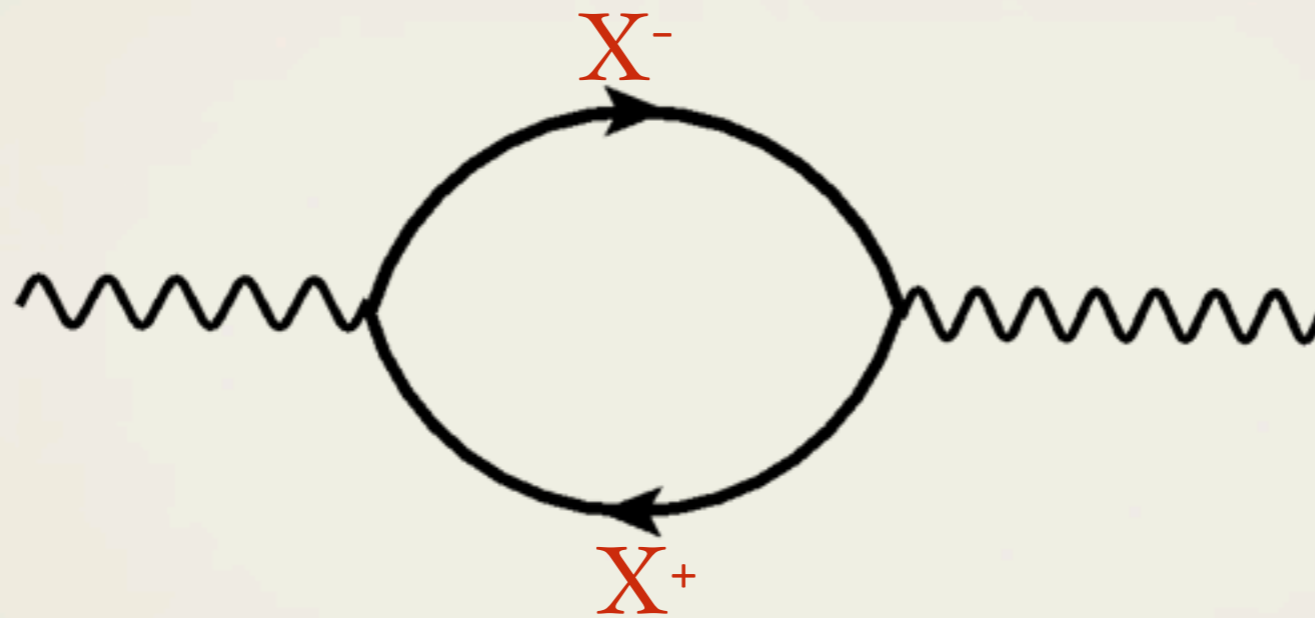
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Physics at shorter distances (space-time structure, new particles) gives rise to an infinity of unknowns....

But:

In the Standard Model all these unknowns can be “packaged” together in a finite number of parameters (plus corrections of order E/M_{New}).

This makes the theory intrinsically insensitive to M_{New}

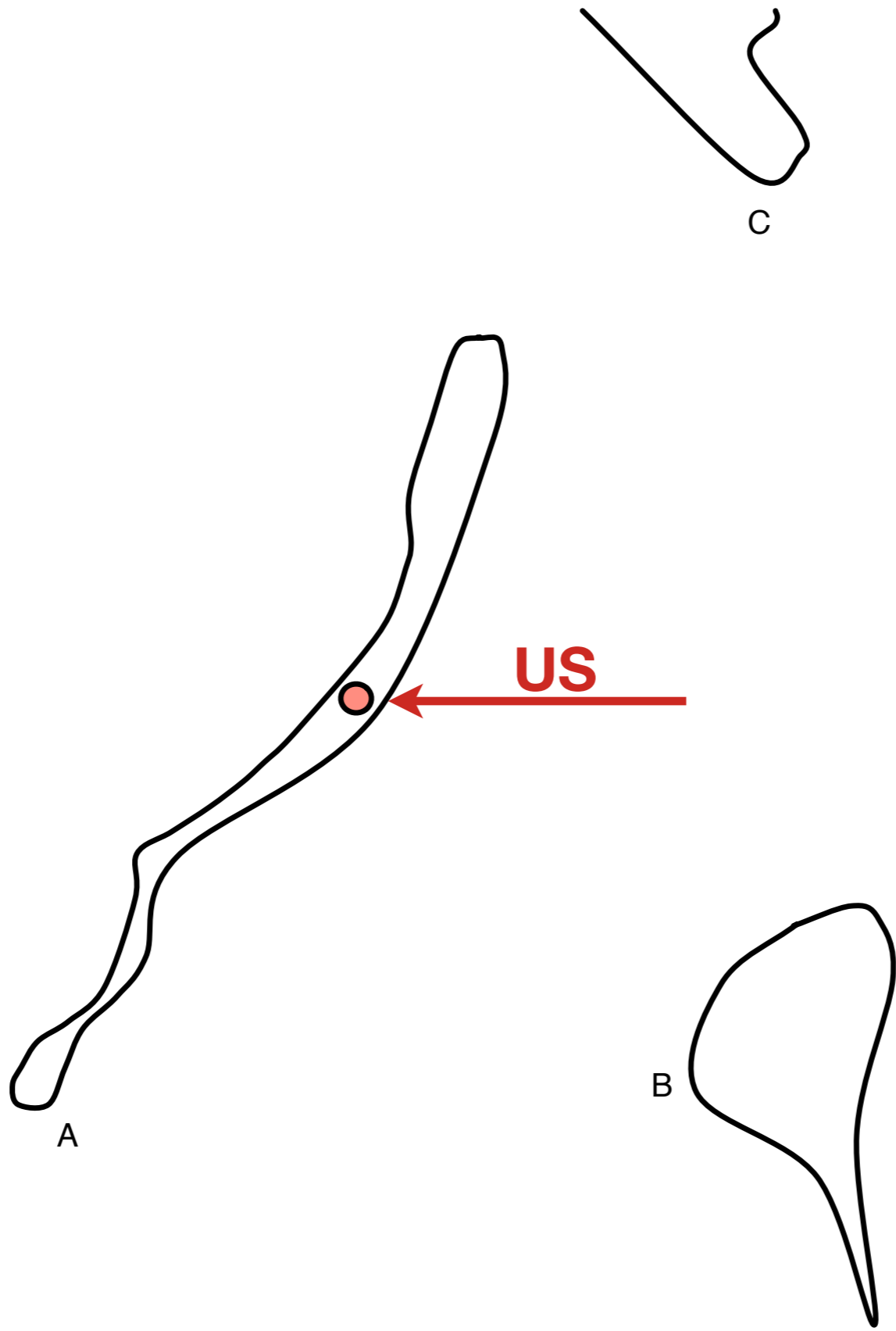
Experimentally M_{New} is at least about 1 TeV, well beyond the scale of Nuclear Physics.

Theoretically, the Standard Model can be extrapolated much further than that, perhaps until $M_{\text{Planck}}=10^{19}$ GeV.

Furthermore this is equally true for the relatives of the Standard Model: other gauge theories, with other groups, representations and parameters.

This allows us to do the following:

A “GEDANKEN” COMPUTATION



Anthropic Features of the Standard Model

- * Structure:
hard to analyse in general, but:
 - Odd SU(N) “color” group seems essential.
 - U(1) with massless photon seems essential.
- * Scales:
 - Strong scale (Λ_{QCD}) determines proton mass.
 - Weak scale determines quark, lepton masses
 - Both must be much smaller than M_{plank} (10^{19} GeV) and not too different from each other.
- * Parameters: $m_u, m_d, m_e, \alpha, \alpha_{\text{QCD}}$ are clearly important.
Less obvious: m_t, m_ν

Quark and lepton masses (GeV)

t,c,u (charge 2/3)	b,s,d (charge -1/3)	e, μ , τ (charge -1)
173	4.2	1.777
1.25	0.095	0.106
0.002	0.005	0.0005

Higgs mechanism: $\text{Mass} = \lambda \times (246 \text{ GeV})$

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t,c,u (charge 2/3)	b,s,d (charge -1/3)	e,μ,τ (charge -1)
173	4.2	1.777
↓ 138	↓ 44	↓ 16
1.25	0.095	0.106
↓ 625	↓ 19	↓ 206
0.002	0.005	0.0005

Higgs mechanism: $\text{Mass} = \lambda \times (246 \text{ GeV})$

Some constraints

- * Larger pion mass reduces the range of the strong force, destabilizing nuclei.

$$m_{\pi} \propto \sqrt{\Lambda_{\text{QCD}}(m_u + m_d)}$$

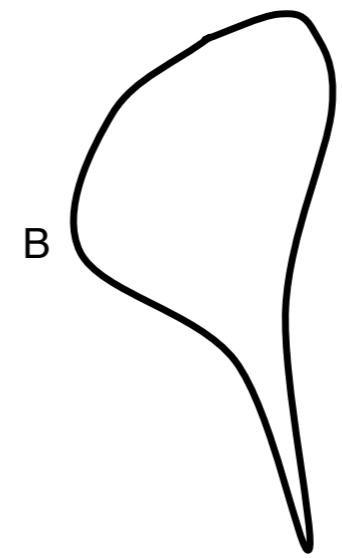
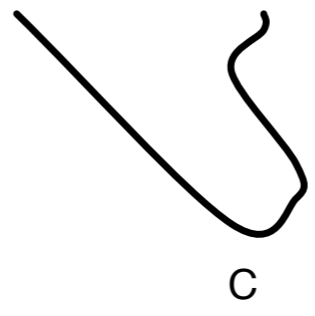
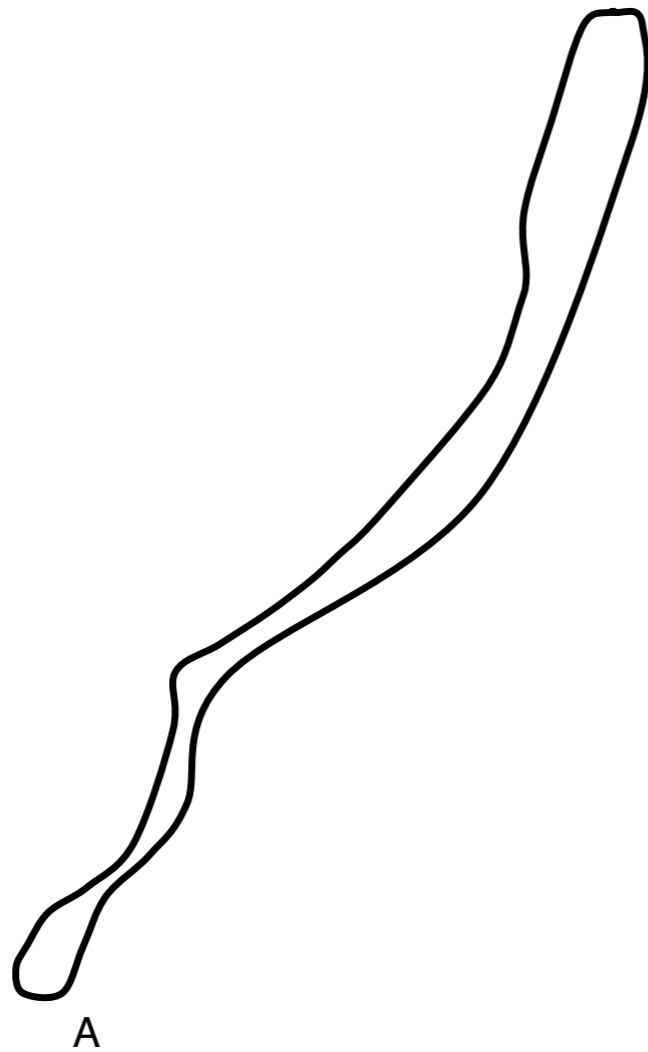
- * The proton (uud) should be stable against decay to a neutron (ddu)

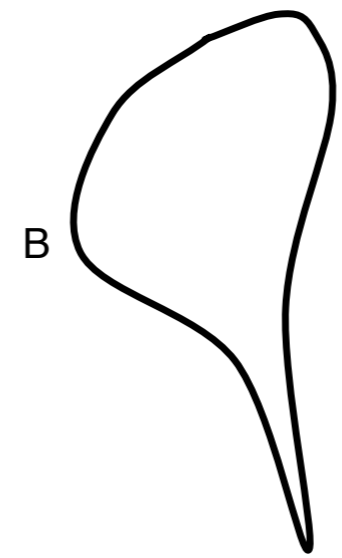
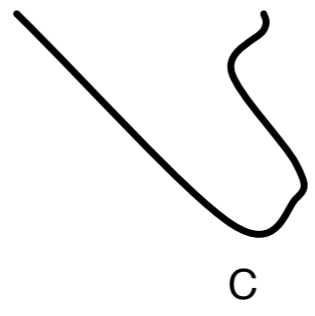
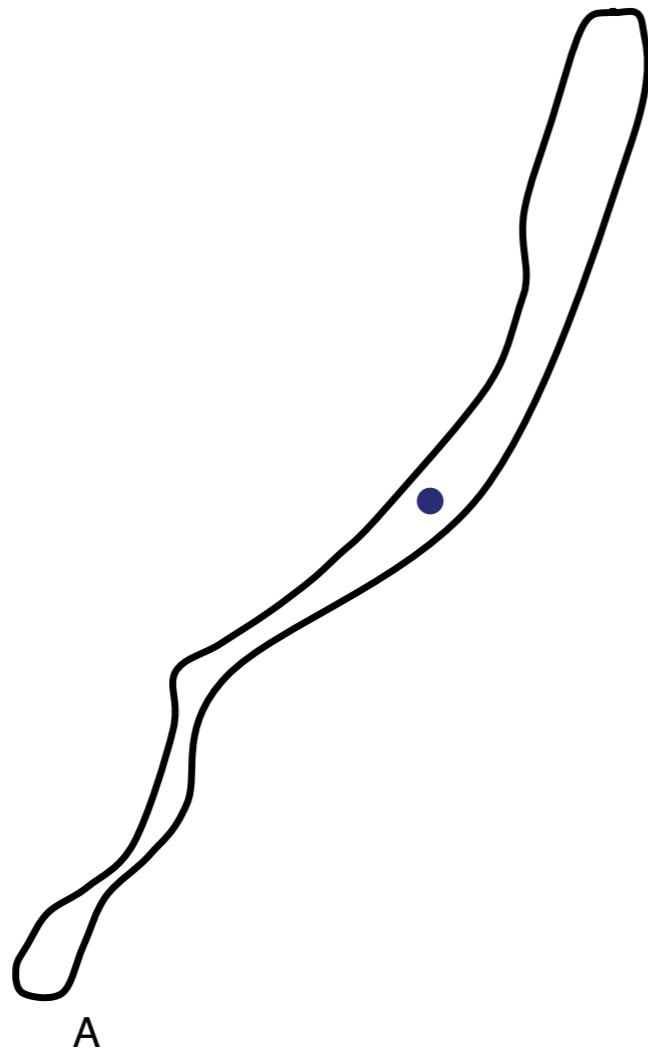


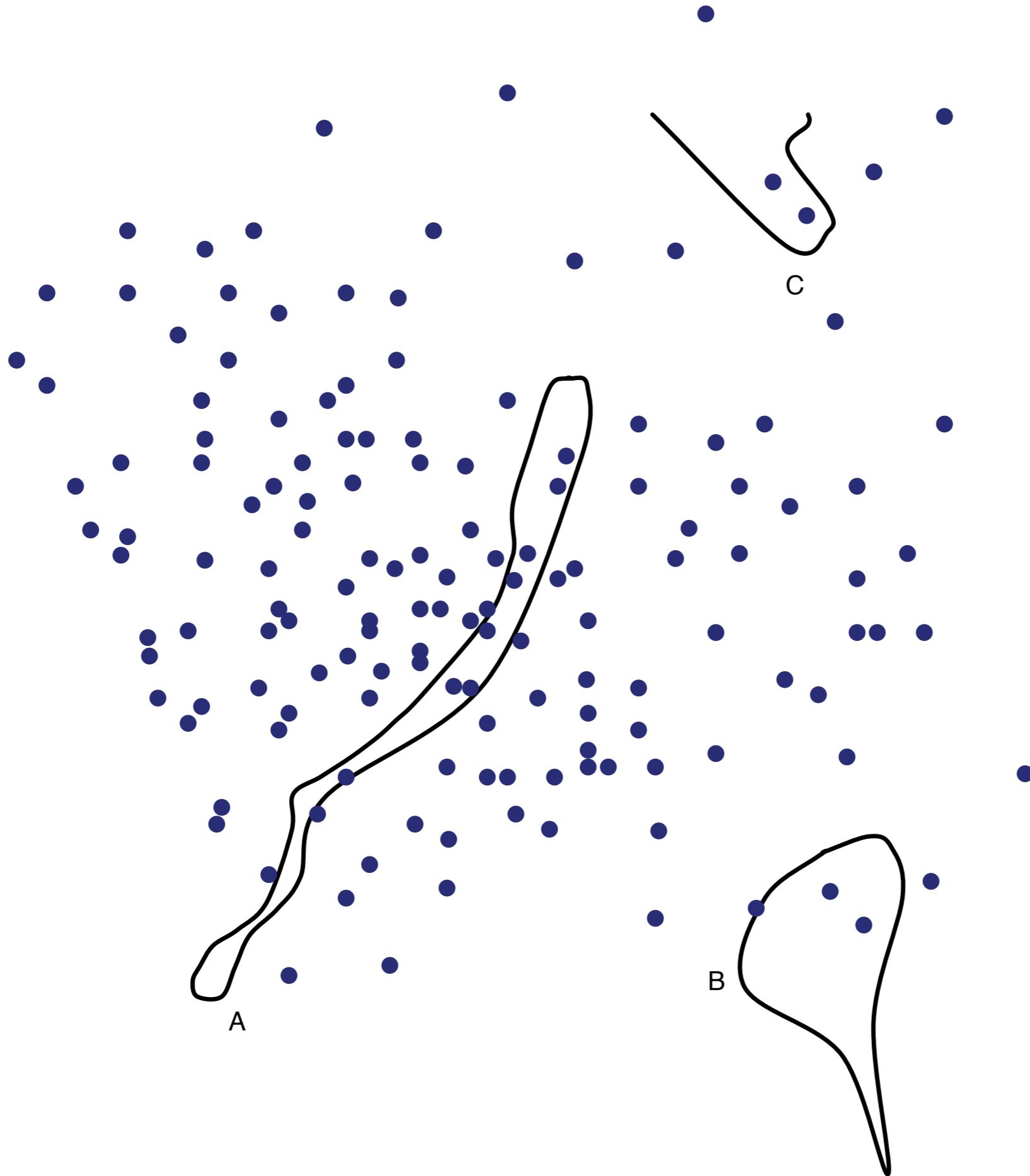
Electromagnetic forces lower the neutron mass with respect to the proton mass. This is solved by the fact that the up-quark is extremely light.

- * The neutron should be unstable, to prevent a neutron dominated universe. This limits the electron mass to $m_n - m_p = 1.29 \text{ MeV}$

A SECOND
“GEDANKEN”
COMPUTATION







How many?

From the knowledge of one point, one cannot decide that.

Assuming a distribution one could compute a required minimum number.

But let us have a look at the other side of the argument...

H. Georgi,

Fourth workshop on Grand Unification, Philadelphia, 1983

The physics of grand unification can provide a partial answer to some of the questions left unanswered at lower scales by correlating the properties of quarks and leptons. But the fundamental problem still remains: What makes the gauge structure and fermion content of the world special and unique?

This puzzle, which I will call the "uniqueness" puzzle, simply cannot be answered in the context of conventional quantum field theory (QFT). Conventional QFT does not single out any particular gauge structure. Thus we might expect the uniqueness question to be answered at some large scale M_B where conventional quantum field theory breaks down.

Arguments in favor of uniqueness

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Uniqueness?

- * The Standard model is just one point in a huge discrete and continuous set.
- * We can observe only one point in this set anyway.
- * There is no argument why the “fundamental equations” should have a unique “solution”.
- * The one we observe does not look mathematically unique.
- * The one we observe seems tuned to allow us to exist: uniqueness would be a disaster!

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You may hope there will be “very few”.
But what does that mean?

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From an ESF proposal in 2009

“...Great progress in this direction has been achieved by introducing compactifications with fluxes. The outcome is still far from being unique and reveals a landscape of possibilities.”

SO WHAT?

Giving up?

To some people this sounds like:

“The laws of physics are the way they are, because otherwise we would not exist. Therefore physics stops here.”

If parameters like the light quark and lepton masses have a distribution of possible values, this is likely to be true for all standard model parameters.

But this does NOT imply that the Standard Model is nothing more than a bunch of random numbers. There is structure requiring an explanation, but we cannot expect to derive the entire set of choices.

All this does is define reasonable expectations for a “fundamental theory”. I am not giving up on that.

In fact, I am aiming for something much better than uniqueness: a theory that contributes to the explanation of our existence, rather than converting that into an eternal mysterious coincidence.

The Ideal Theory

Example: 10^{30} discrete points

The Standard Model provides about 80 digits of data.

This leaves about 50 digits worth of *postdictions*
(plus an infinity of *predictions*).

The fine structure constant would be computable exactly, but only after providing the first 30 digits.

This is more than enough to accept the correctness of such a theory, together with the existence of the $10^{30}-1$ other “solutions”.

It would be obvious that what we observe is biased by our existence (unless all 10^{30} points allow observers).

This anthropic principle would be equally unquestionable as the one for planets.

The difference is that for planetary properties we already have good theories and models, and we can observe alternatives. In such a situation an anthropic principle is only of secondary importance.

Requirements for an Ideal Theory

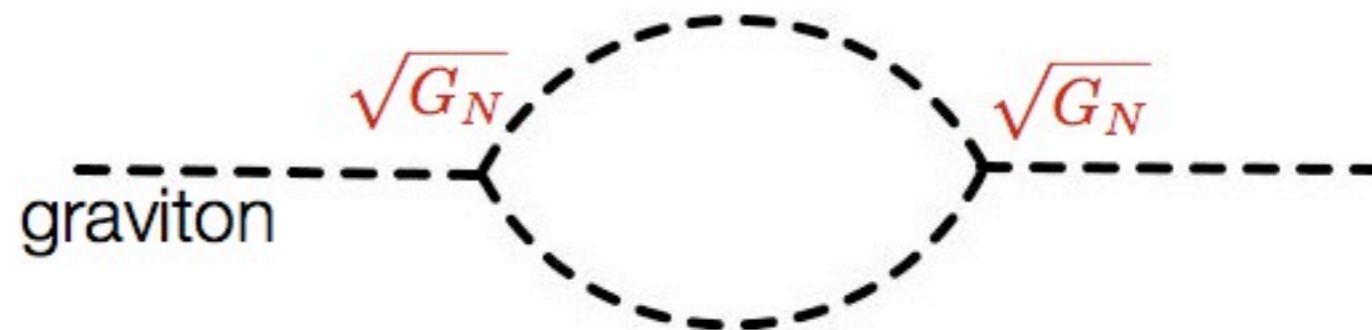
Requirements for an Ideal Theory

- * All parameters should be fixed to some discrete set.
 - We must control all virtual processes (“infinities” of QFT)
 - Including those of quantum gravity.
 - Including all particles we have not observed yet, and all interactions

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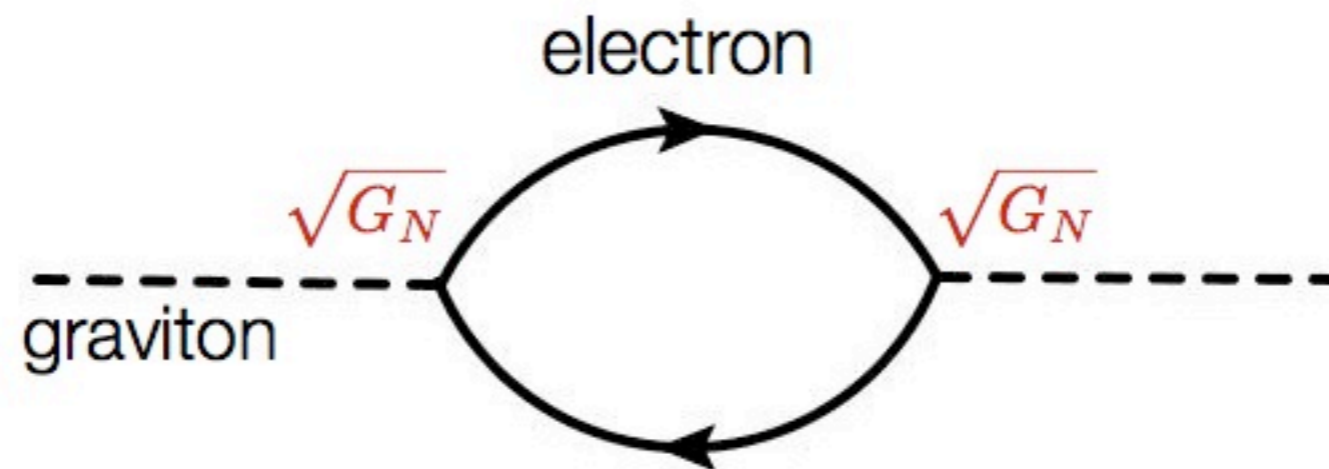
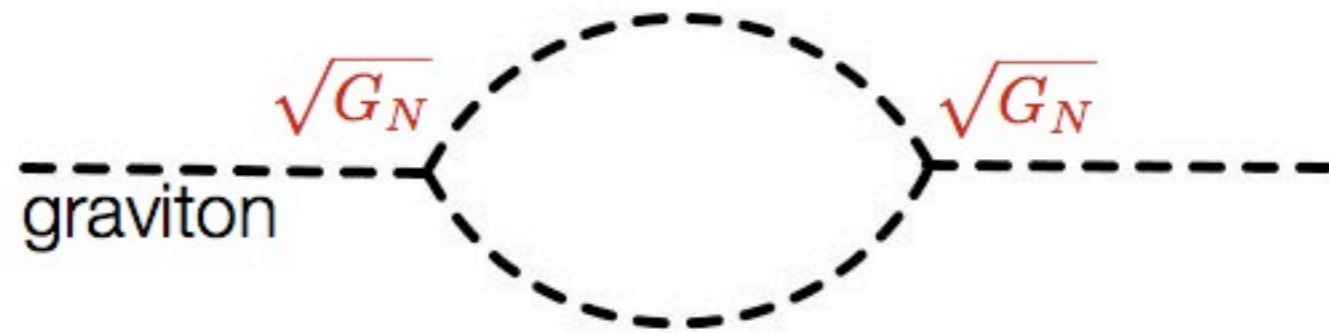
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- * There must be a way to end up with a large set of choices of groups and representations.
- * For each such discrete choice, there must be set of allowed parameter values.
- * Distinct solutions must be connected: we must be able to get to the standard model.

Dynamical Parameters

If we ignore the problems of quantum gravity, perhaps 28 continuous parameters is all we need. This will certainly contain the Standard Model.

However, in QFT there is no relation between QED with $\alpha=1/137.039$ or $\alpha=1/140$.

Possible solution: make all parameters dynamical (functions of space-time satisfying equations of motion).

This forces us to think about vacuum energy: changes in parameters will create changes in the energy of the vacuum.

This is irrelevant in QFT, but also uncalculable (sum over the ground state energy of an infinite number of oscillators). We may regulate it and subtract it for a given value of α , but this is not likely to be correct for a different value of α .

In the presence of gravity, it is no longer irrelevant. However, in the theory we are aiming at, it should be calculable.

Unfortunately, the answer is not likely to be correct.

The Cosmological Constant

Vacuum energy contributes to the infamous cosmological constant Λ

Gravity couples to it:

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R + \Lambda g_{\mu\nu} = 8\pi G_N T_{\mu\nu}$$

Its effect is to make the universe expand ($\Lambda > 0$) or collapse ($\Lambda < 0$)

Expected contribution from quantum gravity: $\approx (M_{\text{planck}})^4$

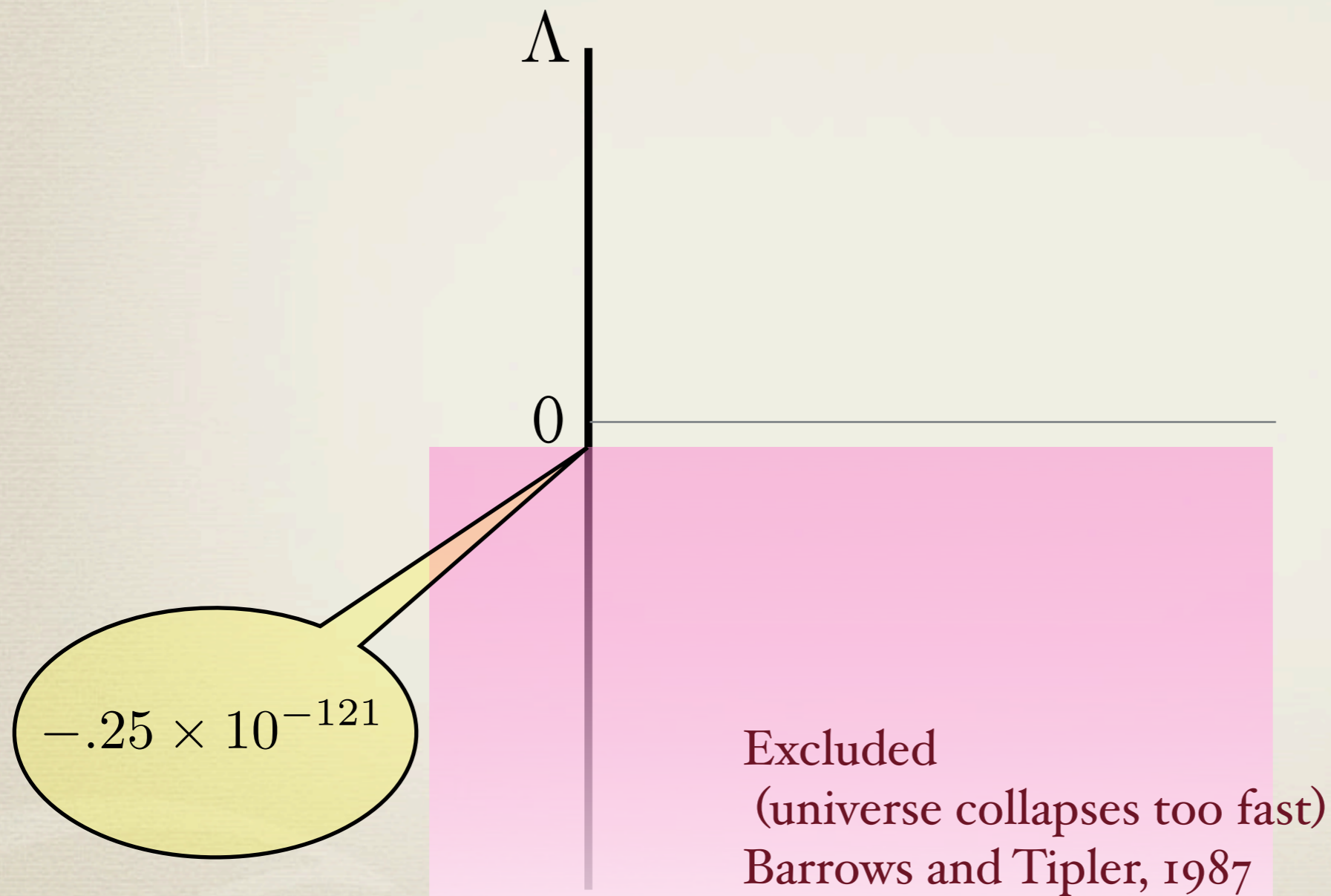
Expected contribution from known physics: $\approx 10^{-56}(M_{\text{planck}})^4$

Observed: $\approx .37 \times 10^{-121}(M_{\text{planck}})^4$

Anthropic Bounds



Anthropic Bounds



Anthropic Bounds

Excluded
(universe expands too rapidly
for galaxies to form)
Weinberg, 1987

Λ

$\approx 10^{-118}$

0

$-.25 \times 10^{-121}$

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Barrows and Tipler, 1987

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C.C. versus S.M.

An anthropic explanation requires more than 10^{120} points, assuming a flat distribution.

But:

Λ is less obviously a true variable of the laws of physics than the 28 standard model parameters.

The latter are clearly decoupled from what we do not know yet: gravity.

But Λ only makes sense in the presence of gravity.

So if in the true theory of gravity of our universe $\Lambda \equiv 0$ (or if gravity does not couple to vacuum energy), we are “out of physics” if we consider $\Lambda \neq 0$.

Of course, in that case we still have to find a way to explain the current observations.

STRING THEORY

Disclaimer

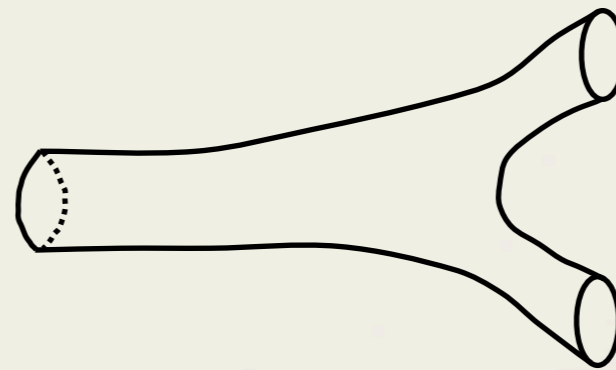
String theory is “work in progress”.

It slowly being discovered using an amazing web of perturbative and non-perturbative methods.

Some of the perturbative methods involve splitting and joining of strings, hence the name.



H_0



ϵH_1

What follows is the picture that seems to be emerging.
There are plenty of things we do not know yet!

What is string theory?

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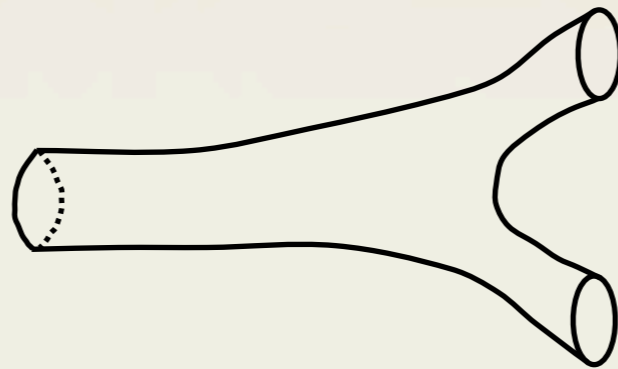
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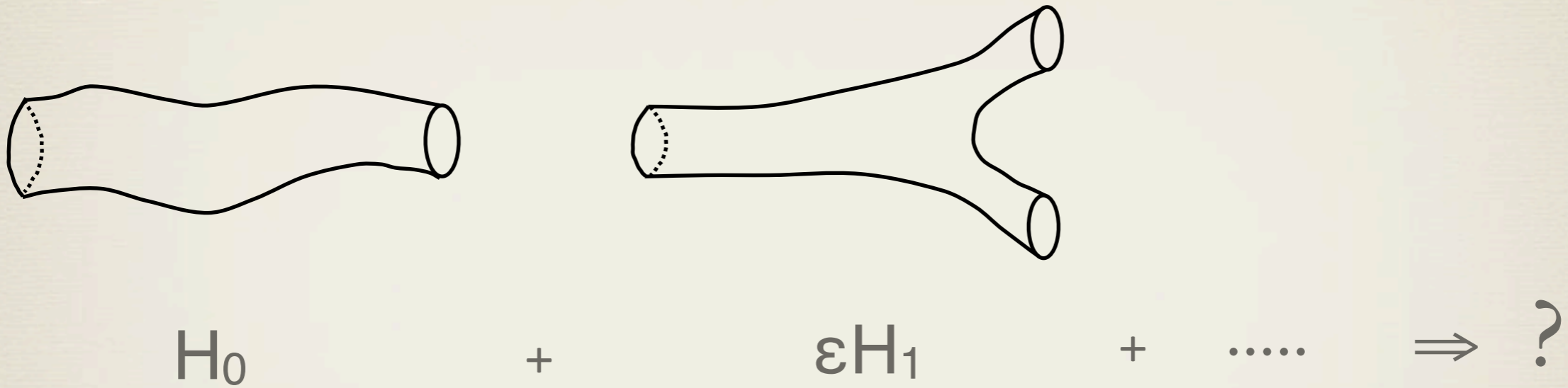
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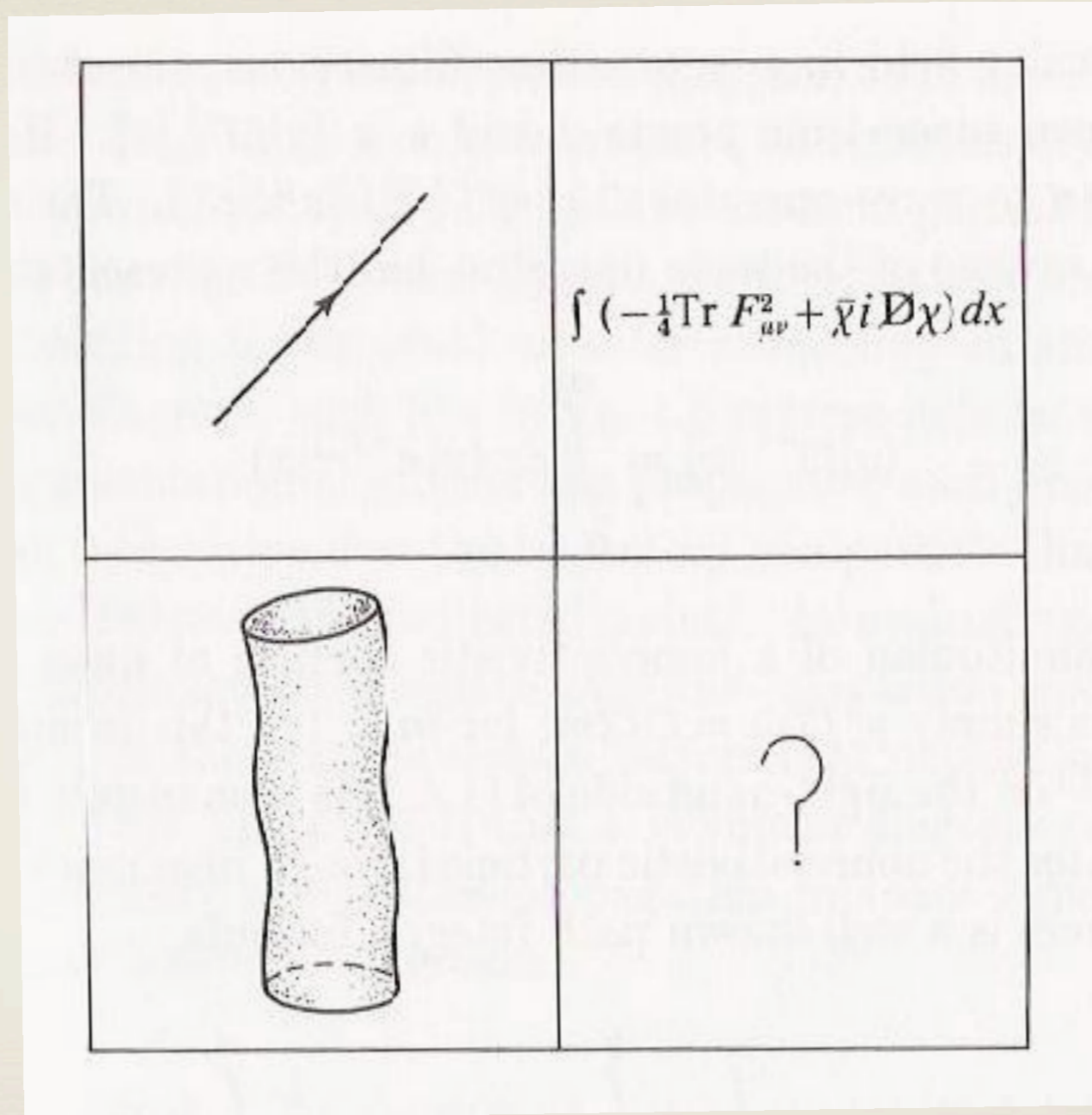
ϵH_1

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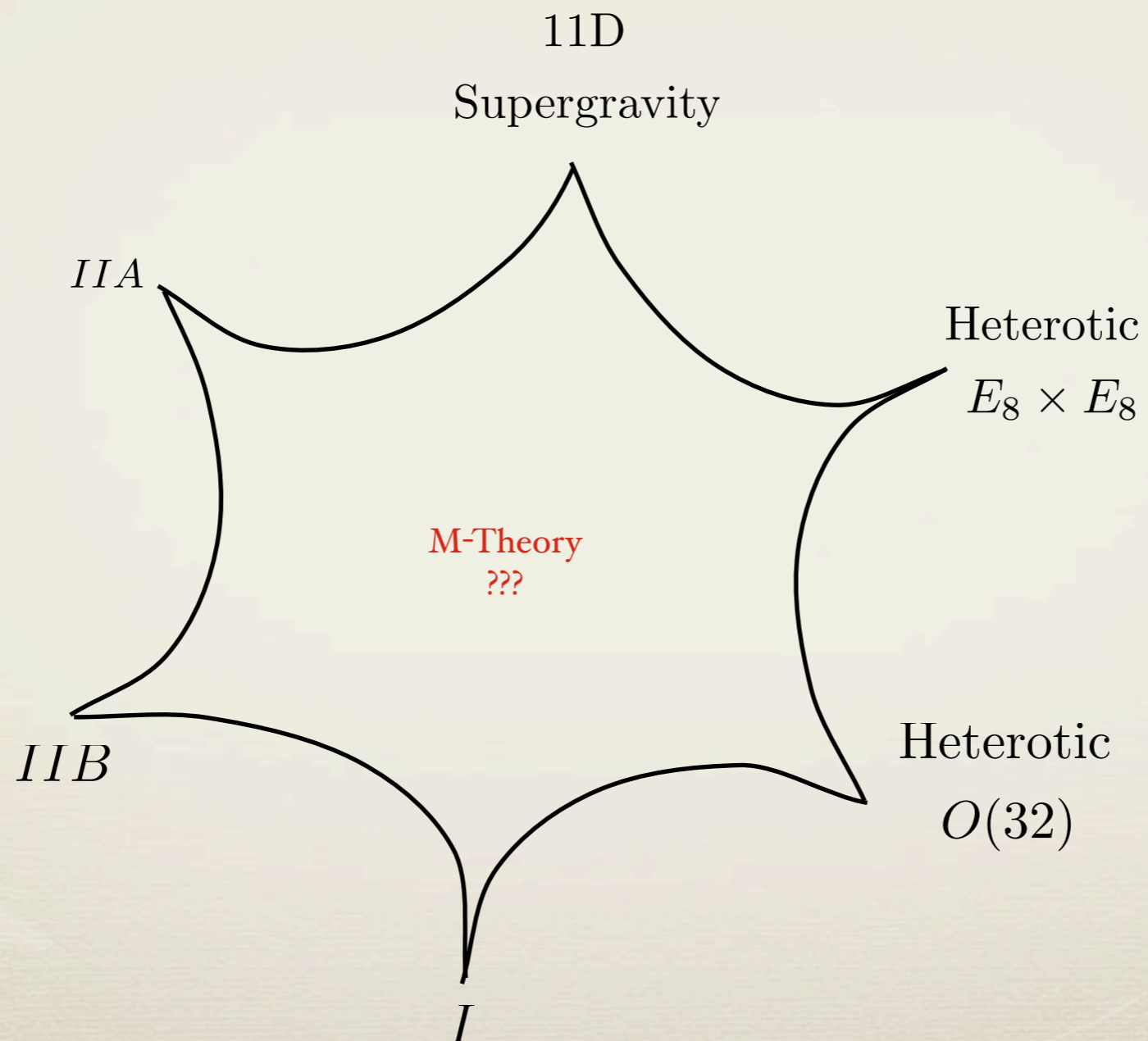


Green, Schwarz and Witten (1987)

What is string theory?

Several perturbative expansions in search of a theory.

(one of them does not even correspond to strings, and in all cases higher dimensional membranes are involved in addition to strings)



Fundamental Theory Requirements

I: Discrete choices

String theory lives naturally in 10 (or 11) dimensions.

But there is a choice of space-time backgrounds.

This choice includes 4D Minkowski times a compact manifold.

There is a huge choice of compact backgrounds.

This apparent “embarrassment of choices” is precisely what is needed to get the required richness of choices for the 4D gauge theory.

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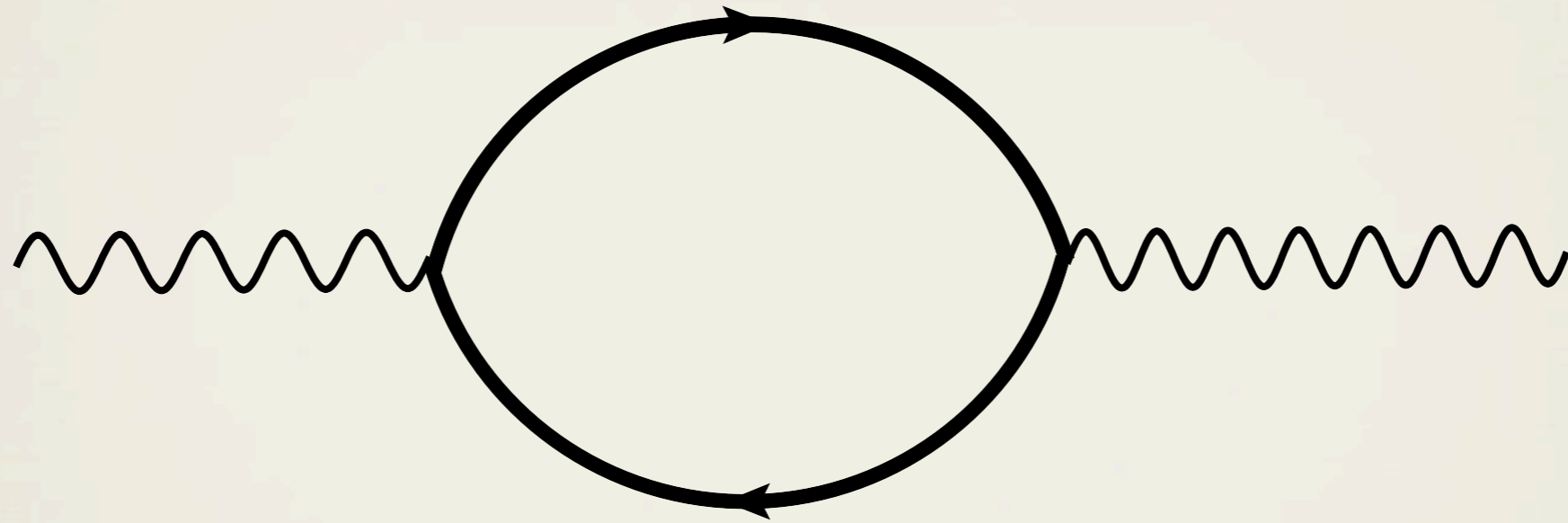
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For the discrete choices the anthropic principle is already established in String theory

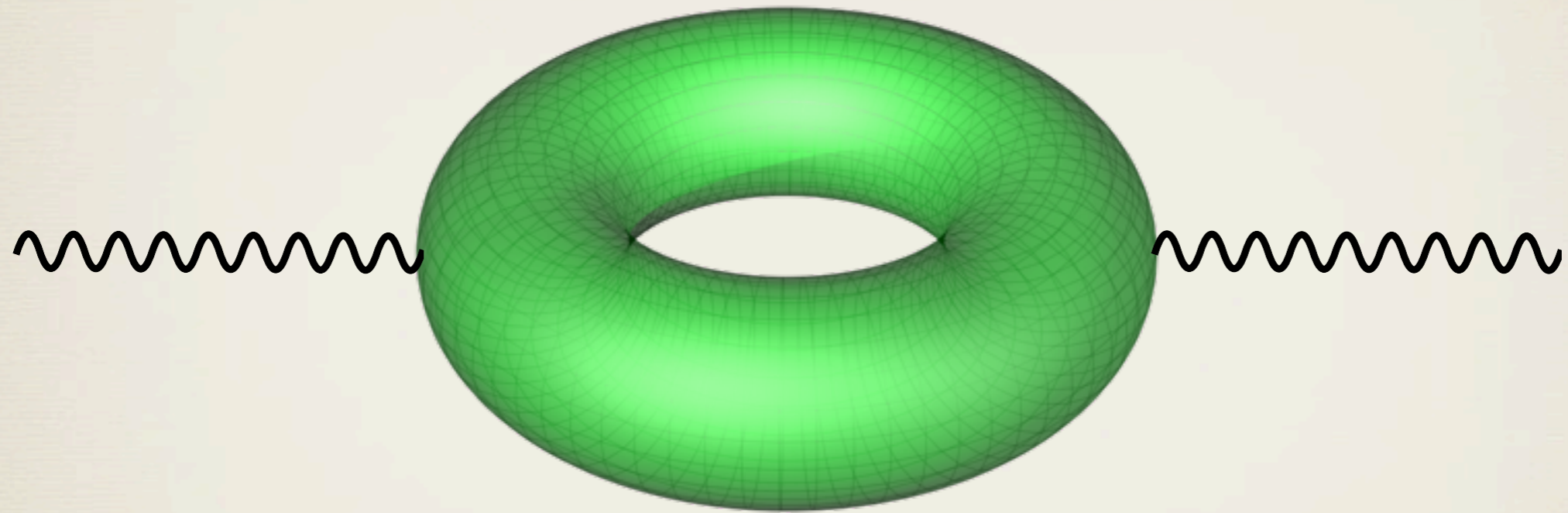
Fundamental Theory Requirements

II: Finiteness and Completeness



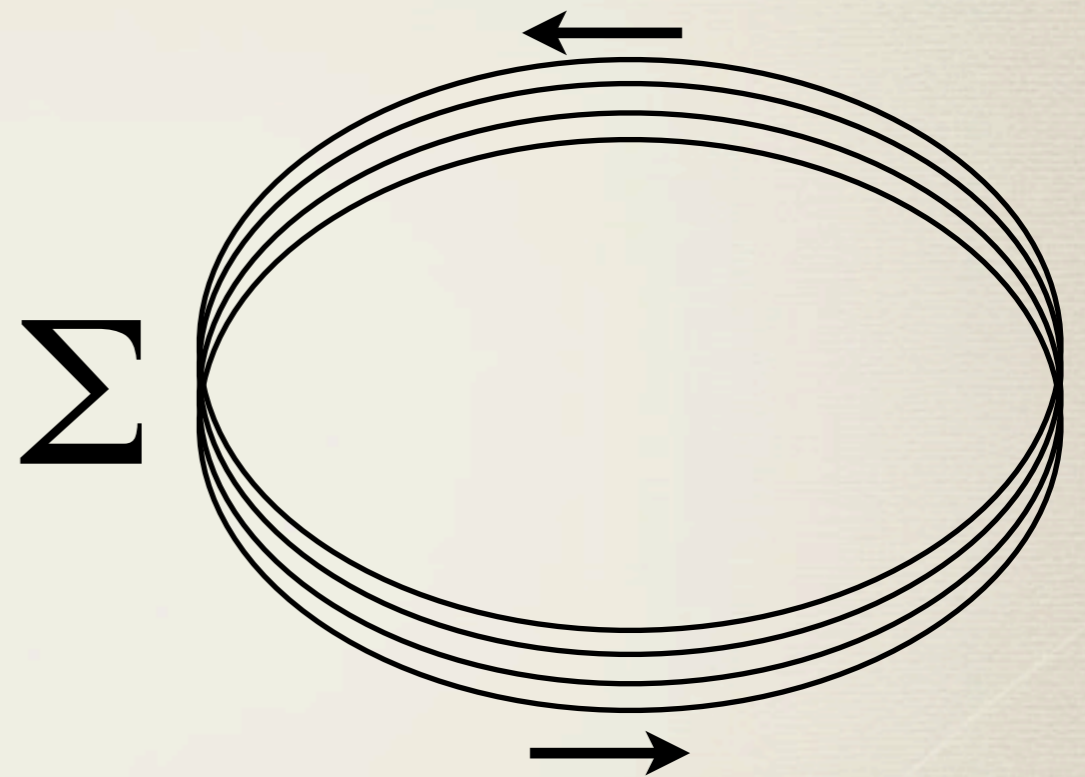
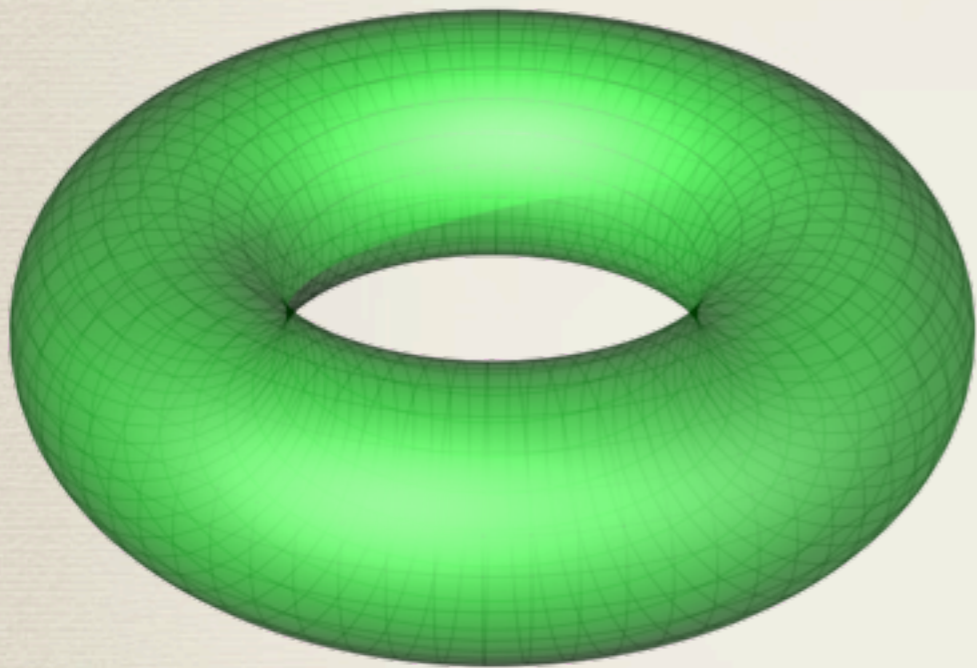
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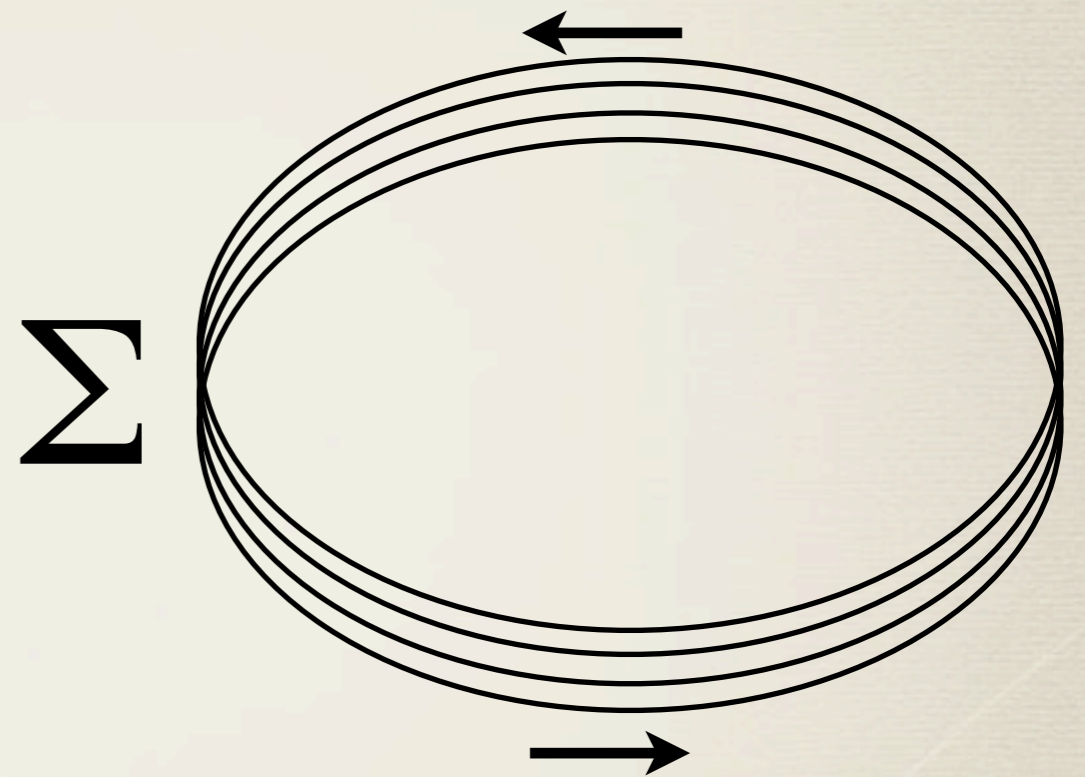
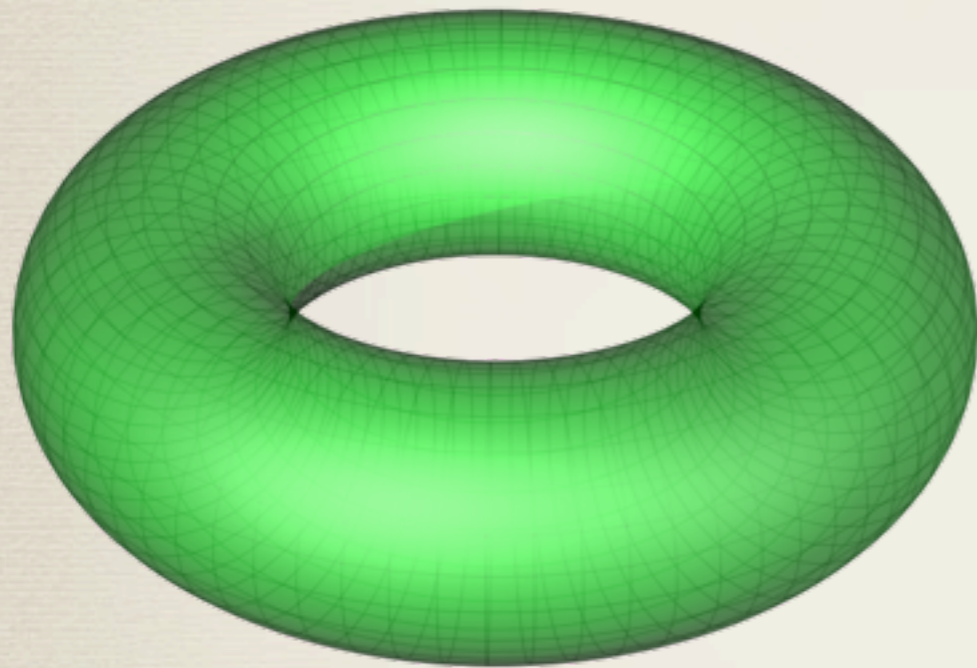
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Σ

Fundamental Theory Requirements

II: Finiteness and Completeness



$$\int \frac{d^2\tau}{(\text{Im}\tau)^{D/2+1}} \text{Tr} e^{-\text{Im}\tau H}$$

$\text{Im}\tau$

$\text{Re}\tau$

$-\frac{1}{2}$

$\frac{1}{2}$

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$$\int \frac{d^2\tau}{(\text{Im}\tau)^{D/2+1}} \text{Tr} e^{-\text{Im}\tau H}$$

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$-1/2$

$1/2$

Modular Invariance

Must be invariant under $SL_2(\mathbf{Z})/\mathbf{Z}_2$

$$\tau \rightarrow \frac{a\tau + b}{c\tau + d}, \quad a, b, c, d \in \mathbf{Z}; \quad ad - bc = 1$$

Generated by

$$\tau \rightarrow \tau + 1$$

$$\tau \rightarrow -\frac{1}{\tau}$$

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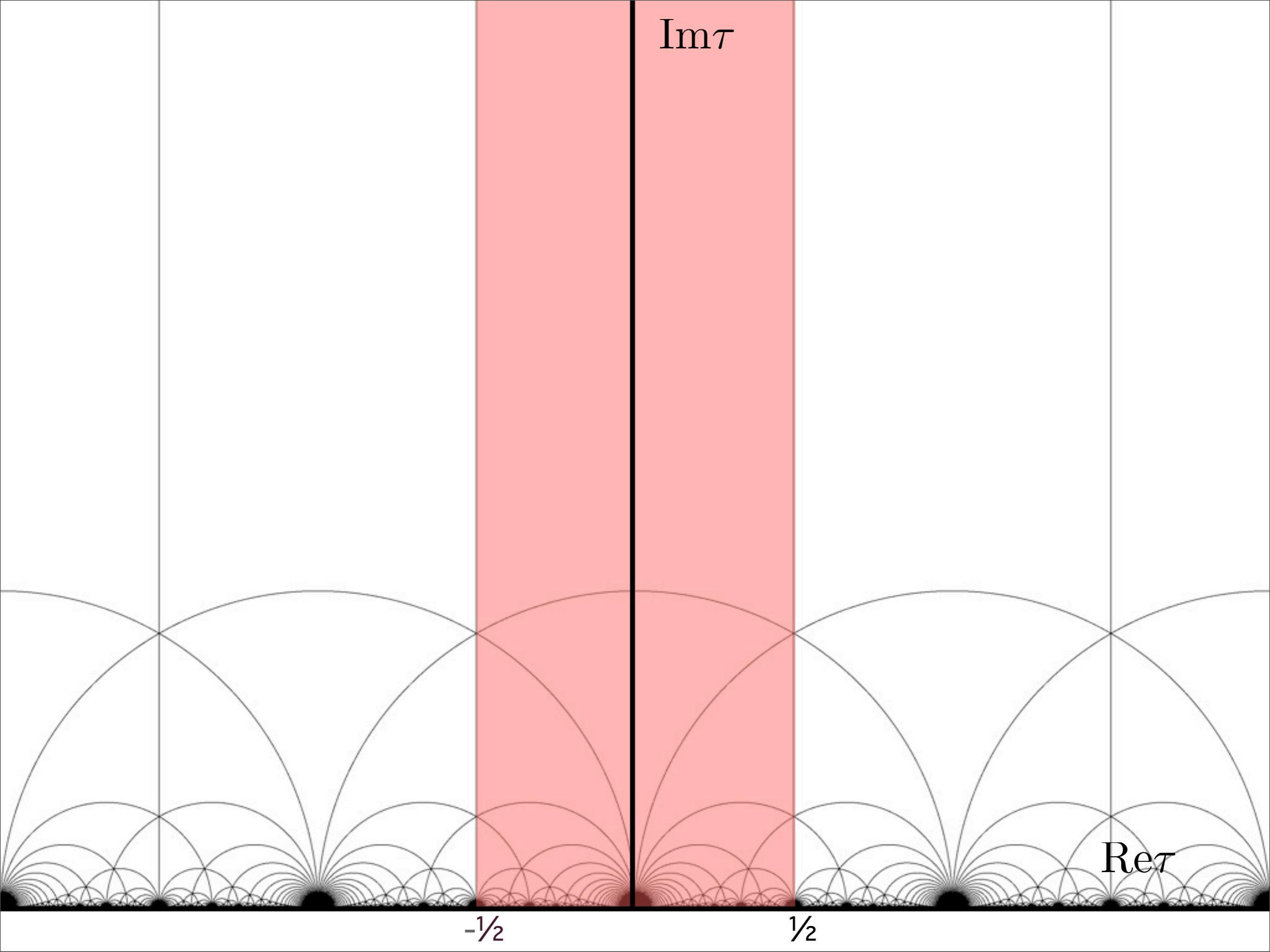
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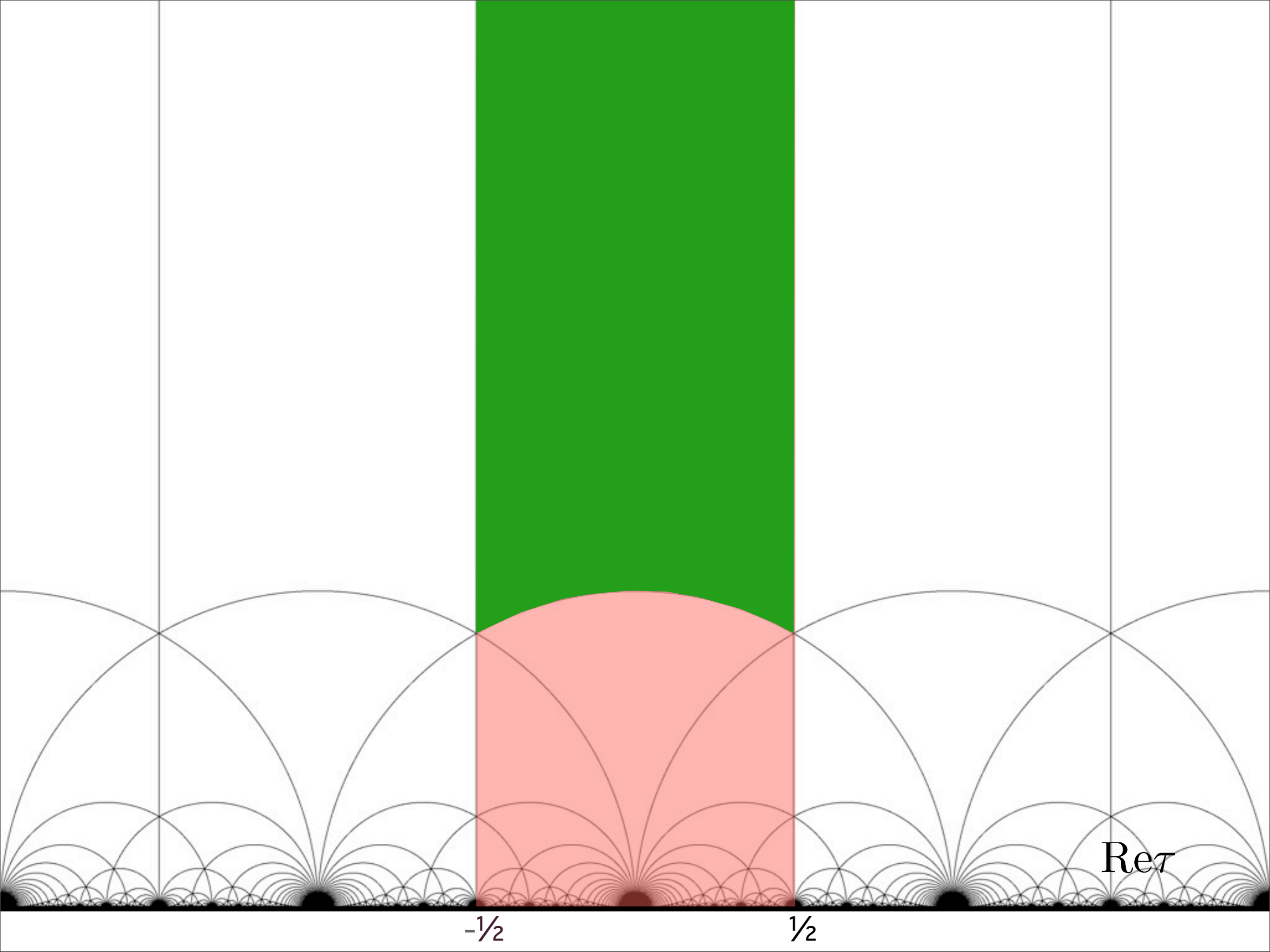
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HOW MANY?

Lerche, Lüst, Schellekens

“Chiral, Four-dimensional Heterotic Strings From Self-Dual Lattices”, 1986

$(\Gamma_{22} \times D_3 \times (D_7)^9)_L$, a Euclidean lattice of dimension 88. A lower limit on the total number of such lattices is provided by the Siegel mass formula [21] [22]

this number is of order 10^{1500} !

Even Self-dual lattices

Solutions to these constraints can be obtained from the partition functions of even self-dual lattices (all norms even, equal to its own dual (reciprocal) lattice).

$$\sum_{v \in L} e^{i\pi\tau v^2}$$

In 1986 we* showed how a class of 10 dimensional strings could be derived from the even self-dual lattices of dimension 24.


Later that year we** showed how a class of 4-dimensional strings could be derived from the even self-dual lattices of dimension 88.

()Ten-Dimensional Heterotic Strings From Niemeier Lattices, W. Lerche, D. Lüst and A.N. Schellekens (1986)*

*(**)Chiral Four-Dimensional Heterotic Strings from Selfdual Lattices, W. Lerche, D. Lüst and A.N. Schellekens, (1986)*

$$N_{8k} > \sum_{\Lambda} \frac{1}{|\text{Aut}(\Lambda)|} = \frac{|B_{4k}|}{8k} \prod_{j=1}^{4k-1} \frac{|B_{2j}|}{4j}$$

Dimension	Estimate	Total
8	2.8×10^{-9}	1
16	4.9×10^{-18}	2
24	15.8×10^{-15}	24
32	8.0×10^7	?
...		
88	$\approx 10^{1500}$?

The image shows the front cover of a book. The cover is a solid, bright orange color. In the center, there is a white rectangular border. Inside this border, the title 'Naar een waardig slot' is printed in a dark blue, serif font. Below the title, the author's name 'Bert Schellekens' is printed in a smaller, italicized, dark blue serif font. The book is shown at a slight angle, with the spine visible on the left side.

Naar een waardig slot

Bert Schellekens

Dutch version
(1998)

physics/0604134



“I have the impression that many of my colleagues hope to find a kind of mathematical formula that has only one solution. That single solution should then correspond to our four-dimensional world, including all quarks, leptons and the four basic forces. Also the values of the nineteen (or more) parameters, such as the masses of all particles, should then ultimately emerge as the outcome of a mathematical computation.”

“Our entire existence depends on a series of subtle processes that occurred during the evolution of the universe. These processes have finally led to a planet where, for example, the crucial element Carbon occurs with sufficient abundance. Various steps in this process depend critically on the parameters of the Standard Model, such as the masses of particles and the strength of interactions. It seems often easy to demonstrate that even small changes of certain parameters would obstruct the entire process.



“From this point of view it would seem absurd that exactly those parameter values would follow from a mathematical computation. We would be left with a much bigger riddle than the one we are trying to solve.

For this reason I was very satisfied when it turned out that String Theory was highly non-unique.

If our planet were the only one in the Universe, it would be a mystery why precisely that single planet would allow life. The fact that there are billions of planets makes the mystery considerably less severe. Analogously, the fact that many kinds of universes are possible makes the existence of conditions for intelligent life in our universe considerably less absurd than if there would be just one possibility.”

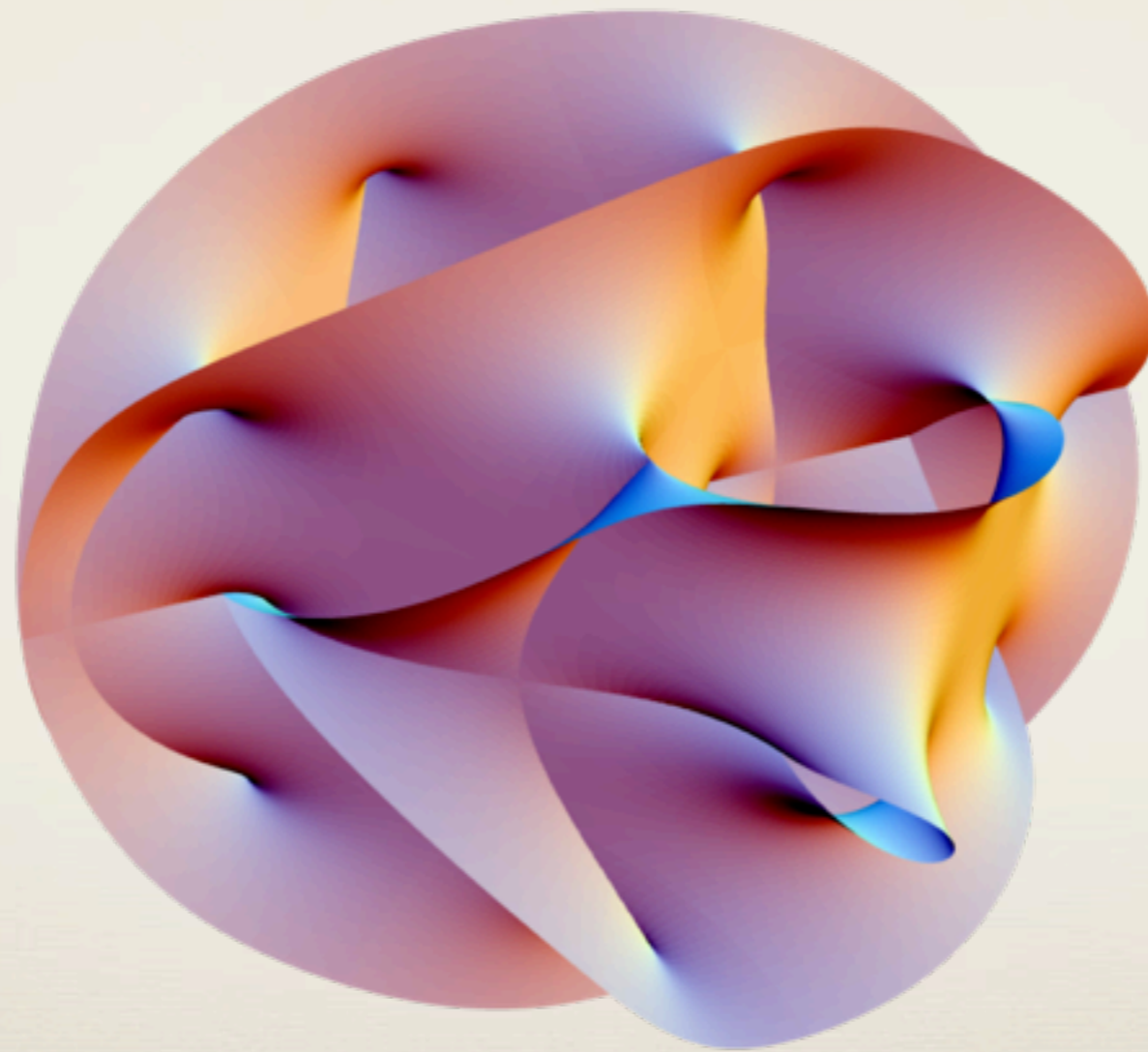


“This kind of reasoning is often referred to as the ‘anthropic principle’. In reality this is a collective name for a variety of ideas, some of which I find quite nonsensical. The anthropic principle states that the universe we observe is characterized by the fact that we exist as observers. It is hard to disagree with this. One can, however, disagree with the consequences that some people derive from it.

As far as I am concerned the anthropic principle only makes sense if our universe is not the only possible one. Furthermore it only makes sense within a completely consistent theory. Otherwise we do not know which changes of the parameters of our universe make sense. For example, it could well be that we are not allowed to change the up/down quark mass ratio at all. Although I would like to have many options for the laws of nature of our universe, I would still prefer the fundamental theory to be unique. String theory seems to accommodate these two demands that at first sight seem contradictory: according to our present insights there is just one theory, but many ground states are possible. This is really the best outcome one could imagine.”

Fundamental Theory Requirements

III: Dynamical Parameters



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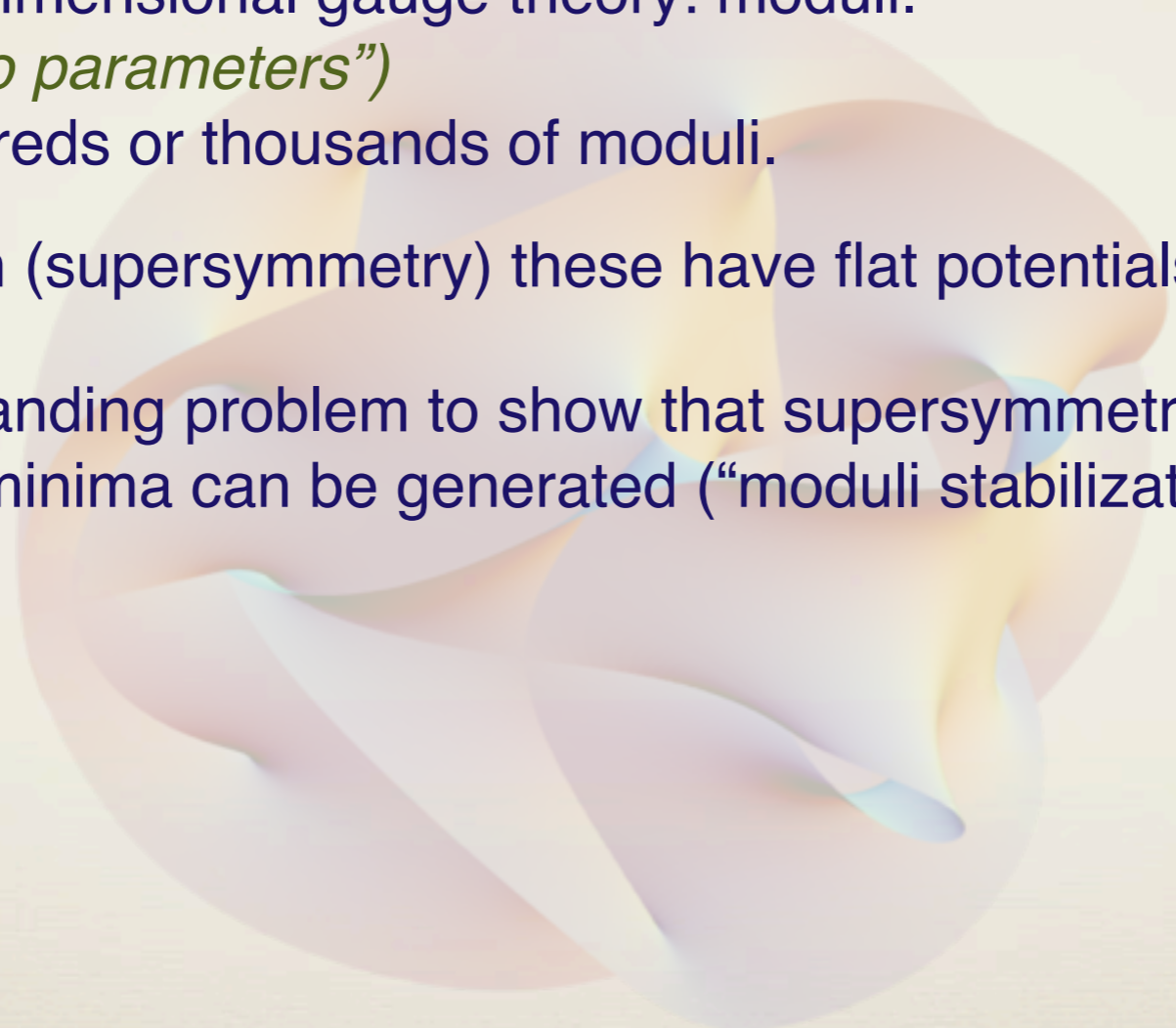
Shapes and size of the handles of internal manifolds give rise to dynamical parameters in the resulting four-dimensional gauge theory: moduli.

(“String theory has no parameters”)

Often there are hundreds or thousands of moduli.

To first approximation (supersymmetry) these have flat potentials.

It has been a long-standing problem to show that supersymmetry can be broken and that potentials with local minima can be generated (“moduli stabilization”)



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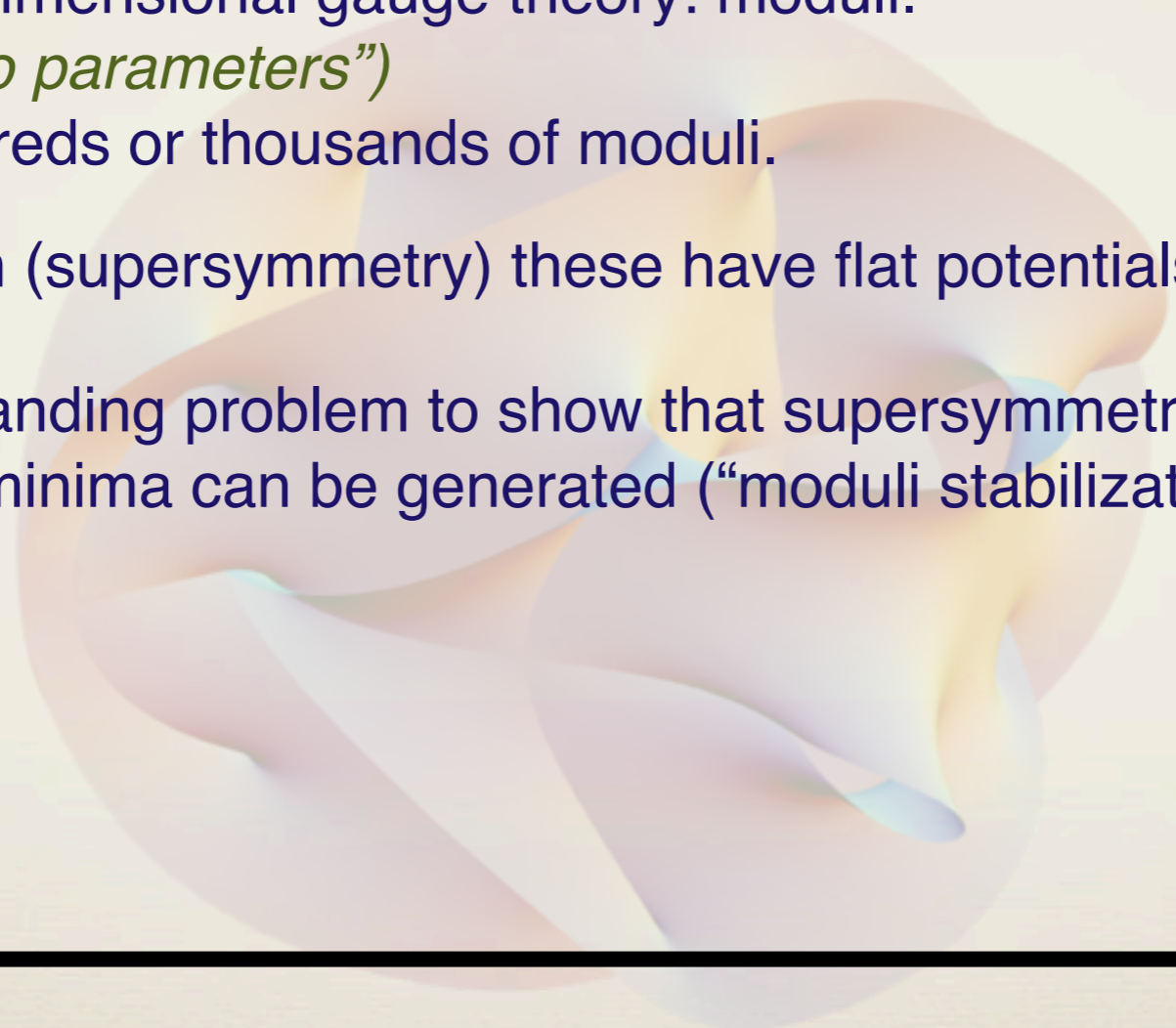
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Fundamental Theory Requirements

IV: The Cosmological Constant

Bousso and Polchinski (2000)

Quantized generalizations of electric & magnetic fields (“fluxes”) living in Minkowski and internal dimensions:

- May wind N times around closed cycles of the internal manifold to help stabilizing some moduli
- Have space-time components that contribute to the cosmological constant.

$$A_{\mu\nu\rho} \rightarrow F_{\mu\nu\rho\sigma} = \partial_{[\sigma} A_{\mu\nu\rho]}$$

Action with four-form contribution

$$S = \int d^4x \sqrt{-g} \left(\frac{1}{2\kappa^2} R - \Lambda_{\text{bare}} - \frac{Z}{48} F_4^2 \right)$$

Solution to equations of motion

$$F^{\mu\nu\rho\sigma} = c\epsilon^{\mu\nu\rho\sigma}$$

Contribution to the cosmological constant

$$\Lambda = \Lambda_{\text{bare}} + \frac{1}{2} \frac{Zc^2}{2}$$

In String Theory:

- The constant c is quantized
- There are many such four-form fields

$$\Lambda = \Lambda_{\text{bare}} + \frac{1}{2} \sum_i^{N_{\text{flux}}} n_i^2 y_i^2$$

If the values of y_i are incommensurate and N_{flux} sufficiently large, Λ can be tuned to a very small value (starting with negative Λ_{bare} of natural size).

$$N_{\text{vacua}} \approx [N_{\text{values}}]^{N_{\text{flux}}}$$

~ 2003

The basic estimate for numbers of flux vacua [4] is

$$\mathcal{N}_{vac} \sim \frac{(2\pi L)^{K/2}}{(K/2)!} [c_n]$$

where K is the number of distinct fluxes ($K = 2b_3$ for IIB on CY_3) and L is a “tadpole charge” ($L = \chi/24$ in terms of the related CY_4). The “geometric factor” $[c_n]$ does not change this much, while other multiplicities are probably subdominant to this one.

Typical $K \sim 100 - 400$ and $L \sim 500 - 5000$, leading to $\mathcal{N}_{vac} \sim 10^{500}$.

(M. Douglas)

The Anthropic Landscape of String Theory

L. Susskind

Department of Physics
Stanford University
Stanford, CA 94305-4060

A. Linde

Eternally Existing Selfreproducing Chaotic Inflationary Universe. **Phys.Lett.B175:395-400,1986**

If our universe would consist of one domain only (as it was believed several years ago), it would be necessary to understand why Nature has chosen just this one type of compactification, just this type of symmetry breaking, etc. At present it seems absolutely improbable that all domains contained in our exponentially large universe are *of the same type*. On the contrary, *all* types of mini-universes in which inflation is possible should be produced during the expansion of the universe, and it is unreasonable to expect that our domain is the only possible one or the best one. From this point of view, an enormously large number of possible types of compactification which exist e.g. in the theories of superstrings should be considered not as a difficulty but as a virtue of these theories, since it increases the probability of the existence of mini-universes in which life of our type may appear. The old question why our universe is the only possible one is now replaced by the question in which theories the existence of mini-universes of our type is possible. This question is still very difficult, but it is much easier than the previous one. In our opinion, the modification of the point of view on the global structure of the universe and on our place in the world is one of the most important consequences of the development of the inflationary-universe scenario.

DISCUSSION

So what would be better?

How many “solutions” should there be?

- 1
- 10^{30}
- 10^{500}
- $10^{10^{500}}$
- Infinitely dense (Q)
- Continuous infinity (R)

- Infinite sequence of effective theories.
- Fundamentally uncertain (Heisenberg)
- Undecidable (Gödel)
- Beyond science.

- We are too stupid and/or ignorant, and we will never know.

So what would be better?

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How many “solutions” should there be?

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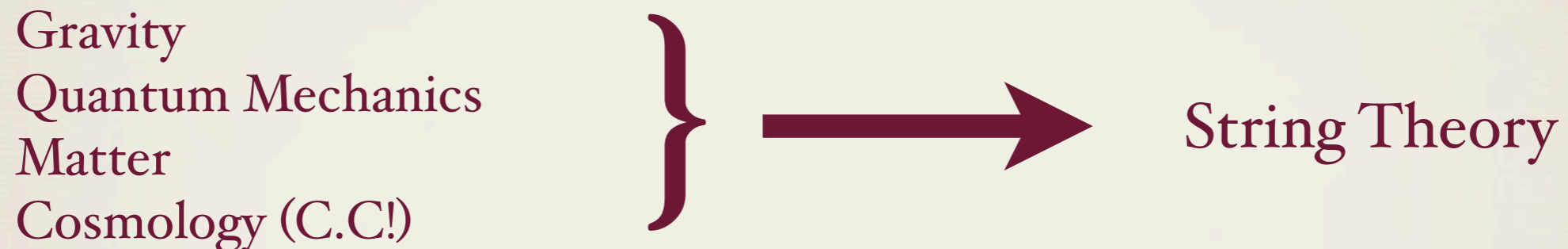
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Will we ever know?

Three difficult stages:

- * Establish the necessity of string theory:



- * Establish that string theory does indeed have a landscape with stabilized moduli and broken supersymmetry.
- * Establish that the SM is indeed in that landscape (probably by studying distributions.)

Each of these may fail...

Falsification?

Not “on command”.

But plenty of things could go wrong:

- Strange results in gravity, cosmology, astrophysics
(cosmological constant, Pioneer, flyby anomalies, photon dispersion, MOND...)
- Strange results from the LHC
(matter in large representations, violations of asymptotic freedom, no Higgs...)
- Variations in constants of nature
*(for example α , m_p/m_e)**

There might also be positive evidence:

- Large extra dimensions
- Extra U(1)'s

(Banks, Dine, Douglas*

The hierarchy problem

The usual argument for low energy supersymmetry:

“We need bose-fermion cancellation to explain why the weak scale does not get large quadratic corrections”.

But the cosmological constant gets much larger quartic corrections.

If we accept that these “just” cancel, why do we need a special mechanism for the weak scale hierarchy?

Both hierarchies are anthropically needed!

A small dilemma:

From the landscape point of view, finding “just the Higgs” might seem attractive. But it gives little information.

Finding supersymmetry would be a puzzle from the anthropic landscape point of view. But it does give lots of useful information.

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- *“String theory is just a framework for discussing problems in Quantum Gravity”*
- *“The anthropic principle is not even worth the name principle”*

The moral of the story

- Just like the emperor, we are so convinced of our own importance that we believe we must be unique.
*(and this has happened many times before...
but will this be the last time?)*
- It is often hard to see the obvious, if you don't like what you see