

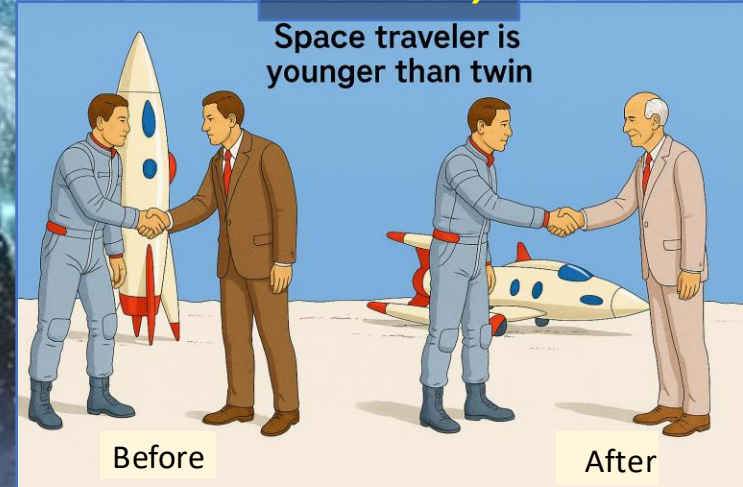
The Relativistic Quantum World

A lecture series on
Relativity Theory and Quantum Mechanics

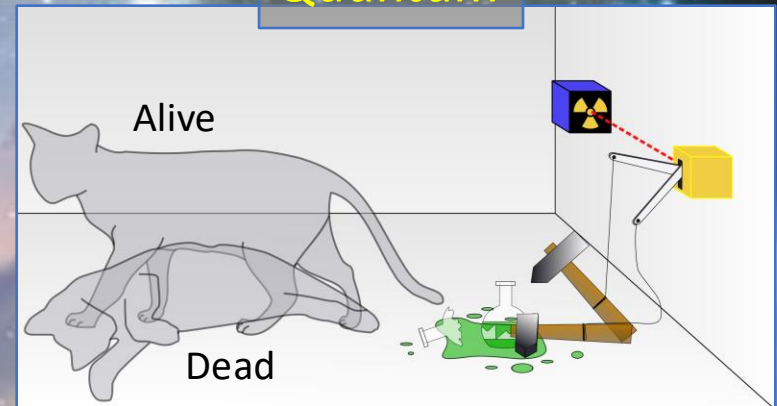
Marcel Merk
Studium Generale Maastricht
Sep 10 – Oct 8, 2025

Relativity

Space traveler is
younger than twin



Quantum



Relativity

Sep. 10:

Lecture 1: The Principle of Relativity and the Speed of Light
Lecture 2: Time Dilation and Lorentz Contraction

Sep. 17:

Lecture 3: The Lorentz Transformation and Paradoxes
Lecture 4: General Relativity and Gravitational Waves

Quantum Mechanics

Sep. 24:

Lecture 5: The Early Quantum Theory
Lecture 6: Feynman's Double Slit Experiment

Oct. 1 :

Lecture 7: Wheeler's Delayed Choice and Schrodinger's Cat
Lecture 8: Quantum Reality and the EPR Paradox

Standard Model

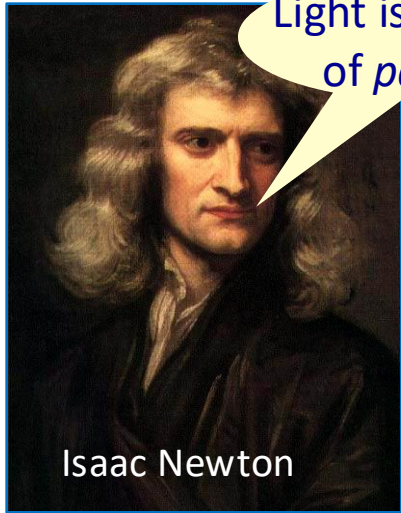
Oct. 8:

Lecture 9: The Standard Model and Antimatter
Lecture 10: Why is there something rather than nothing?

Lecture notes, written for this course, are available: www.nikhef.nl/~i93/Teaching/
Prerequisite for the course: High school level physics & mathematics.

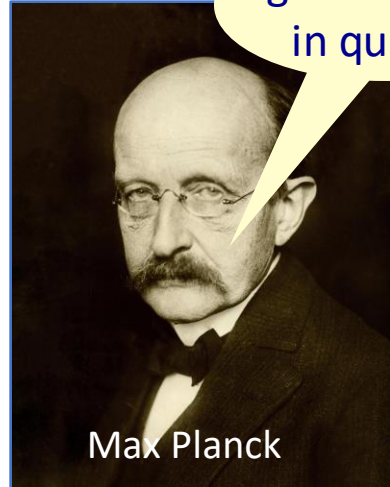
Quantum Mechanics

2



Light is a stream
of *particles*

Isaac Newton



Light is *emitted*
in quanta

Max Planck

No, similar to
sound light consists
of *waves*



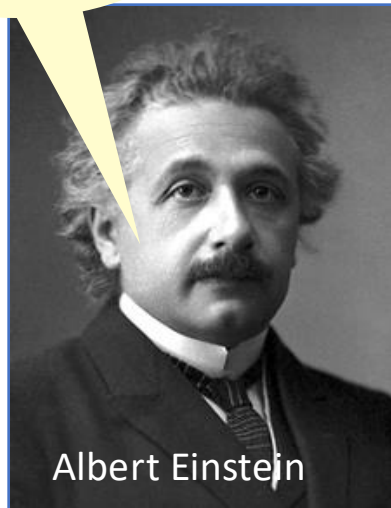
Christiaan Huygens

Yes, because
it *interferes*



Thomas Young

The *nature* of
light is quanta



Albert Einstein

Yes, because
photons collide!



Arthur Compton

Particles have a
wave nature:
 $\lambda = h/p$



Louis de Broglie

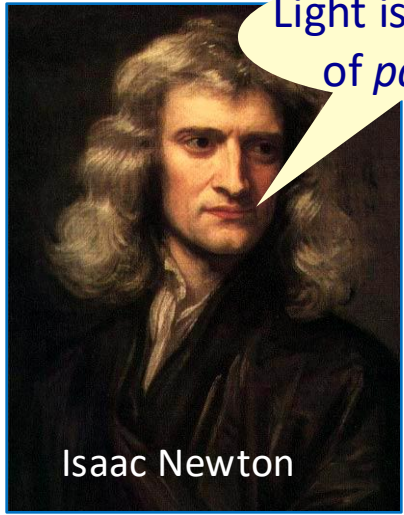
Particles are
probability waves



Niels Bohr

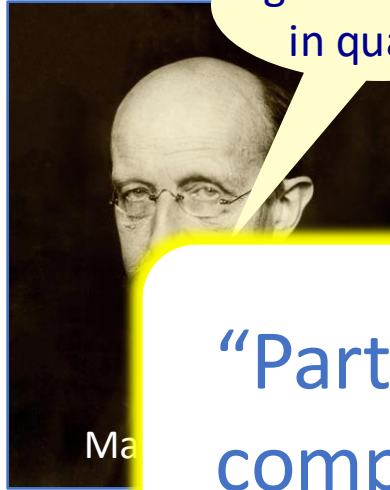
Quantum Mechanics

2



Isaac Newton

Light is a stream of *particles*



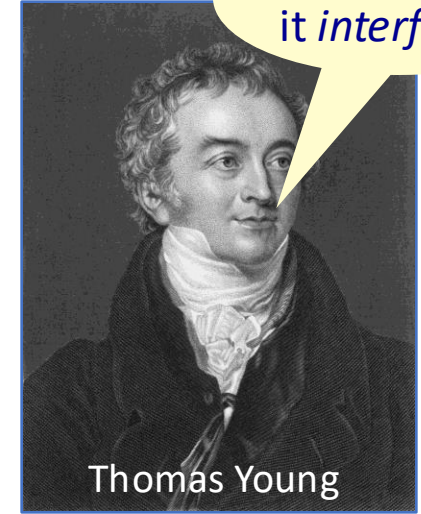
Ma

Light is *emitted* in quanta

No, similar to sound light consists of *waves*



gens

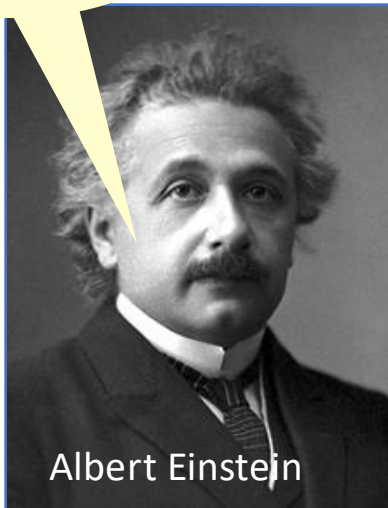


Thomas Young

Yes, because it *interferes*

“Particle” and “Wave” are complementary aspects.

The *nature* of light is quanta



Albert Einstein



Arthur Compton

photons collide!



Louis de Broglie

$\lambda = h/p$



Niels Bohr

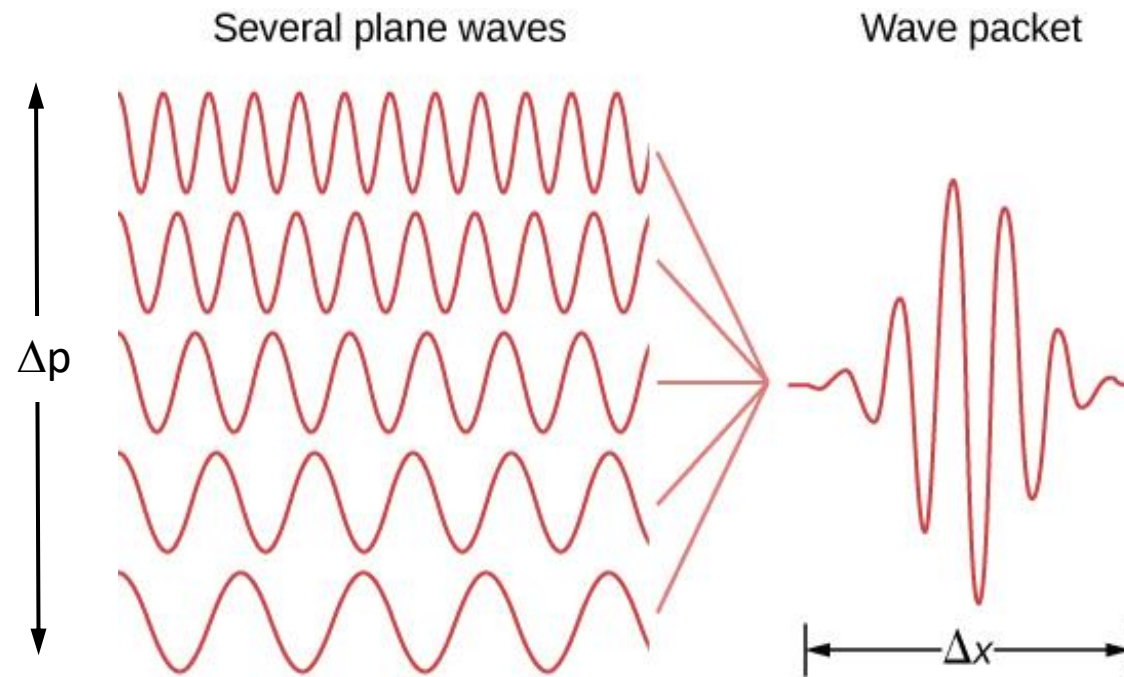
Particles are *probability waves*

Uncertainty Relation

3

It is *not* possible to determine *position* and *momentum* at the same time:

$$\Delta x \Delta p \geq \frac{\hbar}{2}$$



$$p = \frac{h}{\lambda} = \frac{hf}{c}$$

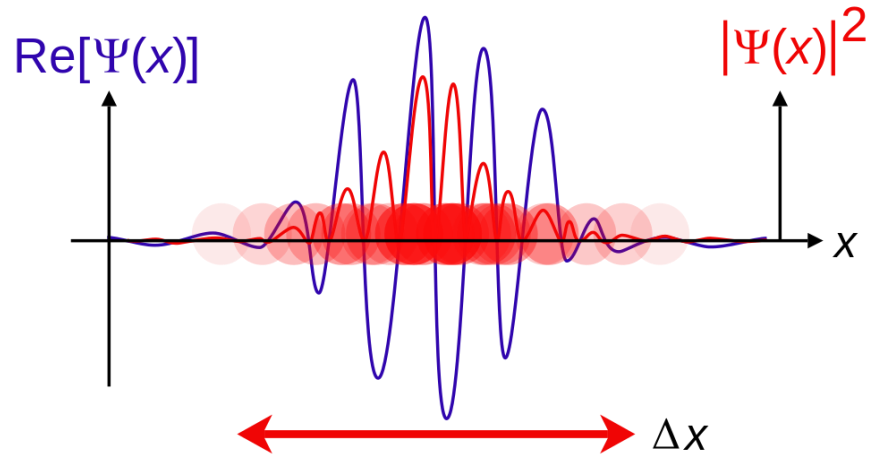


A particle *does not have* well defined position and momentum at the same time.

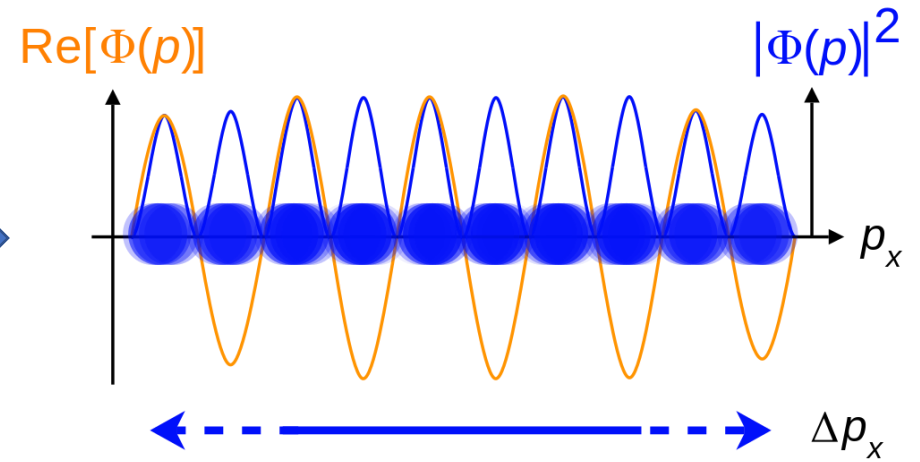
The wave function ψ

4

Position fairly known



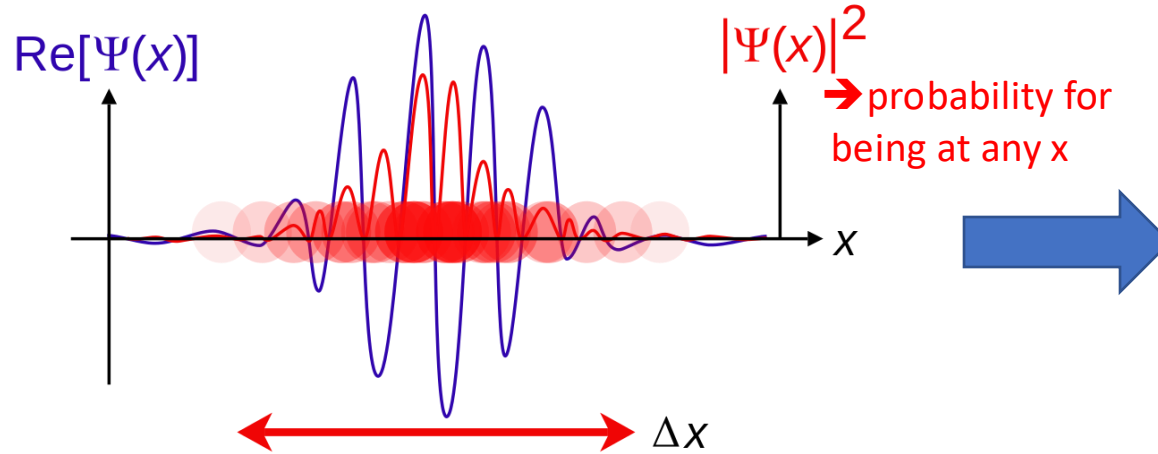
Momentum badly known



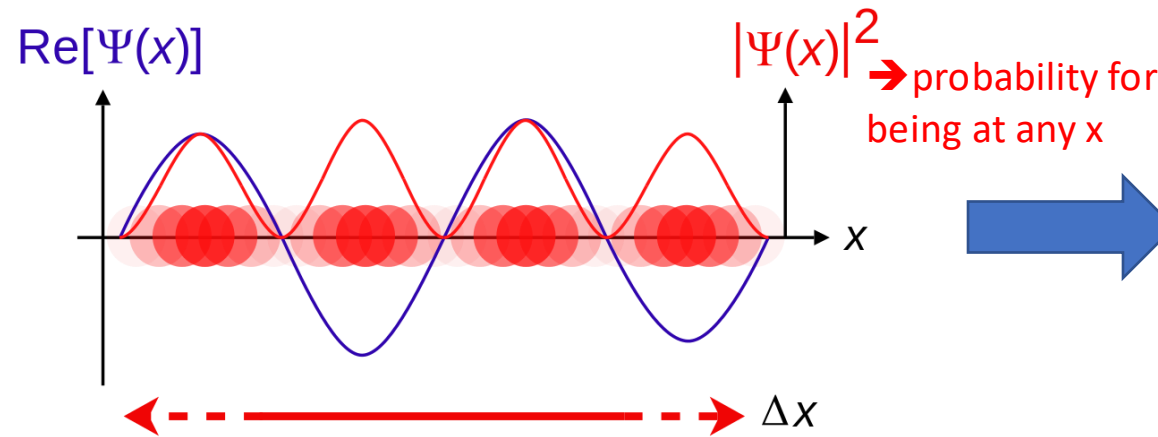
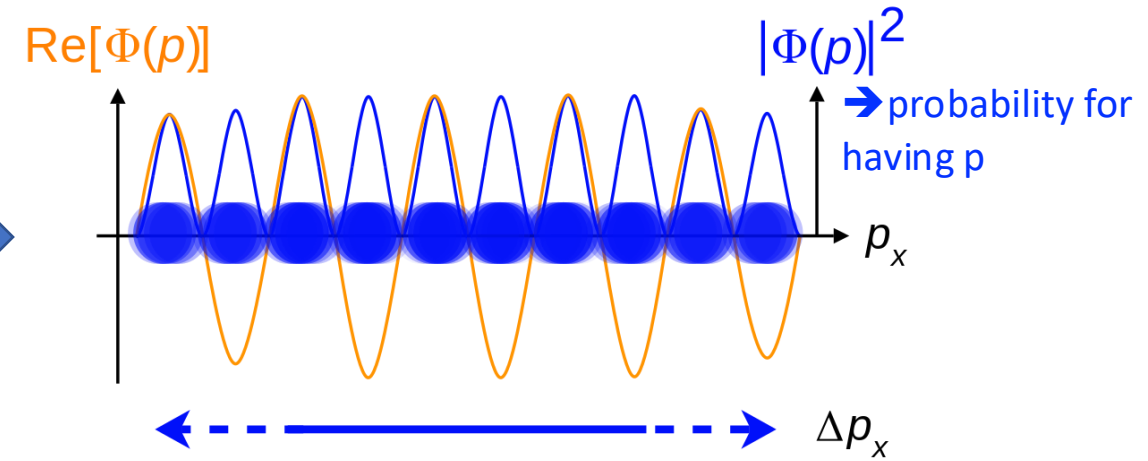
The wave function ψ

4

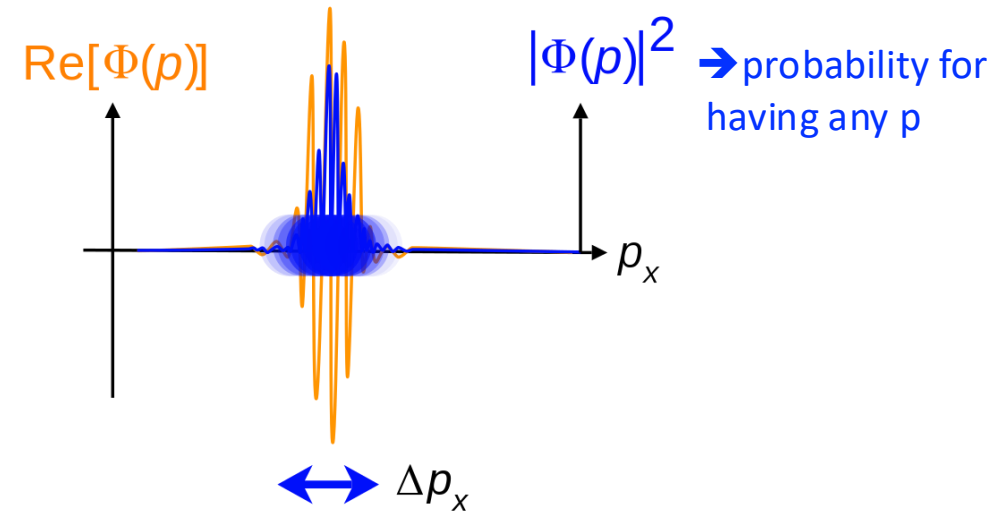
Position fairly known



Momentum badly known



Position badly known



Momentum fairly known

Lecture 6

Feynman's Double Slit Experiment

“It doesn't matter how beautiful your theory is, it doesn't matter how smart you are. If it doesn't agree with experiment it's wrong.”

- Richard Feynman

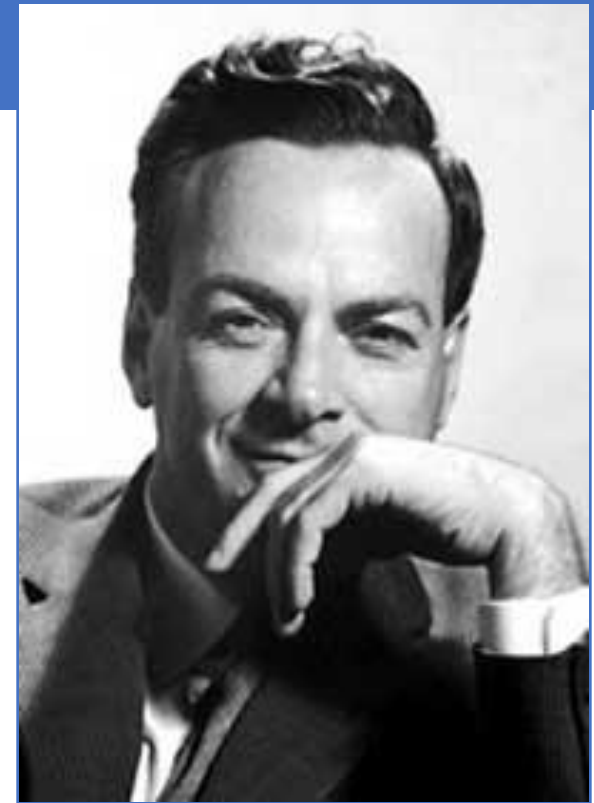
Richard Feynman (1918 – 1988)

6

Nobelprize 1965: Quantum Electrodynamics
(Path Integral formulation of quantum mechanics)

Mostly known from:

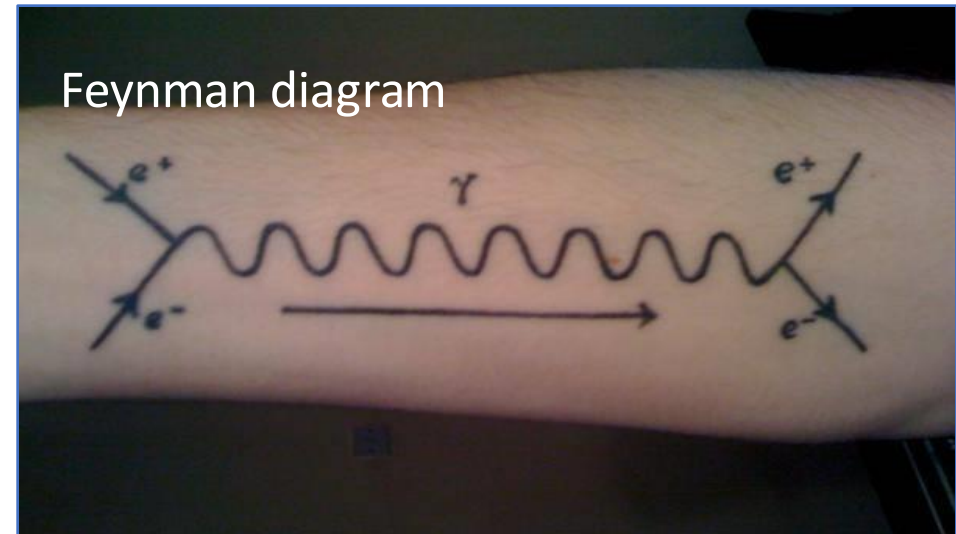
- Feynman diagrams
- Challenger investigation
- Popular books



Challenger disaster 1986



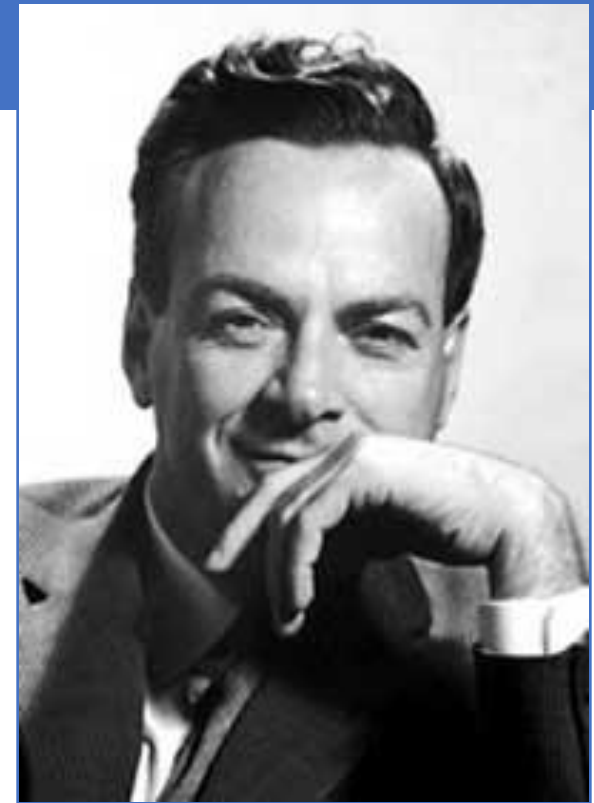
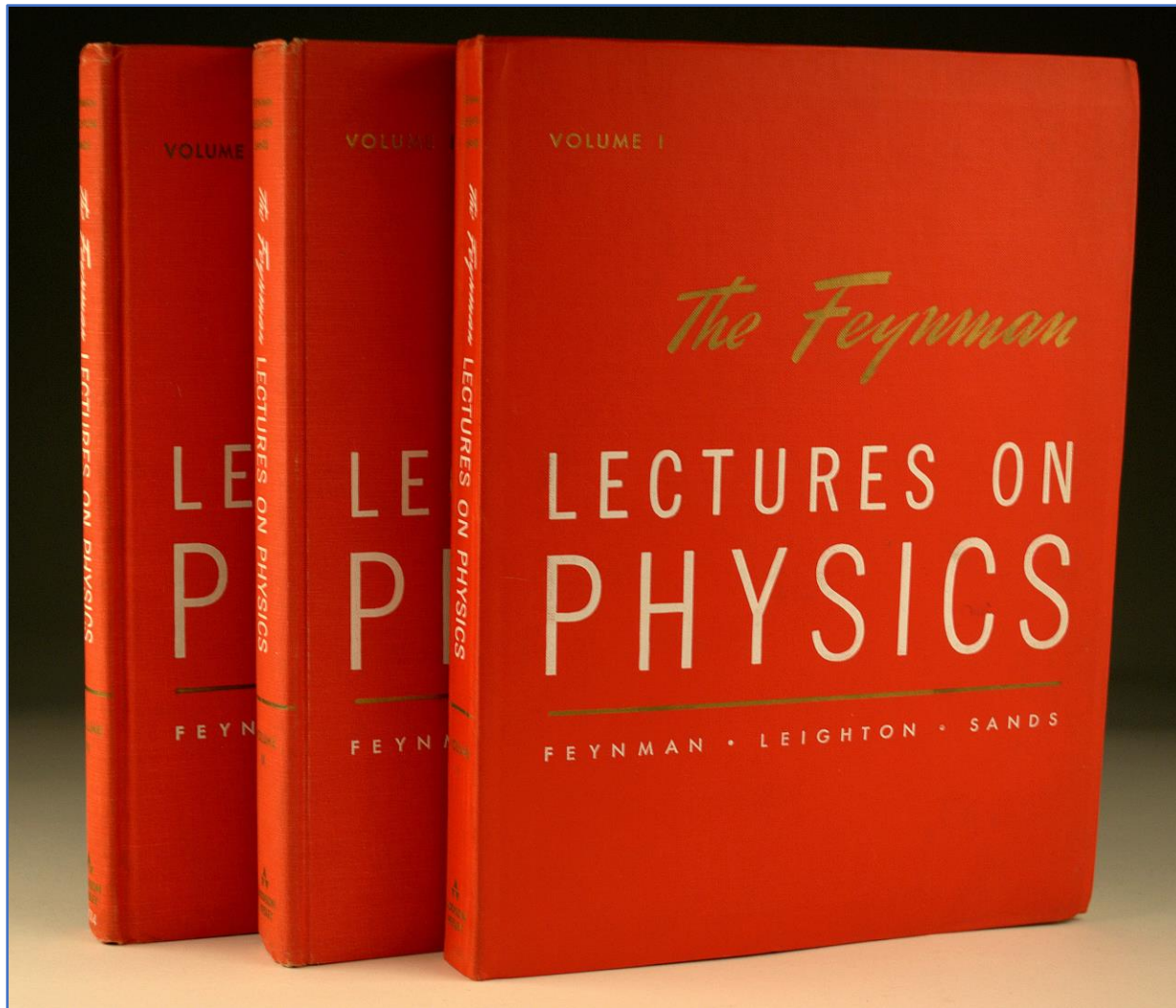
Feynman diagram



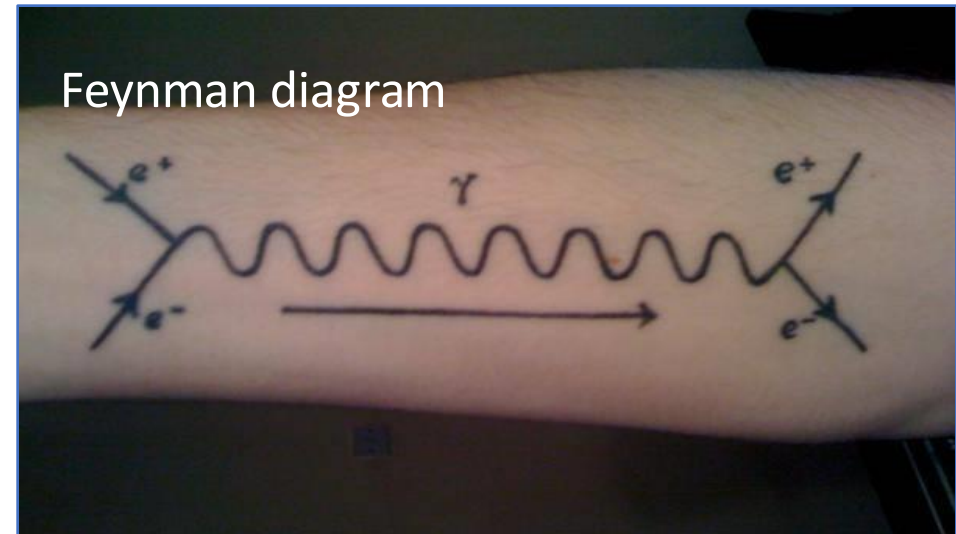
Richard Feynman (1918 – 1988)

7

Nobelprize 1965: Quantum Electrodynamics
(Path Integral formulation of quantum mechanics)



Feynman diagram





The double slit experiment demonstrates the fundamental aspect of the quantum world.

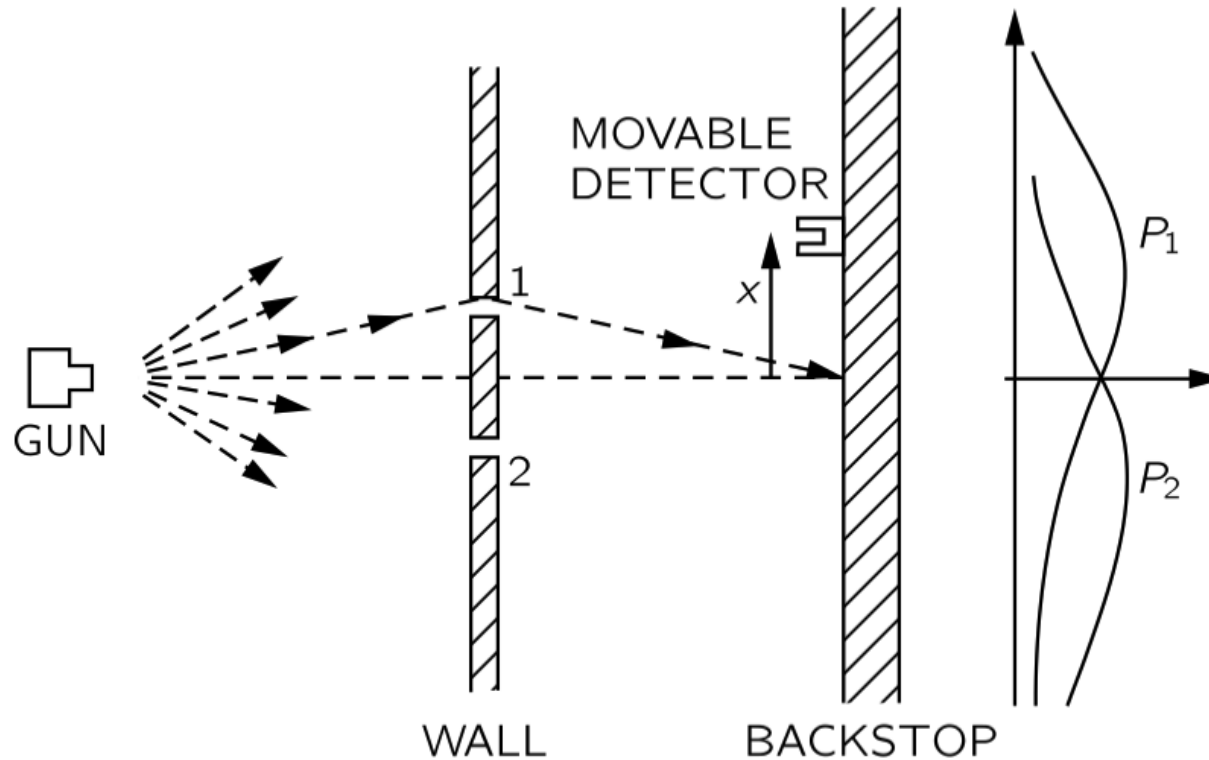
Case 1: An Experiment with Bullets



Case 1: Experiment with Bullets

10

A gun fires bullets in random direction. Slits 1 and 2 are openings through which bullets can pass. A moveable detector “collects” bullets and counts them.



Observation:
Bullets come in
“lumps”.

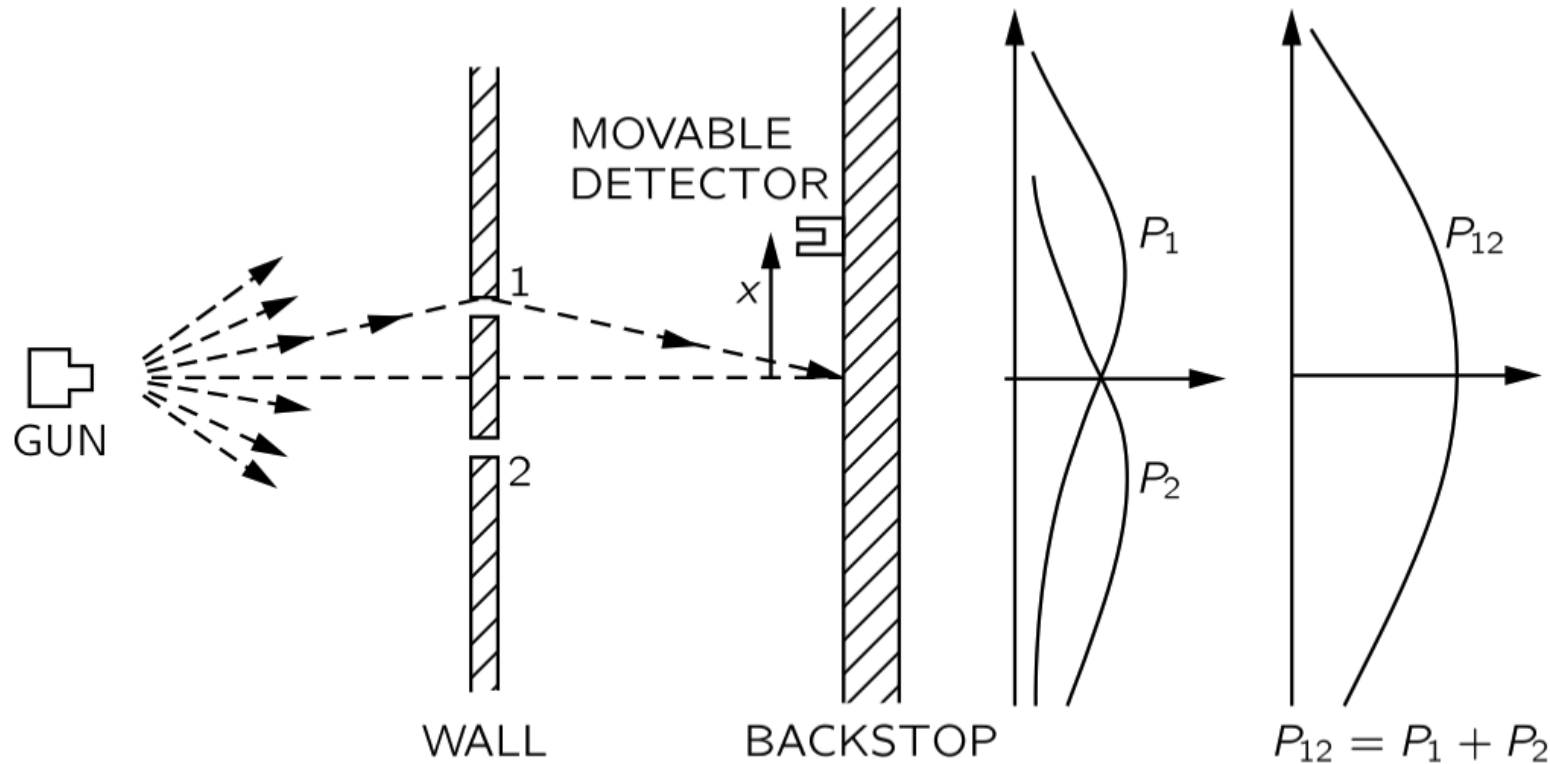
P_1 is the probability curve when only slit 1 is open
 P_2 is the probability curve when only slit 2 is open

What is the probability curve when both slit 1 and slit 2 are open?

Case 1: Experiment with Bullets

11

A gun fires bullets in random direction. Slits 1 and 2 are openings through which bullets can pass. A moveable detector “collects” bullets and counts them.

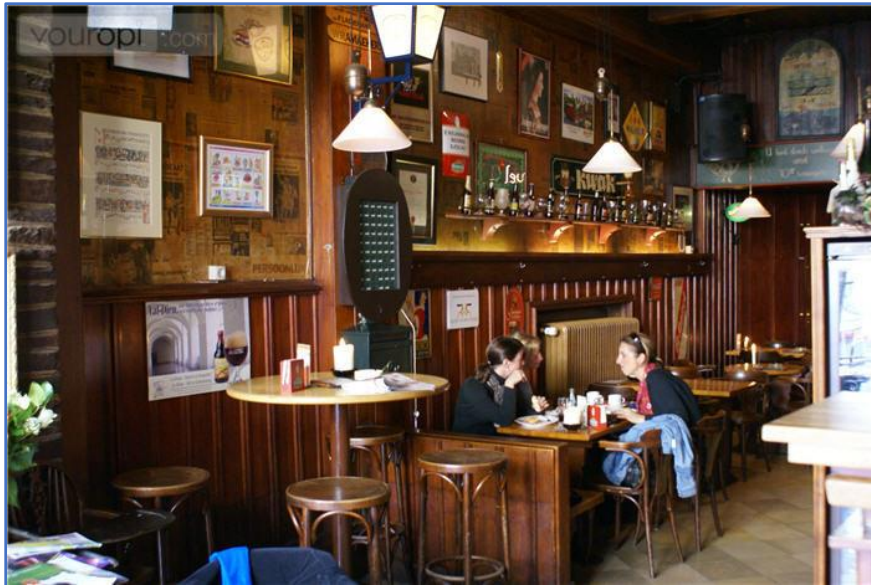


P_1 is the probability curve when only slit 1 is open
 P_2 is the probability curve when only slit 2 is open

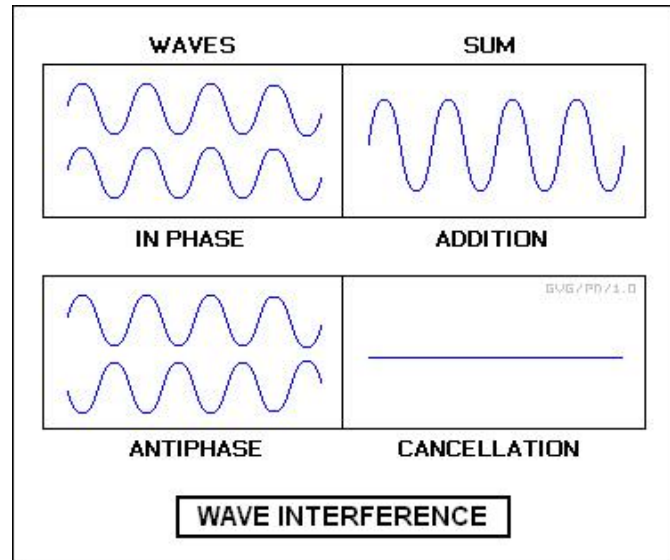
When both slits are open: $P_{12} = P_1 + P_2$

We can just add up the probabilities.

Case 2: An Experiment with Waves



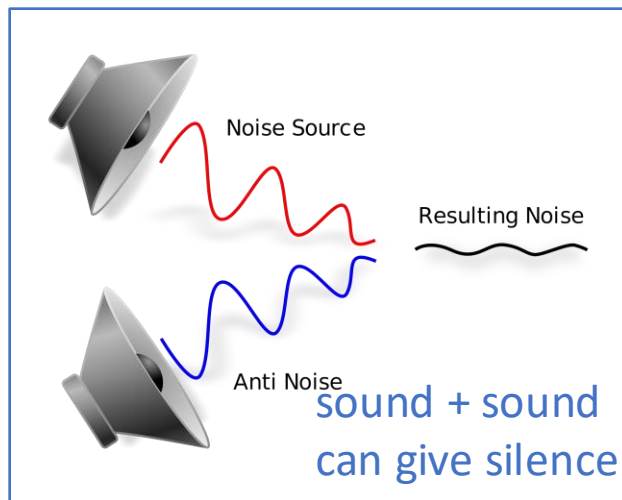
Waves: Interference principle:



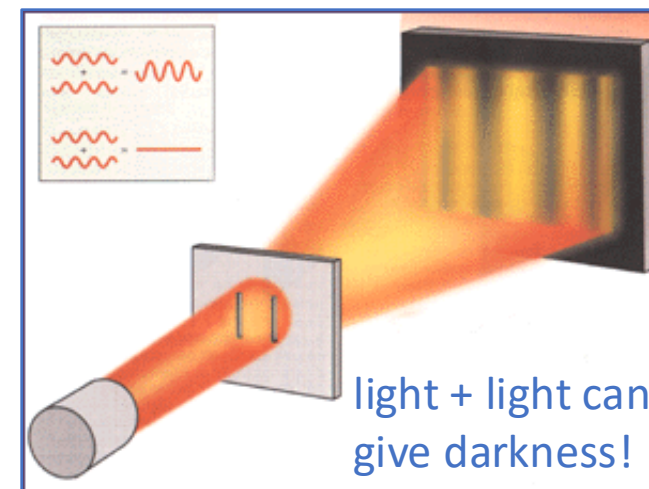
Water: Interference pattern:



Sound: Active noise cancellation:

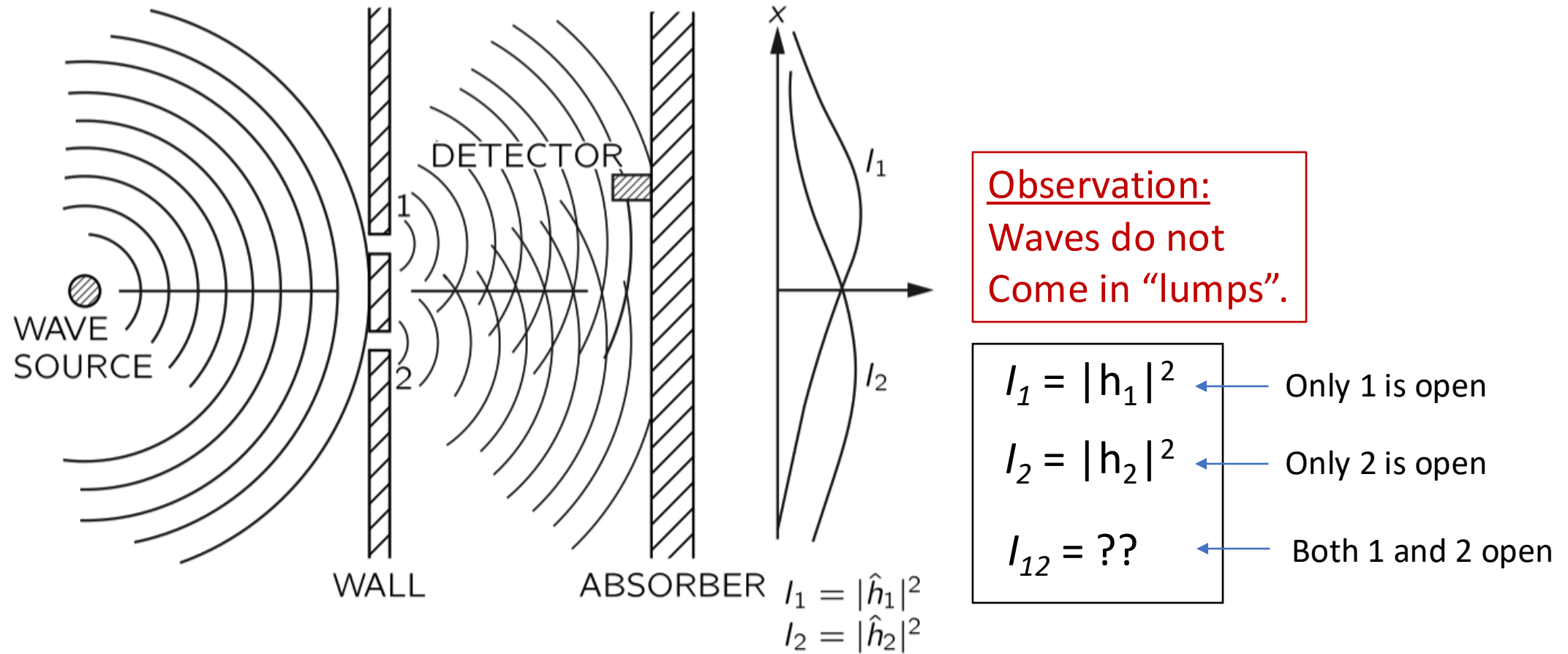


Light: Thomas Young experiment:



Case 2: Experiment with Waves

We replace the gun by a wave generator: think of water waves. Slits 1 and 2 act as new wave sources. The detector measures now the intensity (energy) in the wave.

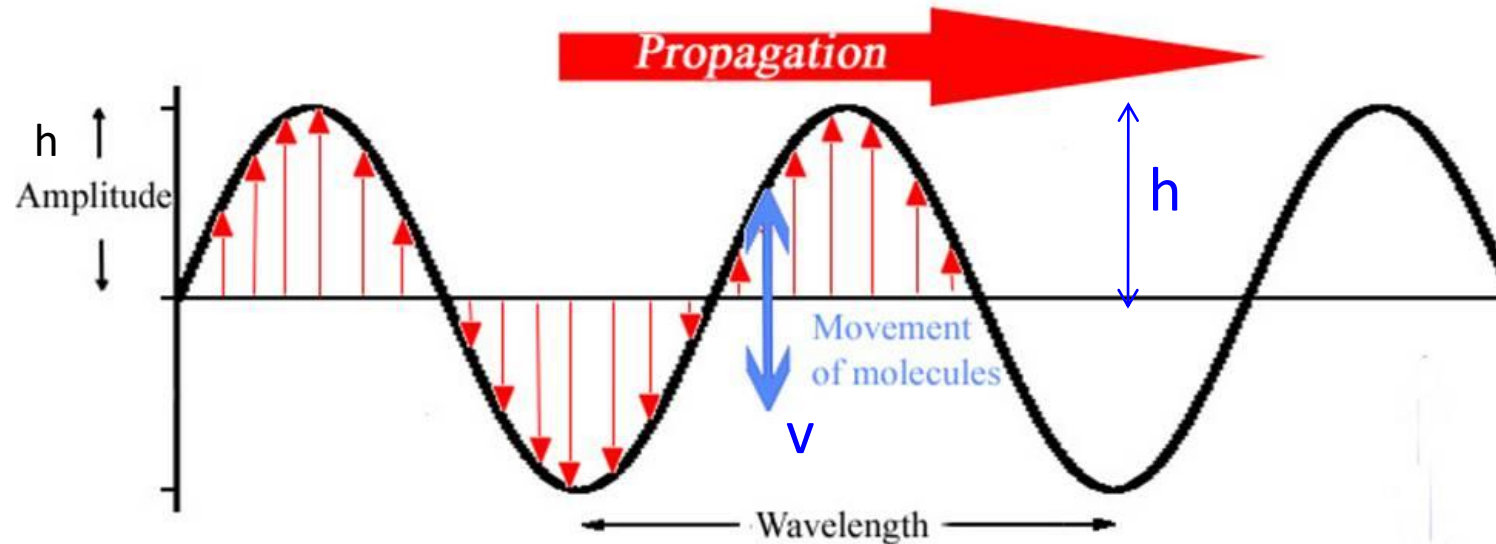


The intensity of a wave is the square of the amplitude...

Energy in the oscillation (up-down) movement of the molecules:

$E_{kin} = \frac{1}{2}mv^2$ and v is proportional to the amplitude or height: $v \approx h$

So that the intensity of the wave is: $I \approx h^2$



Formula for the resulting oscillation of a water molecule somewhere in the wave:

$$W(t) = h \cos(2\pi ft + \phi)$$

and the Intensity: $I = h^2$

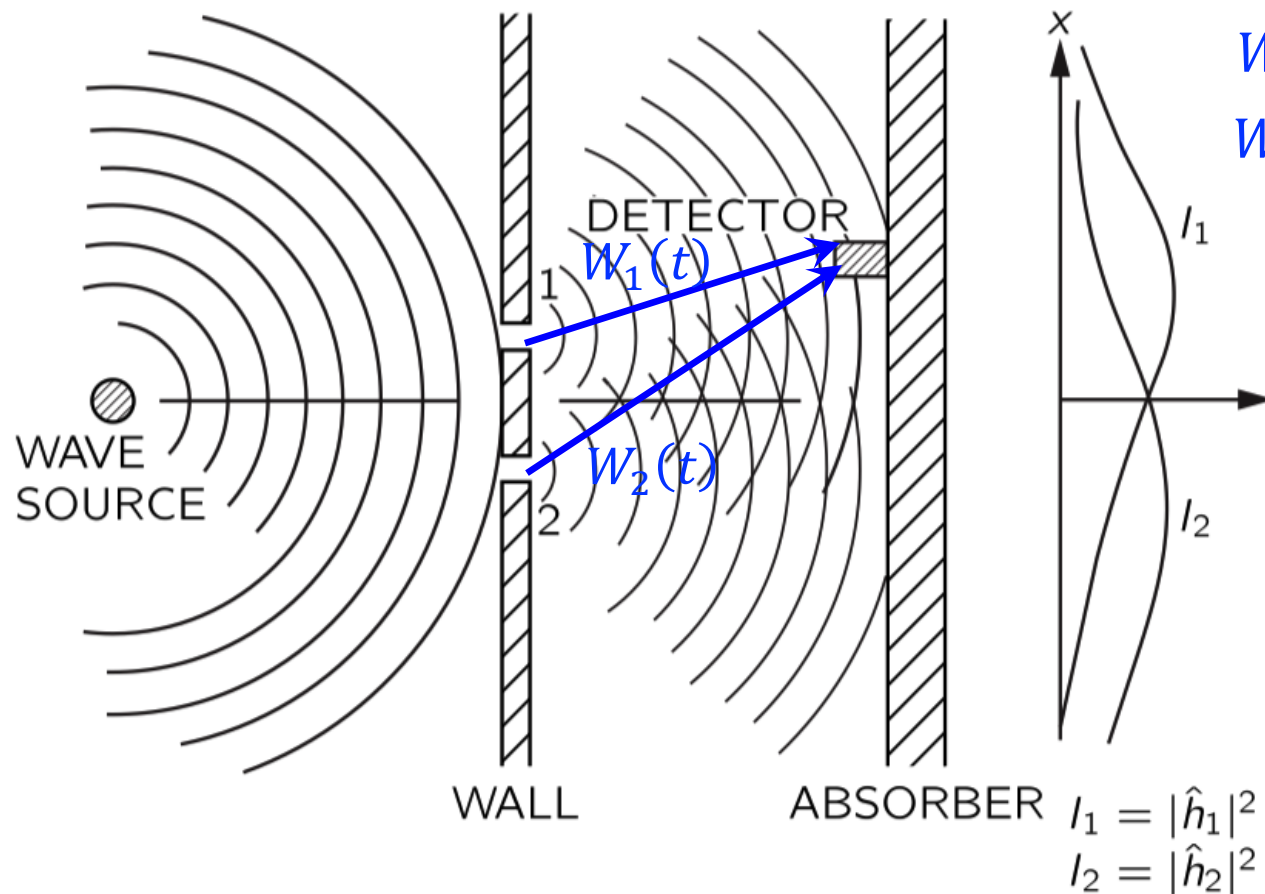
f = frequency

ϕ = phase

Case 2: Experiment with Waves

16

When both slits are open there are two contributions to the wave the oscillation at the detector: $R(t) = R_1(t) + R_2(t)$



$$W_1(t) = h_1 \cos(2\pi f t + \phi_1)$$

$$W_2(t) = h_2 \cos(2\pi f t + \phi_2)$$

ϕ_1 and ϕ_2 depend on distance to 1 and 2

$$I_1 = |h_1|^2$$

$$I_2 = |h_2|^2$$

$$I_{12} = ??$$

$$I_1 = |\hat{h}_1|^2$$
$$I_2 = |\hat{h}_2|^2$$

First combine: $W(t) = W_1(t) + W_2(t)$

Afterwards look at the amplitude and intensity of the resulting wave!

For math lovers: let's calculate

$$W_{12}(t) = h_1 \cos(2\pi f t + \phi_1) + h_2 \cos(2\pi f t + \phi_2)$$

Assume equal size waves: $h_1 = h_2 = h$

Find amplitude of sum wave $W_{12}(t)$.

From math textbook: $\cos(A) + \cos(B) = 2 \cos\left(\frac{1}{2}(A - B)\right) \cos\left(\frac{1}{2}(A + B)\right)$

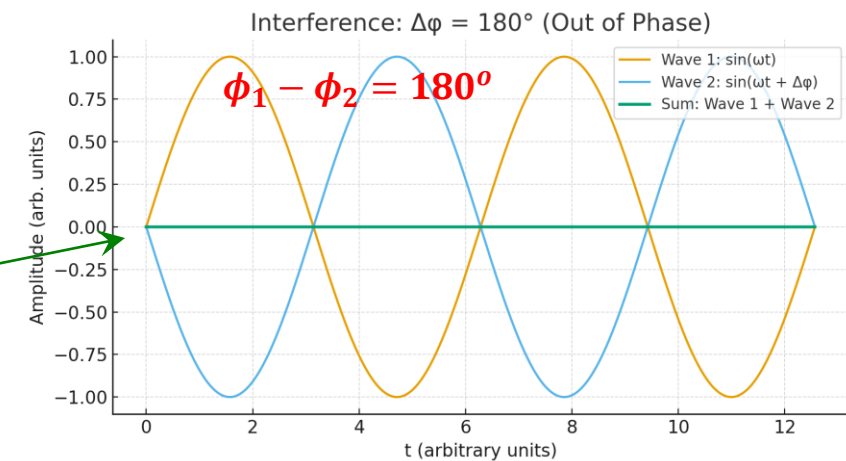
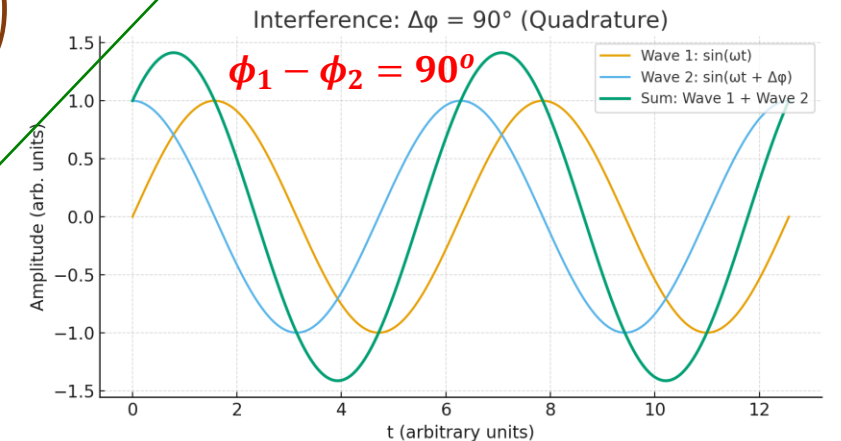
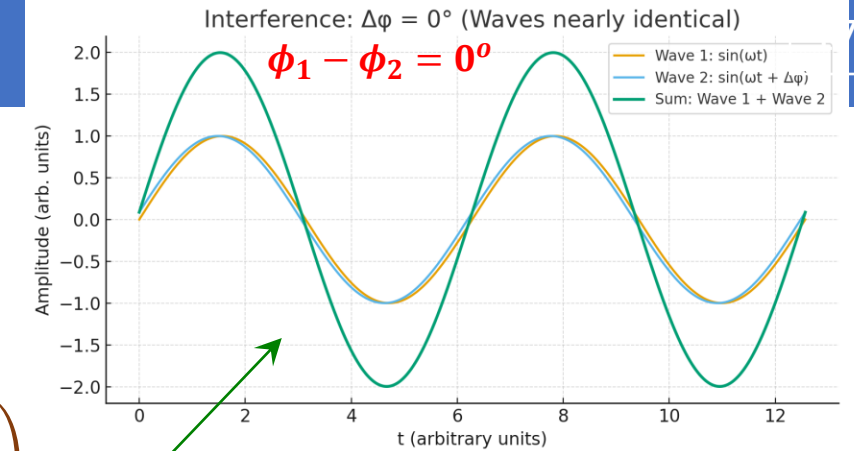
Use this to find:

$$W_{12}(t) = h' \cos\left(2\pi f t + \frac{1}{2}(\phi_1 + \phi_2)\right)$$

With $h' = 2h \cos\left(\frac{1}{2}(\phi_1 - \phi_2)\right)$

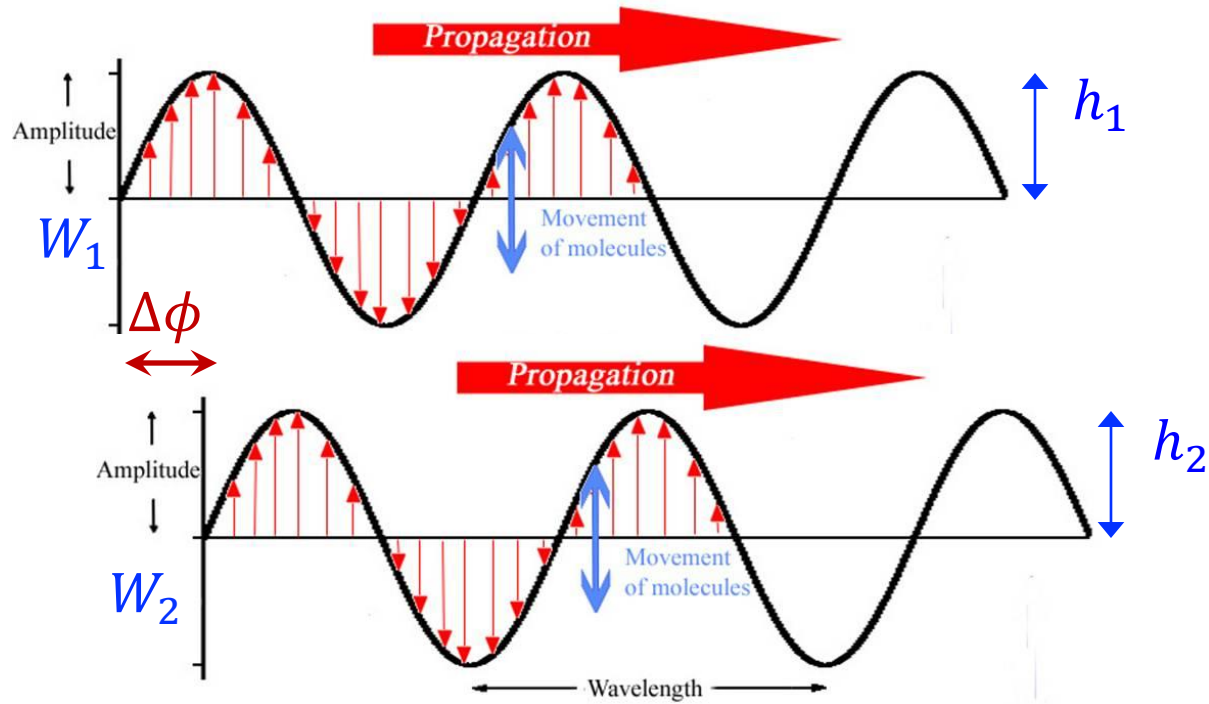
If $\phi_1 - \phi_2 = 0^\circ$ then double resulting amplitude:
constructive interference

If $\phi_1 - \phi_2 = 180^\circ$ then zero resulting amplitude:
destructive interference



Interference of Waves

18

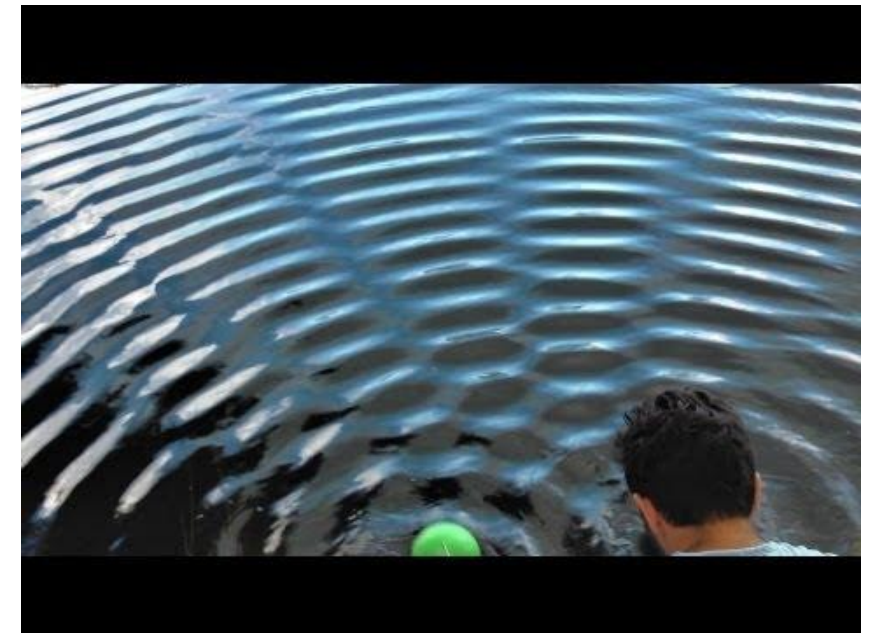
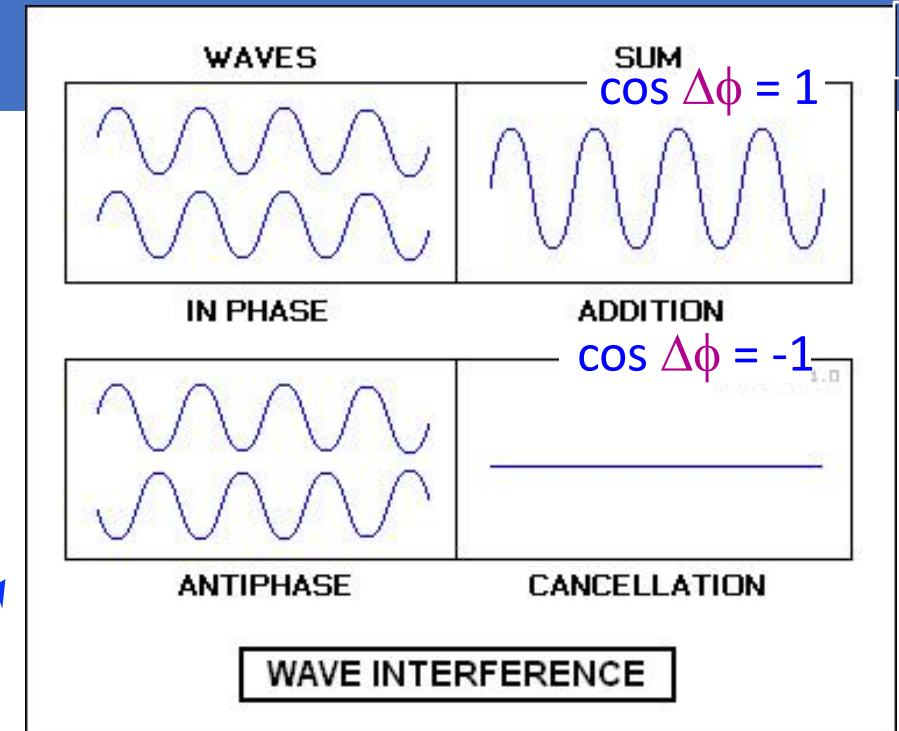


Interfering waves: $\Delta\phi = \phi_1 - \phi_2$

$$I_{12} = |W_1 + W_2|^2 = h_1^2 + h_2^2 + 2h_1h_2 \cos(\Delta\phi)$$

Regions of *constructive* interference: $I_{12} = 2 \times (I_1 + I_2)$

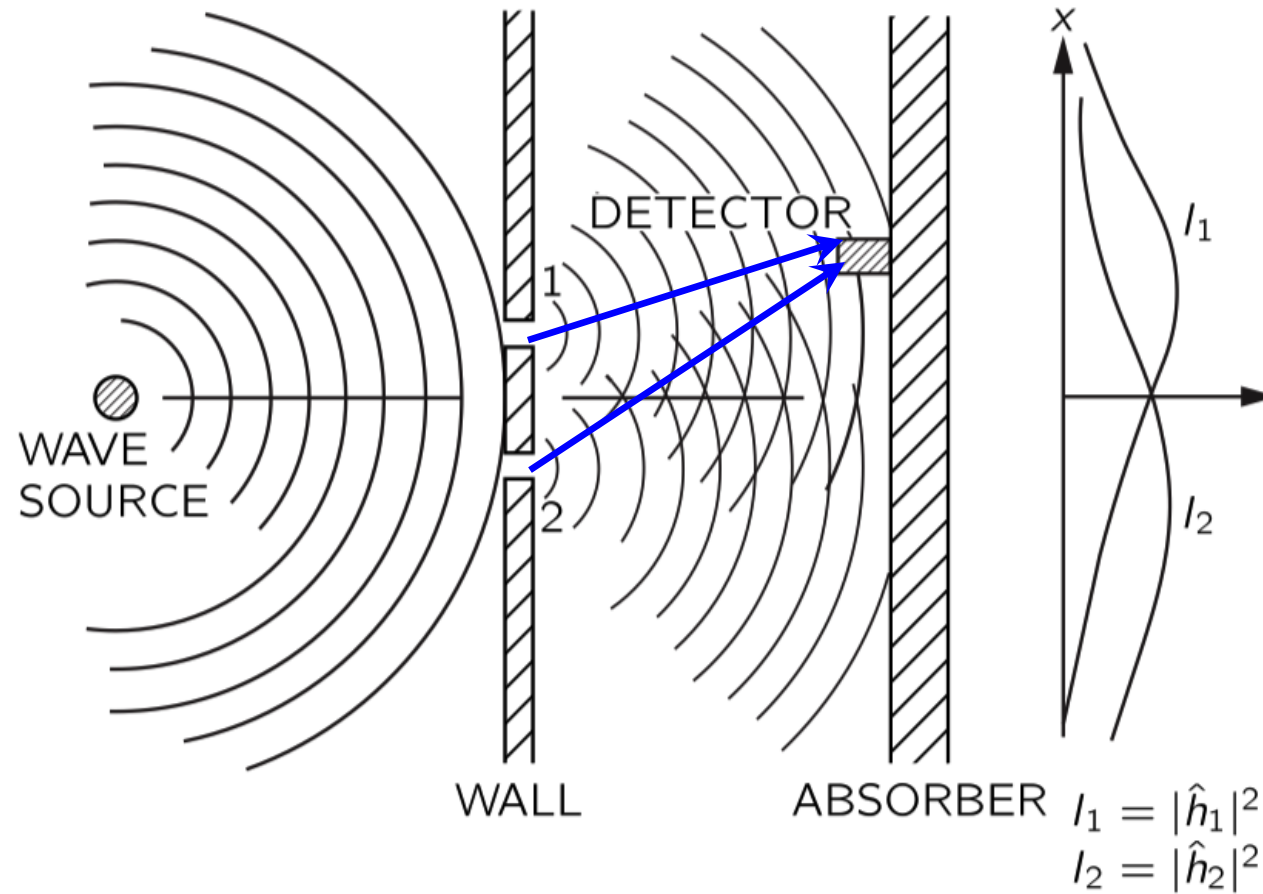
Regions of *destructive* interference: $I_{12} = 0$



Case 2: Experiment with Waves

19

When both slits are open there are two contributions to the wave the oscillation at the detector: $W(t) = W_1(t) + W_2(t)$



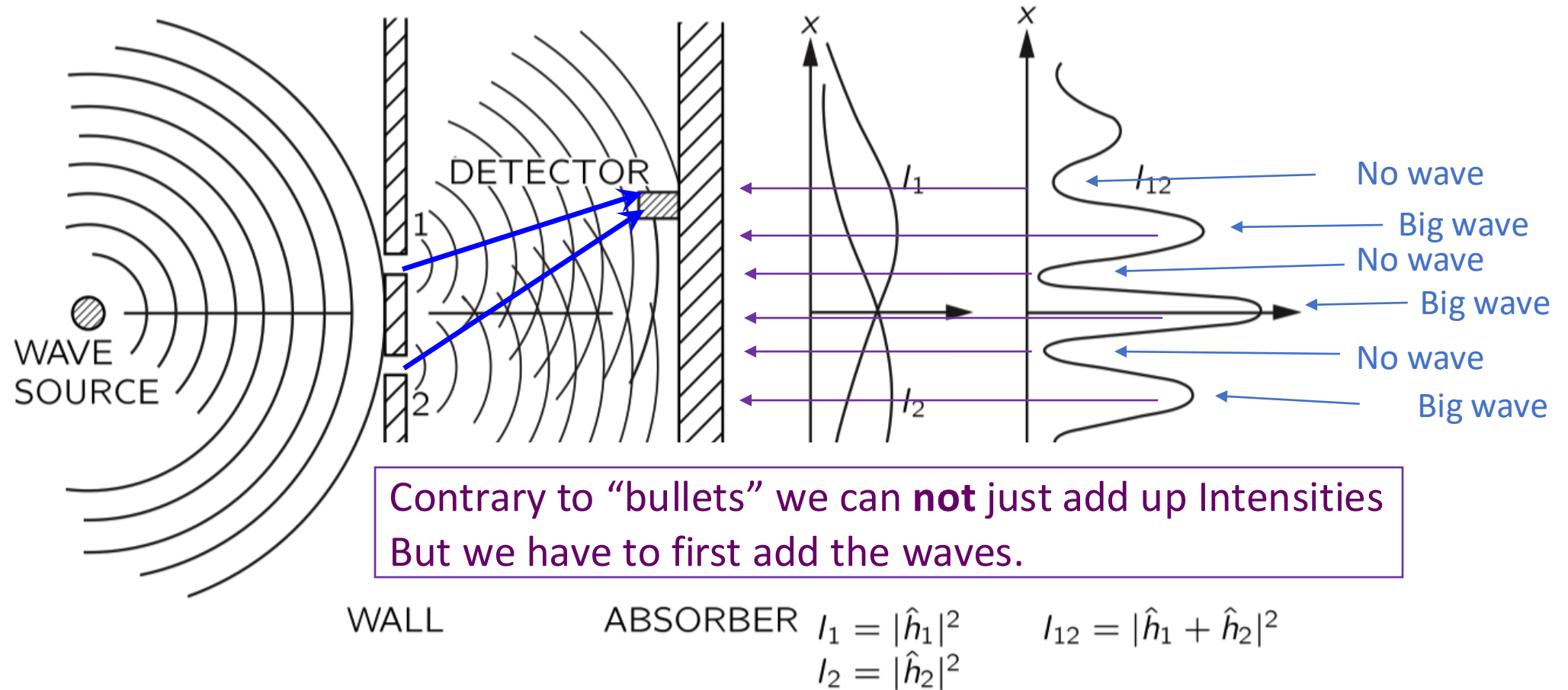
First combine: $W(t) = W_1(t) + W_2(t)$

Afterwards look at the amplitude and intensity of the resulting wave!

Case 2: Experiment with Waves

20

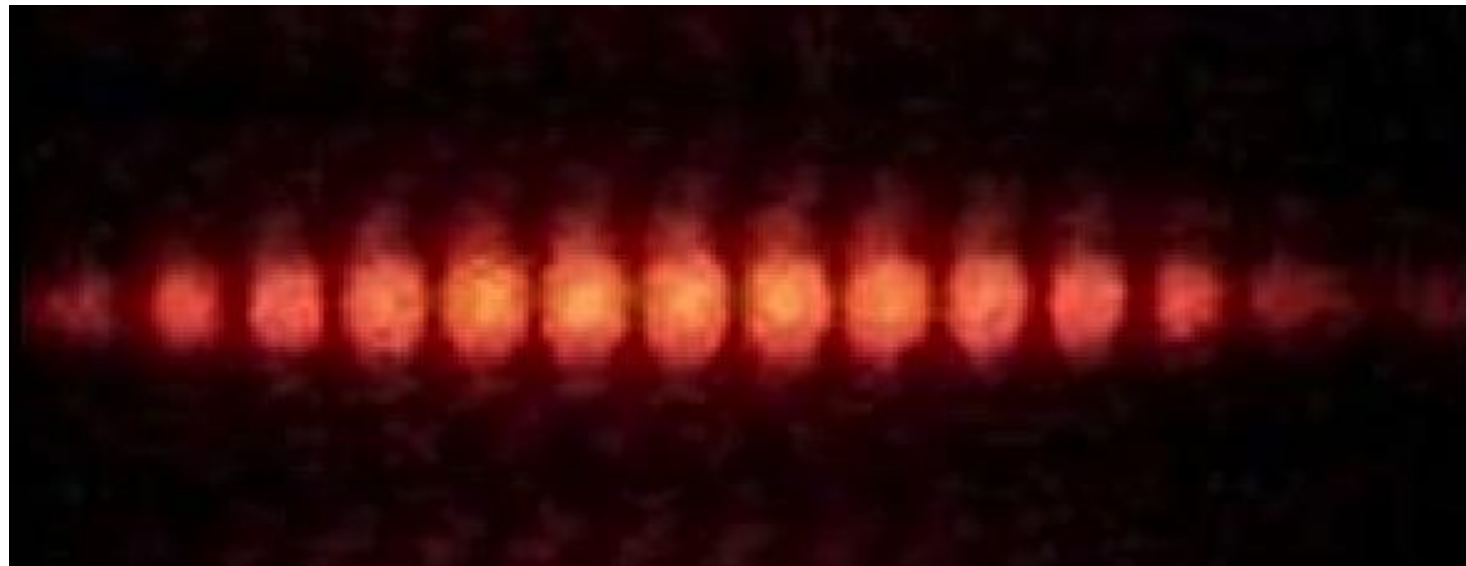
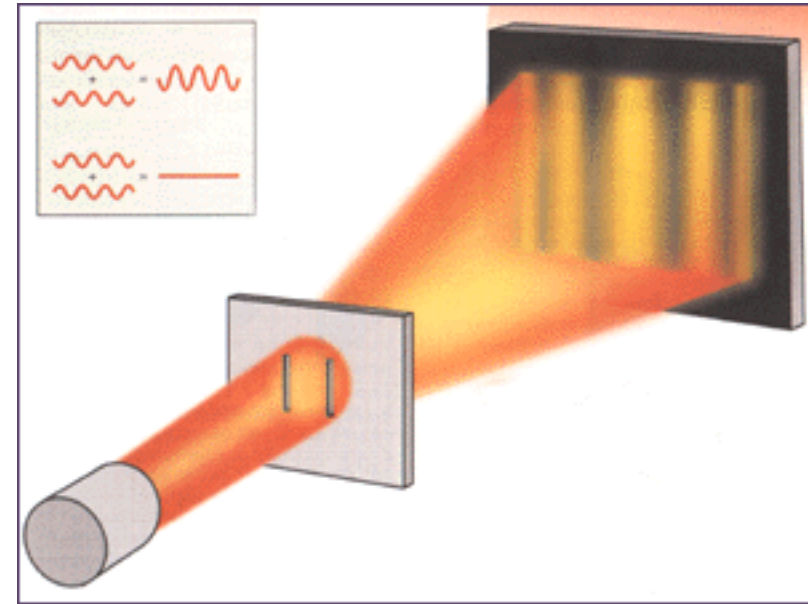
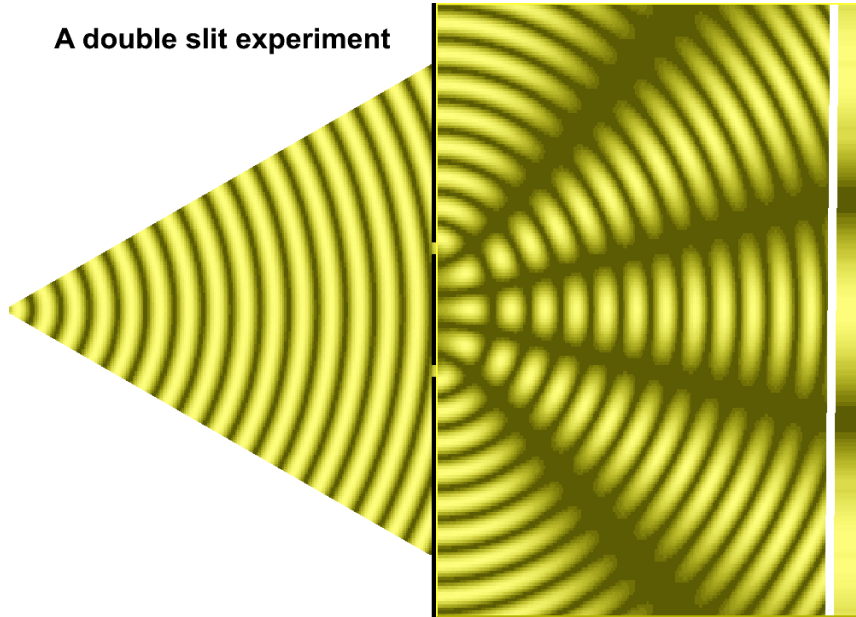
When both slits are open there are two contributions to the wave the oscillation at the detector: $W(t) = W_1(t) + W_2(t)$



Interference pattern: $I_{12} = |W_1 + W_2|^2 = h_1^2 + h_2^2 + 2h_1h_2 \cos(\Delta\phi)$
Regions where waves are *amplified* and regions where waves are *cancelled*.

Double Slit Experiment with Light (Young)

A double slit experiment



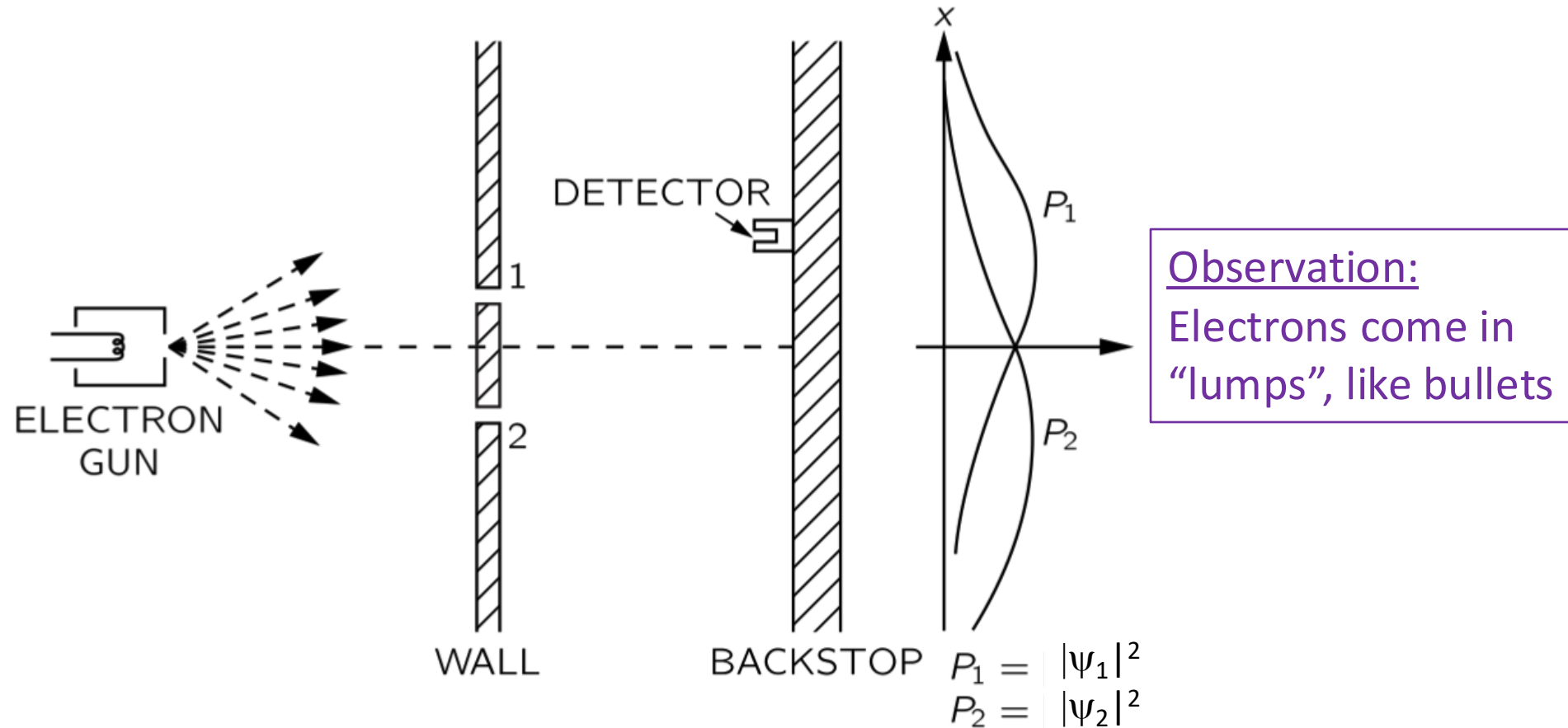
Case 3: An Experiment with Electrons



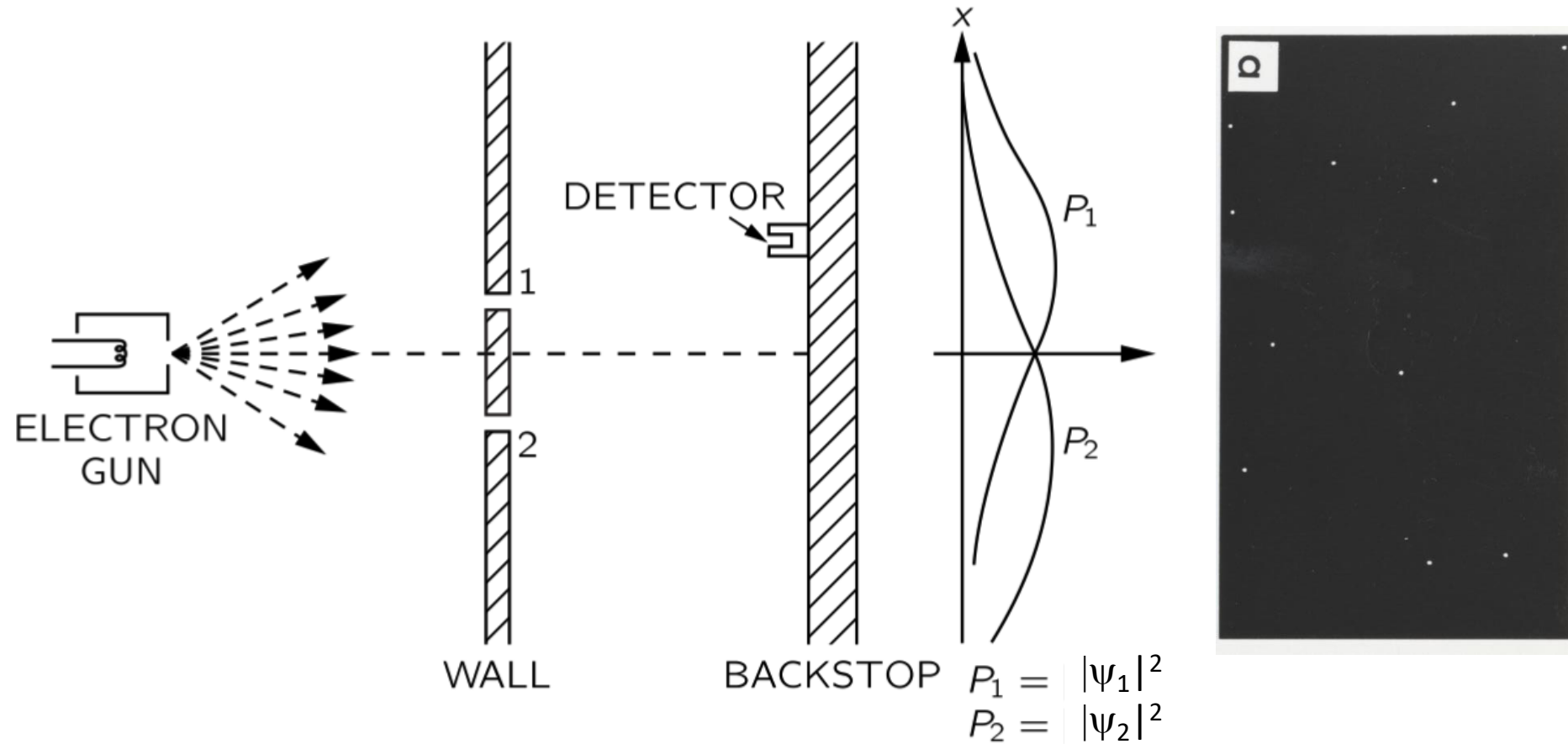
Case 3: Experiment with Electrons

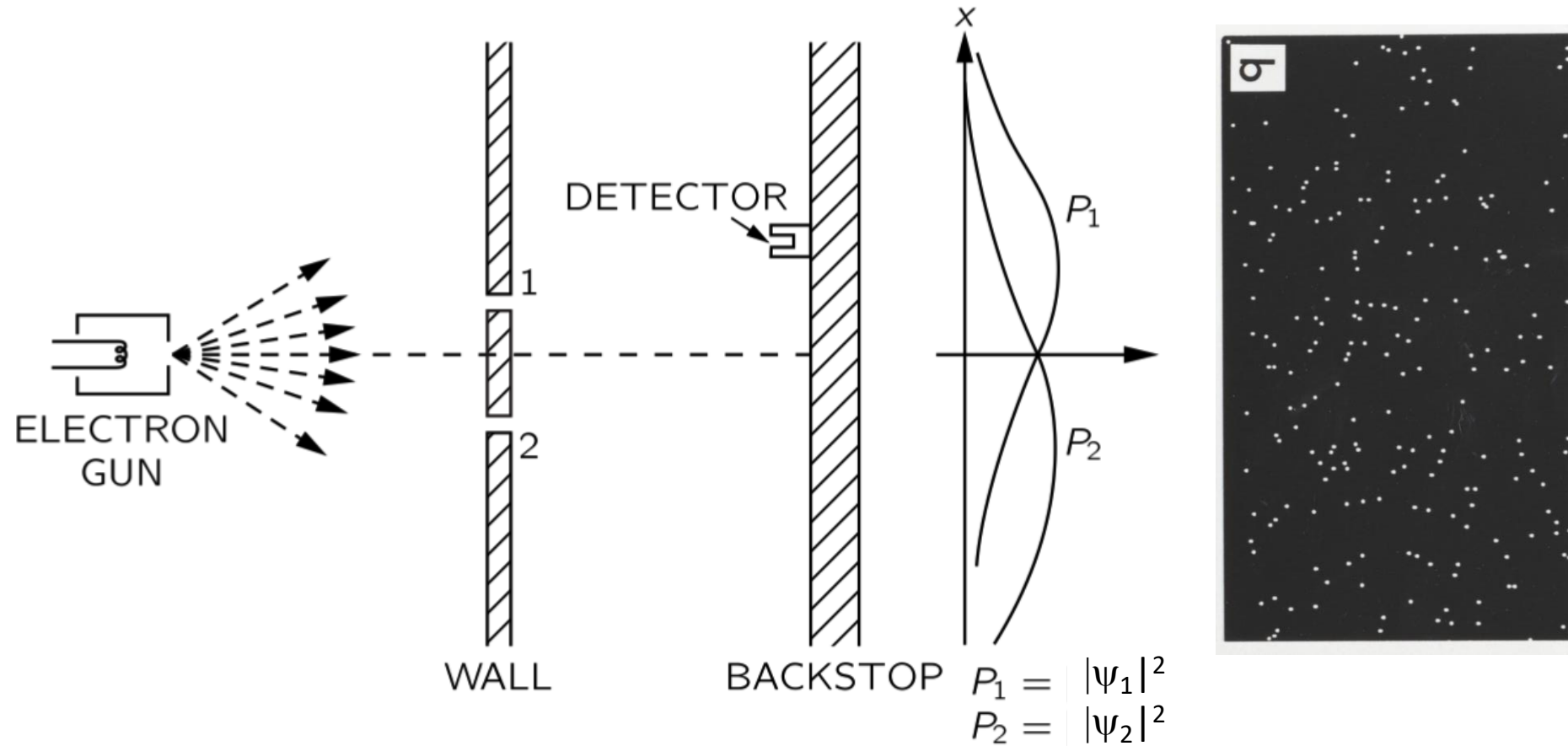
23

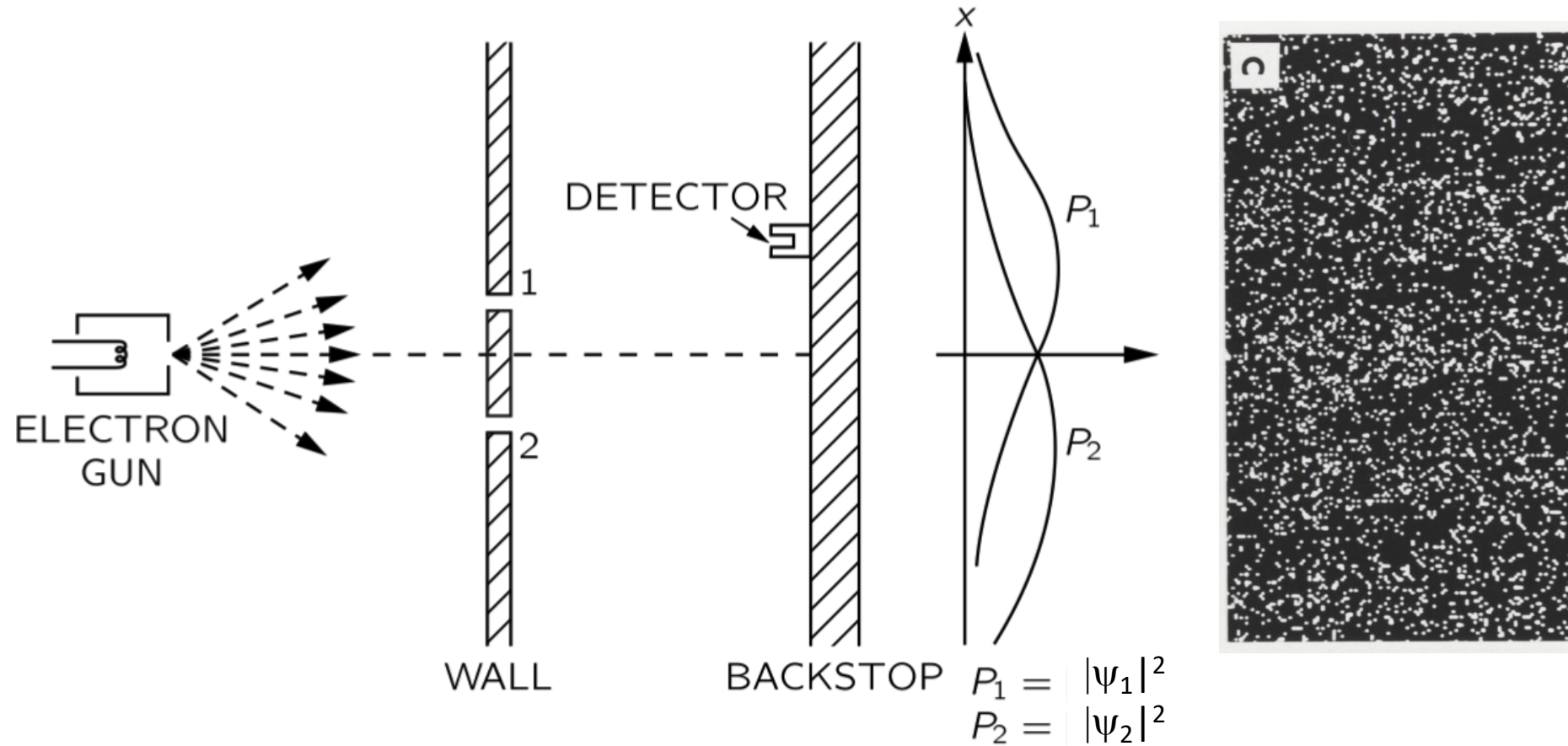
From the detector counts deduce again the probabilities P_1 and P_2

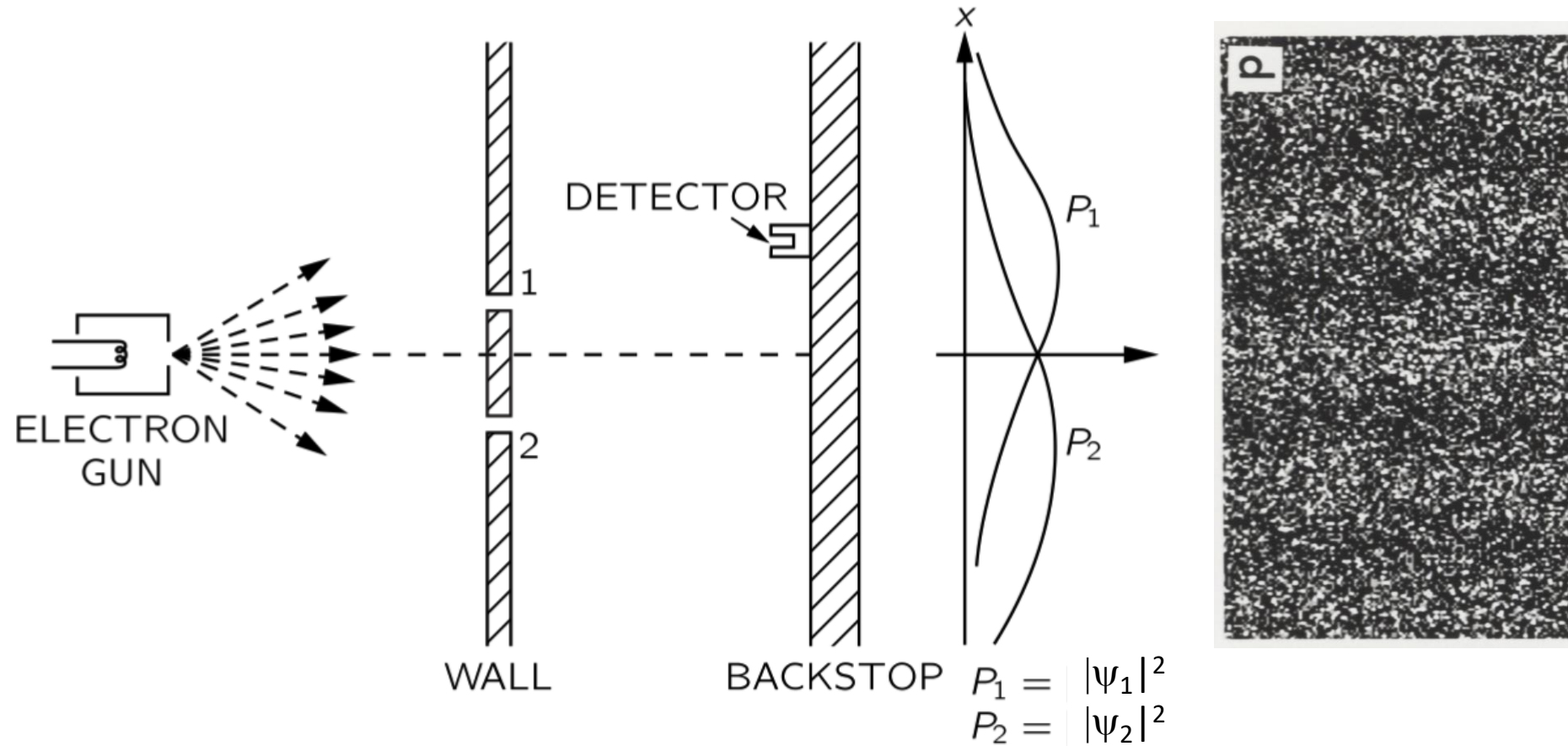


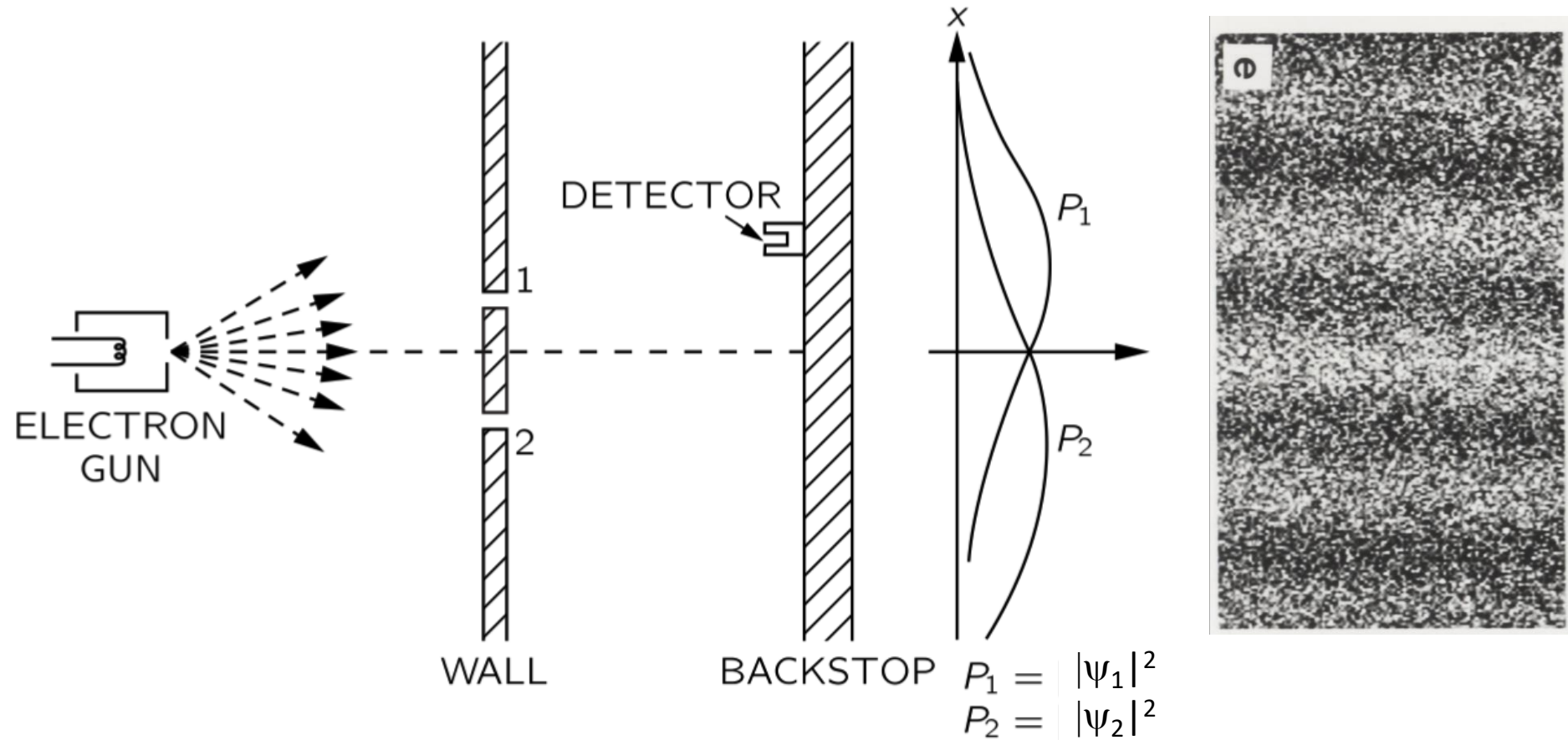
What do we expect when both slits are open?

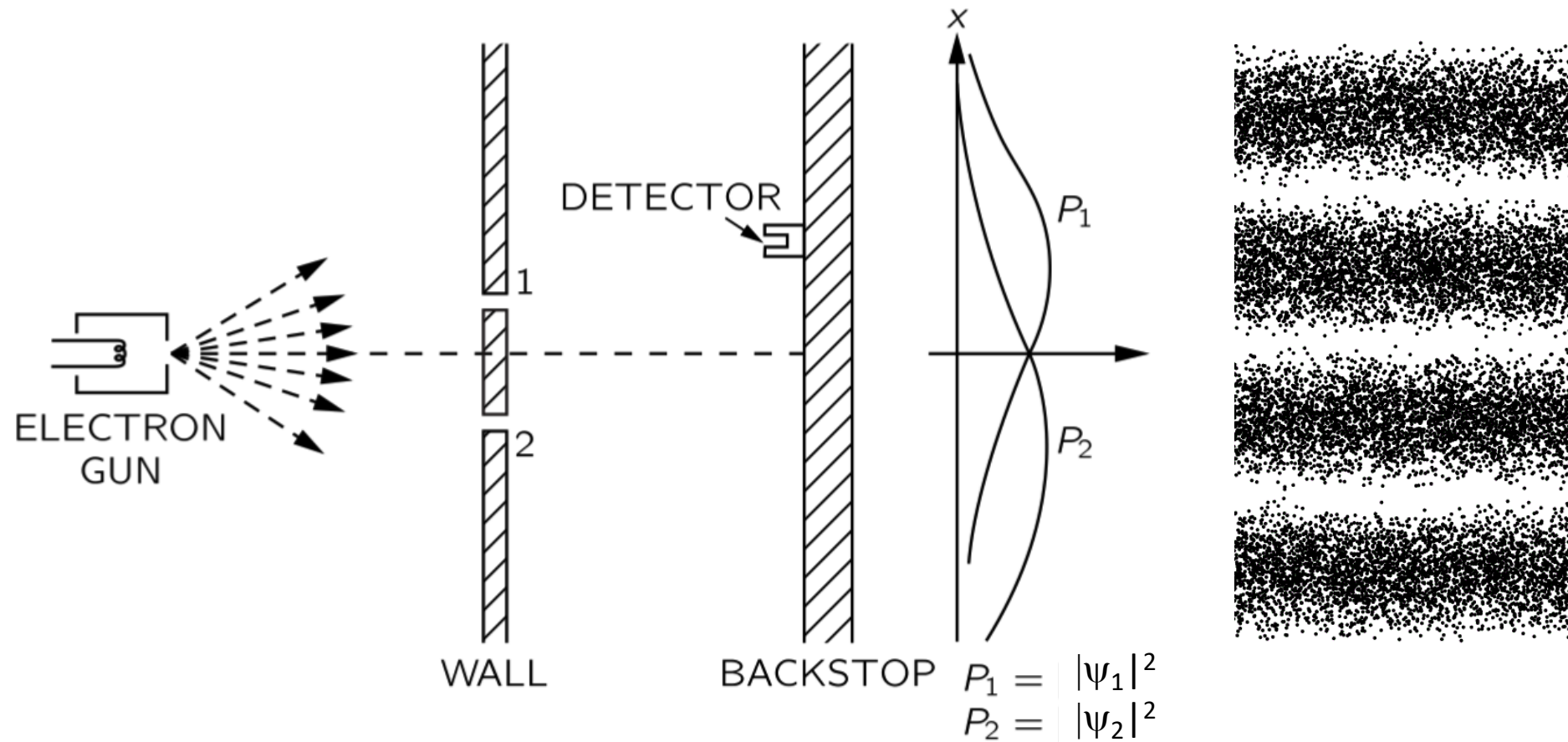










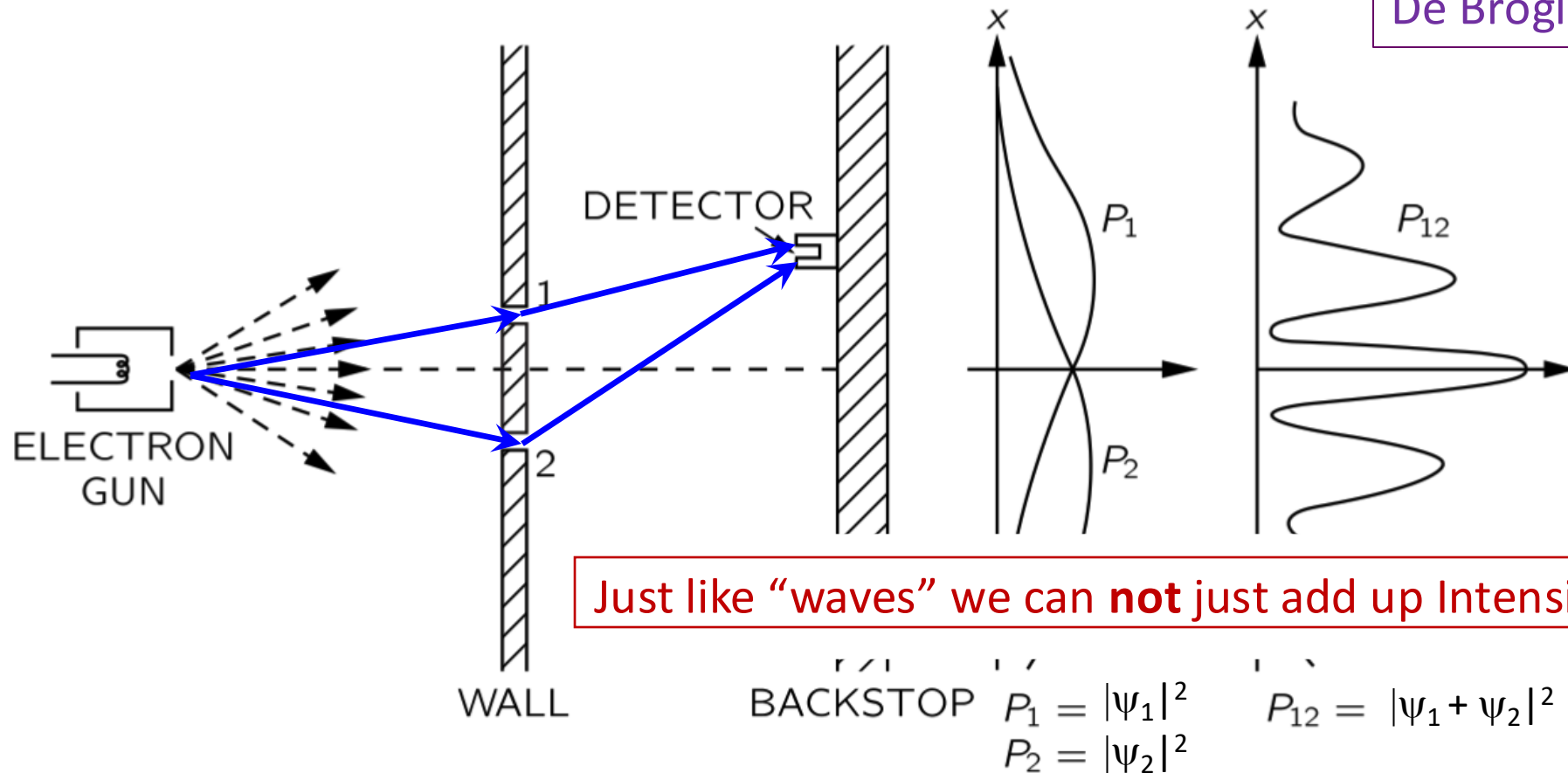


Case 3: Experiment with Electrons

25

An Interference pattern!

The electron wave function behaves exactly like classical waves.



Add the wave amplitudes:

$$\psi_{12} = \psi_1 + \psi_2$$

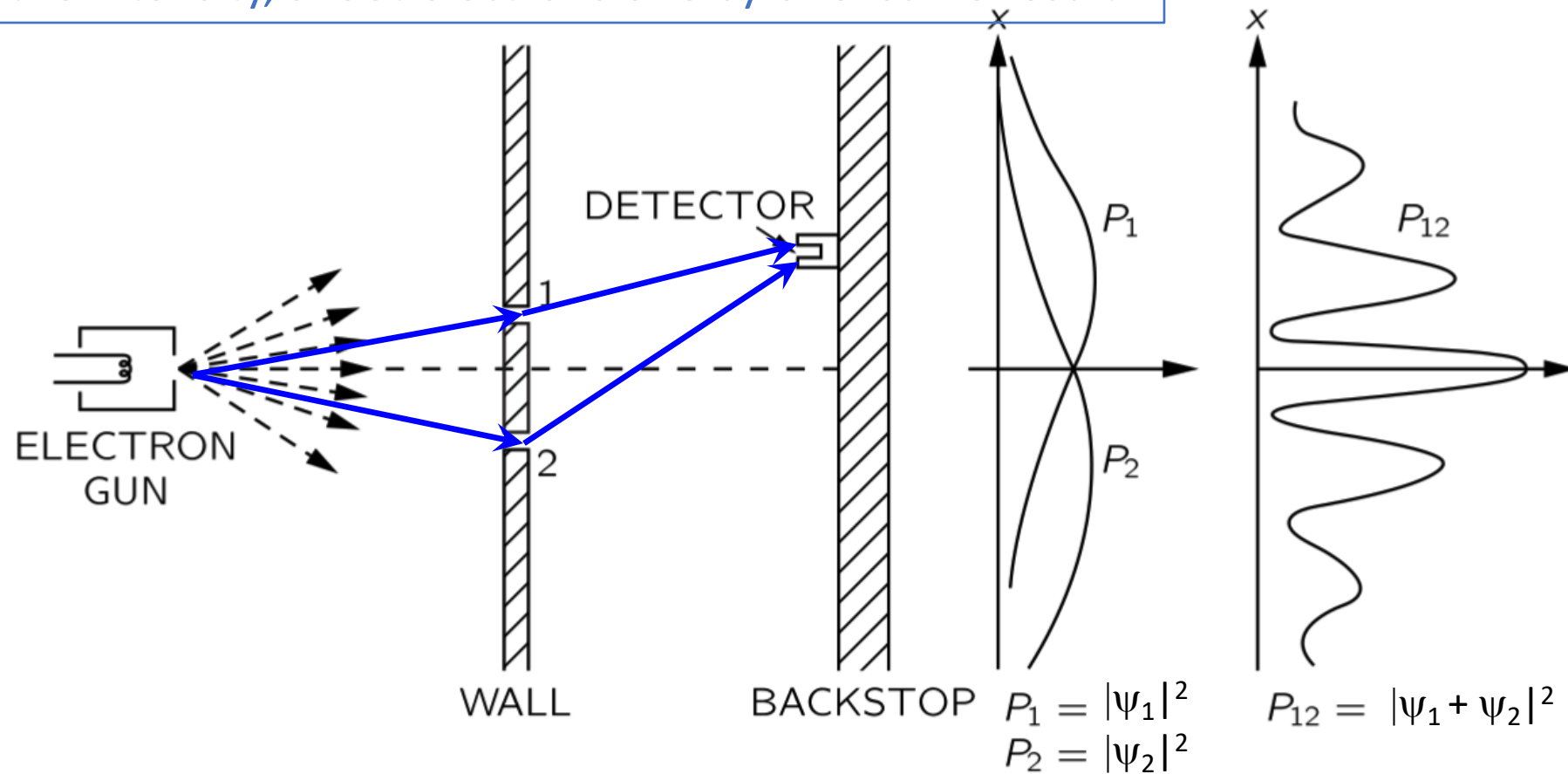
The probability is the square of the sum:

$$P_{12} = |\psi_{12}|^2 = |\psi_1 + \psi_2|^2 = |\psi_1|^2 + |\psi_2|^2 + 2\psi_1\psi_2^*$$

Case 3: Experiment with Electrons

26

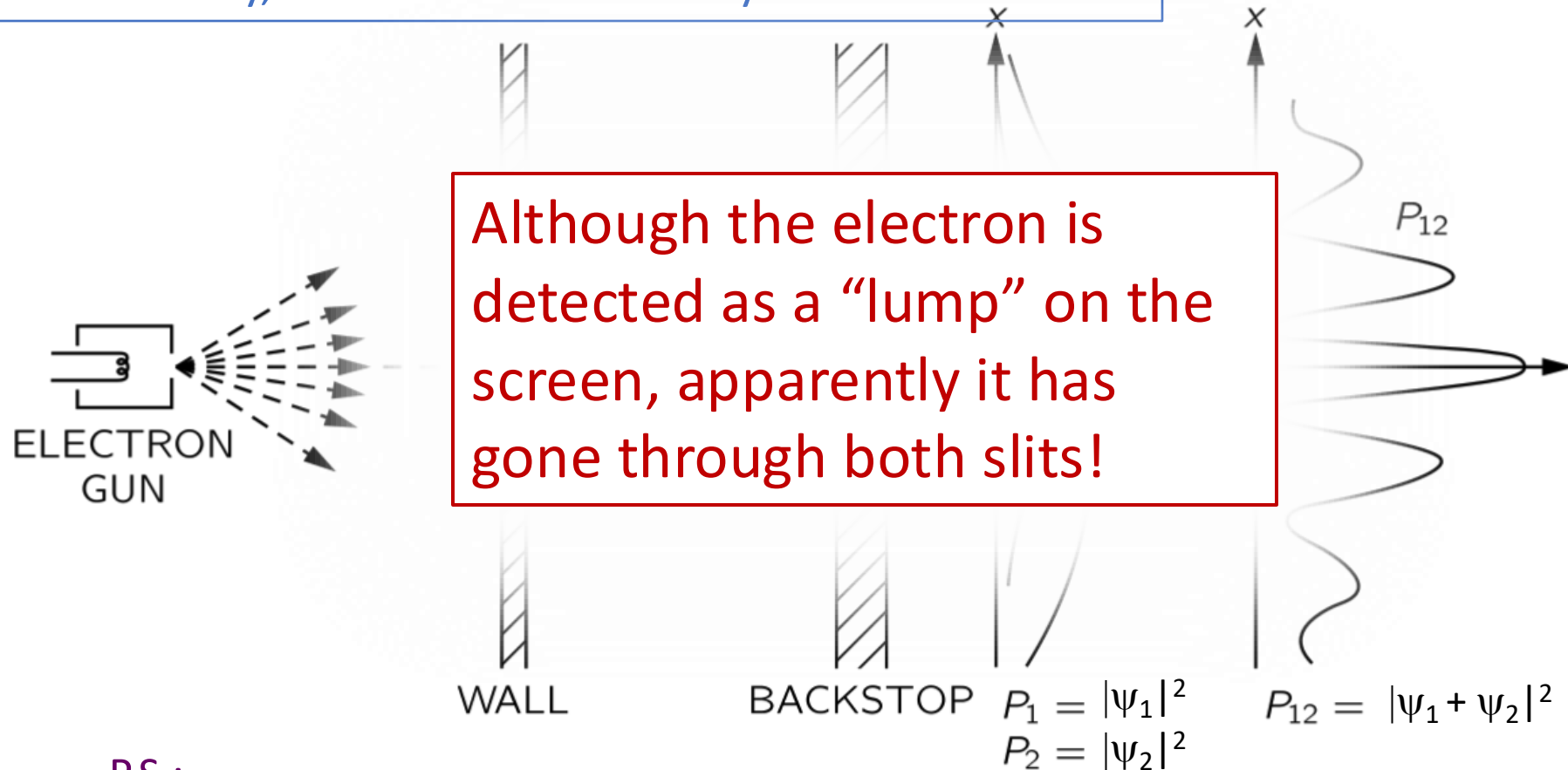
Perhaps the electrons interfere with each other.
Reduce the intensity, shoot electrons one by one: same result.



Case 3: Experiment with Electrons

27

Perhaps the electrons interfere with each other.
Reduce the intensity, shoot electrons one by one: same result.



P.S.:

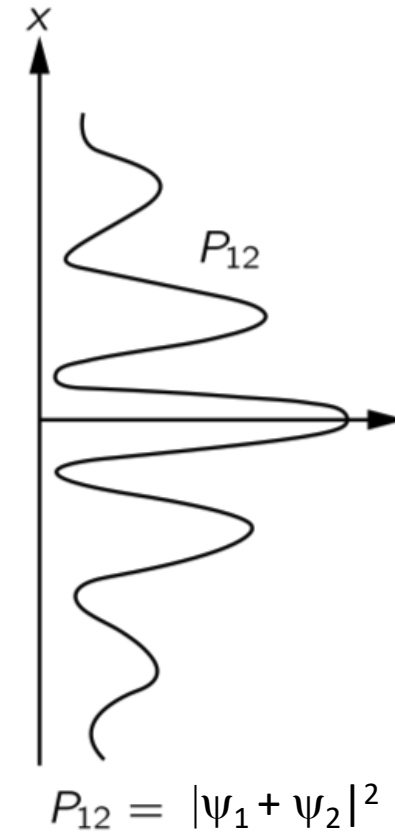
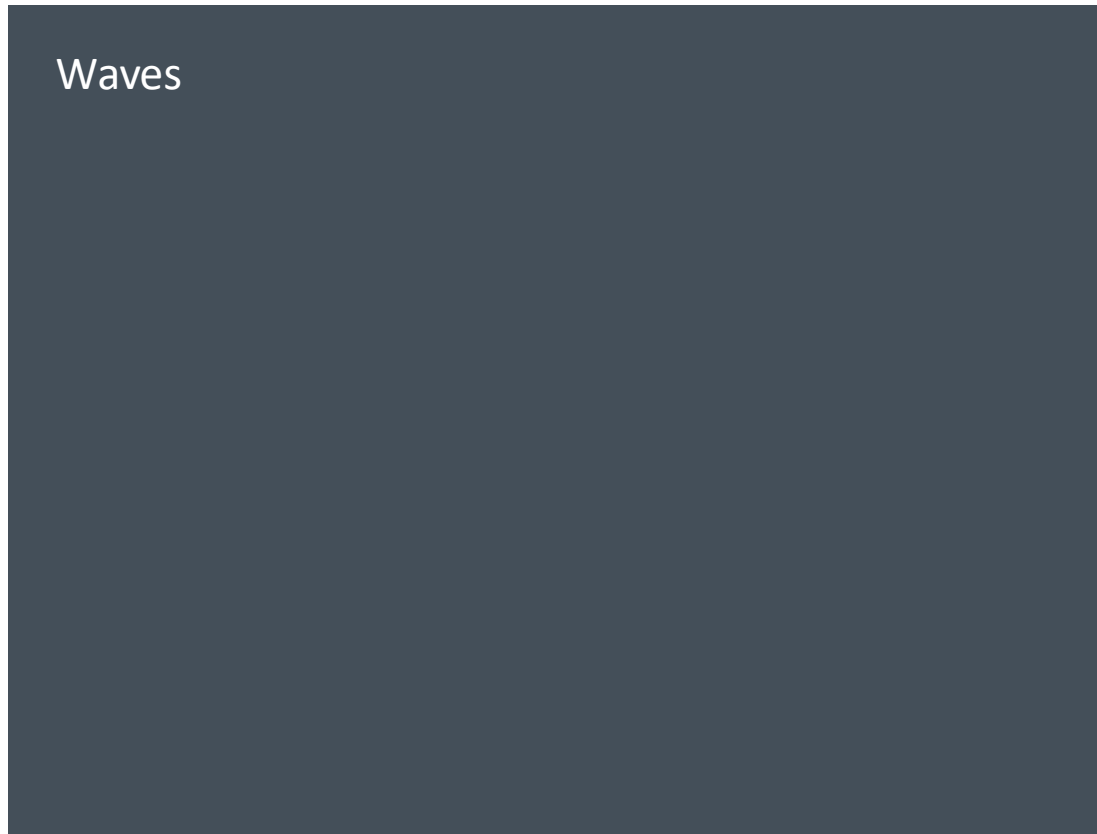
Classically, light behaves light waves. However, if you shoot light, photon per photon, it “comes in lumps”, just like electrons.

Quantum Mechanics: for photons it is the same story as for electrons.

Case 3: Experiment with Electrons

28

Perhaps the electrons interfere with each other.
Reduce the intensity, shoot electrons one by one: same result.



P.S.:

Classically, light behaves light waves. However, if you shoot light, photon per photon, it “comes in lumps”, just like electrons.

Quantum Mechanics: for photons it is the same story as for electrons.

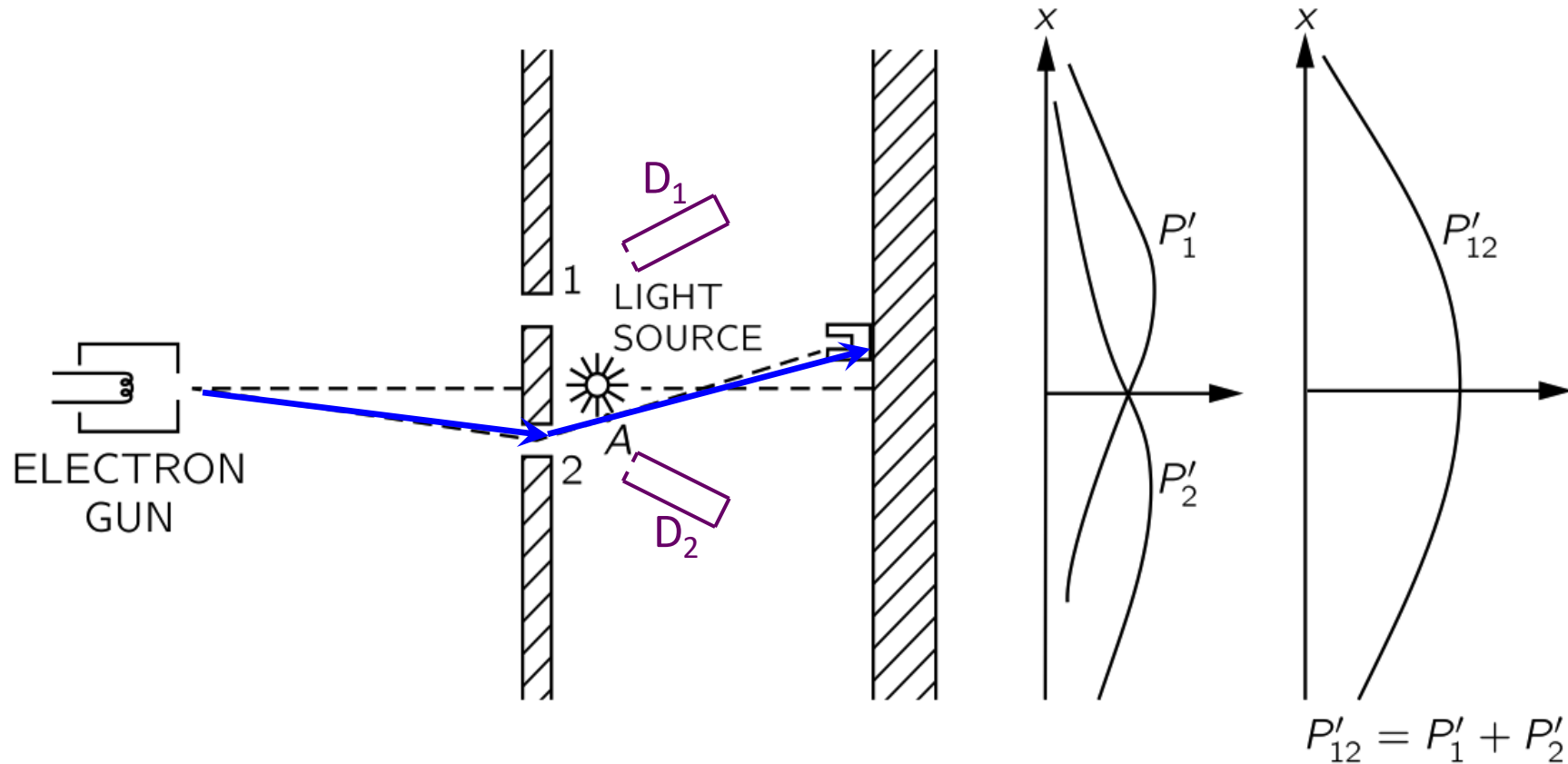
Case 4: A Different Experiment with Electrons



Case 4: Watch the Electrons

30

Let us try to out-smart the electron: just watch through which slit it goes!

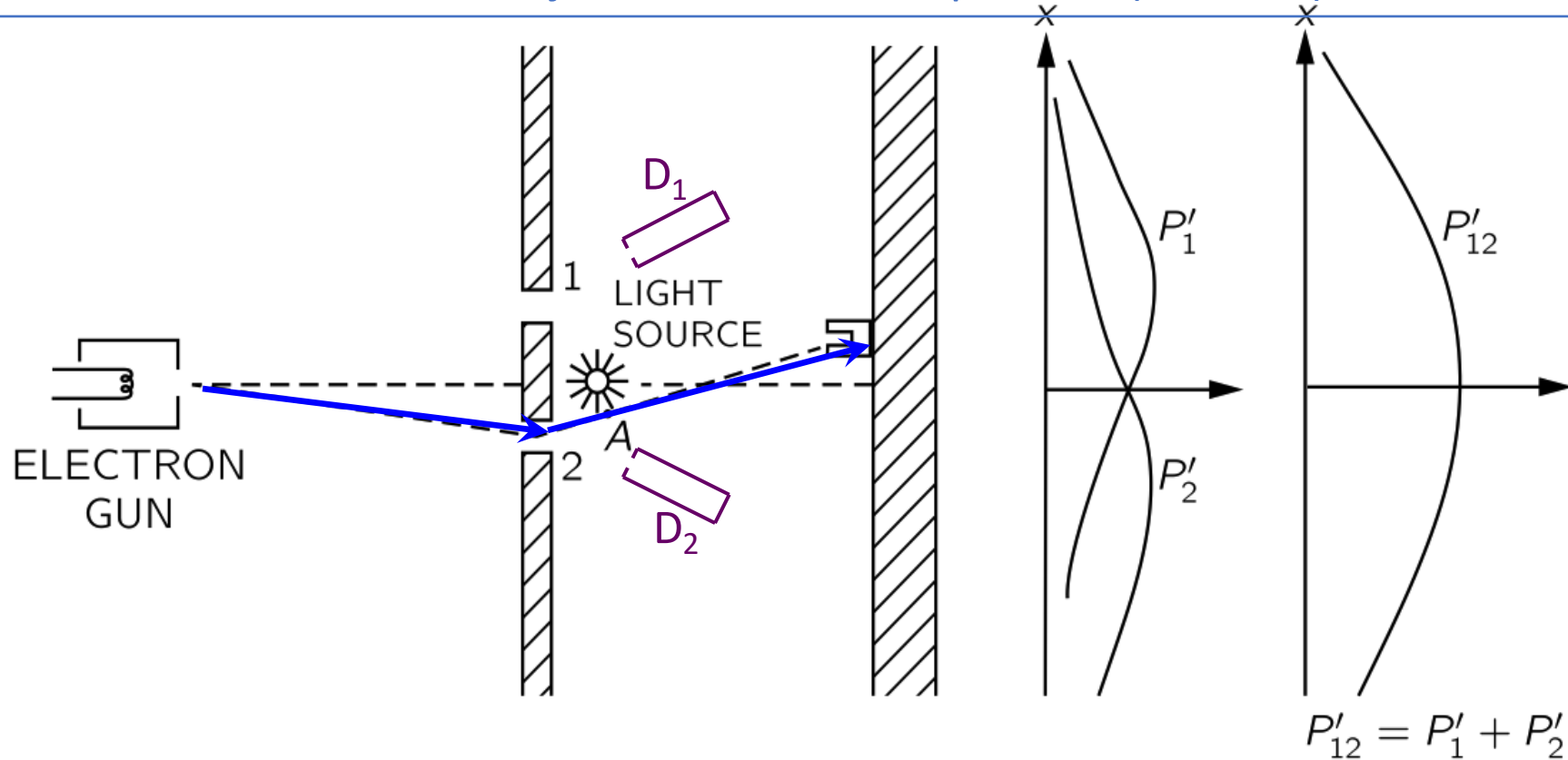


D_1 and D_2 are two “microscopes” looking at the slits 1 and 2, respectively.

Case 4: Watch the Electrons

31

When we watch through which slit the electrons go, we destroy the interference! Now the electron behaves just like a classical particle (“bullet”).

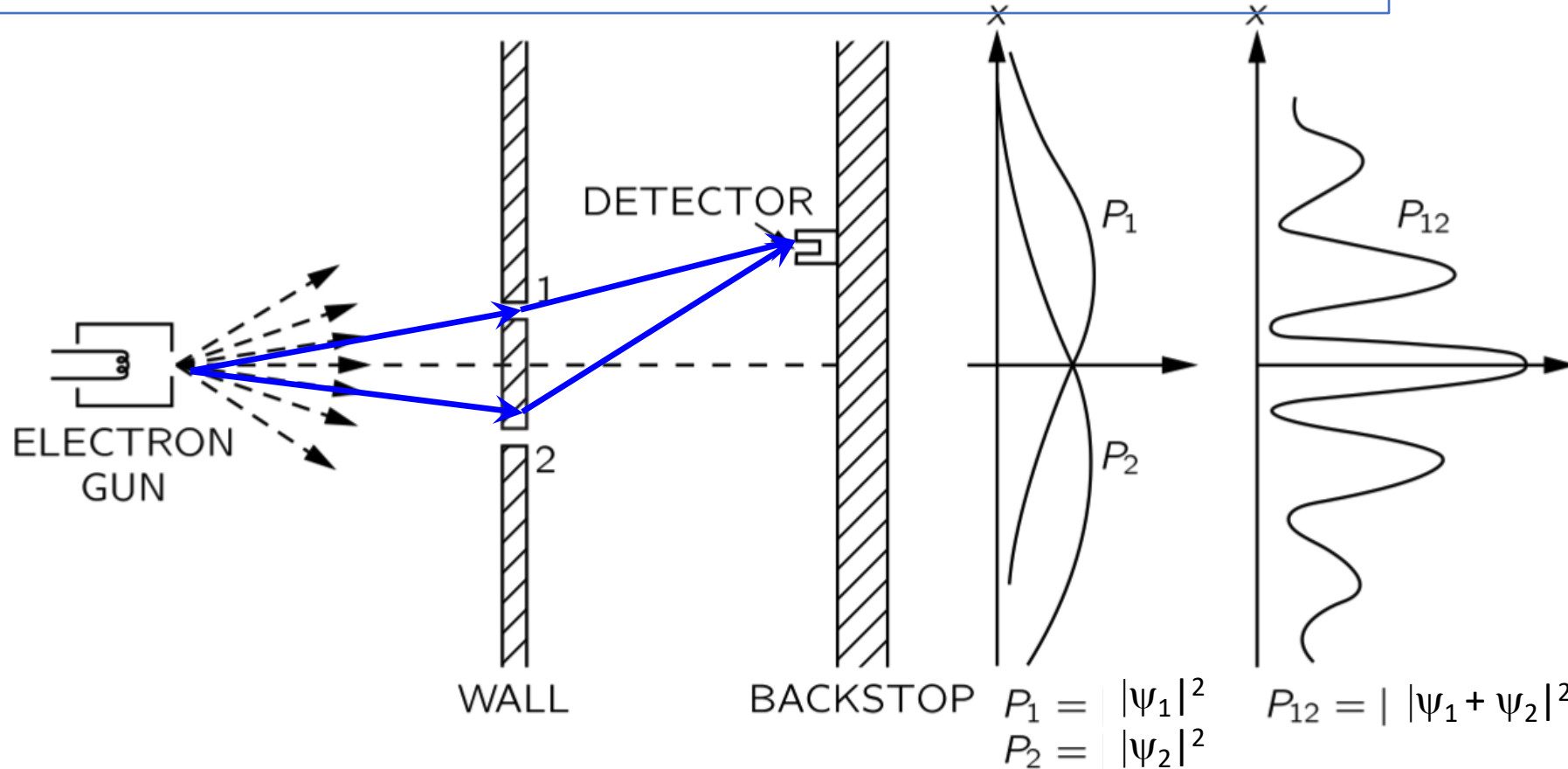


It requires an observation to let the quantum wave function “collapse” into reality. As long as no measurement is made the wave function keeps “all options open”.

Case 3: Don't Watch the Electrons

32

When we don't watch through which slit the electrons go, the electron is an object that interferes with itself!



It requires an observation to let the quantum wave function “collapse” into reality. As long as no measurement is made the wave function keeps “all options open”.

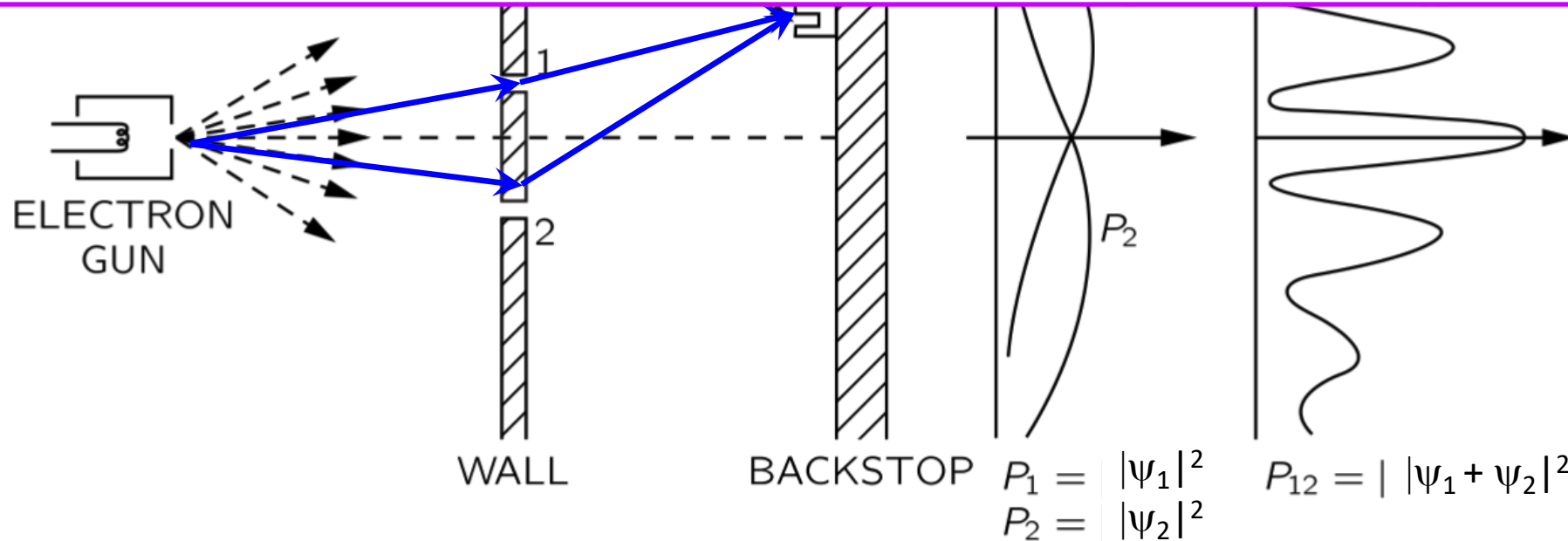
If you watch *half the time*; you only get the interference for the cases you *did not watch*.

Case 3: Don't Watch the Electrons

32

When we don't watch through which slit the electrons go, the electron is an object that interferes with itself!

By the act of watching a quantum object we interfere with the quantum system and force it to bring one of its possible quantum states into reality.



It requires an observation to let the quantum wave function “collapse” into reality. As long as no measurement is made the wave function keeps “all options open”.

If you watch *half the time*; you only get the interference for the cases you *did not watch*.



© 2011 JESSE TAHIRALI

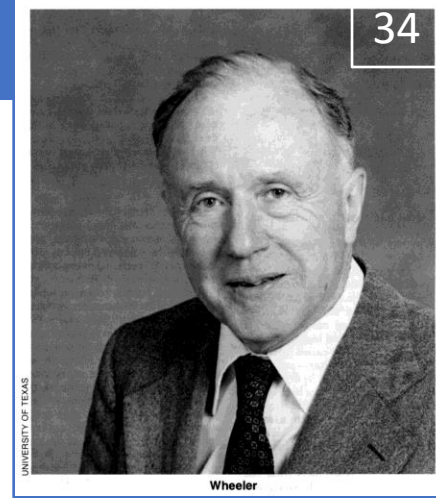
THIS IS EXACTLY HOW WAVE-PARTICLE DUALITY WORKS

GODSOFTHEMOON.COM

Next lecture we will try to out-smart nature one step further...
... and face the consequences.

Next Lecture: Wheeler's Delayed Choice

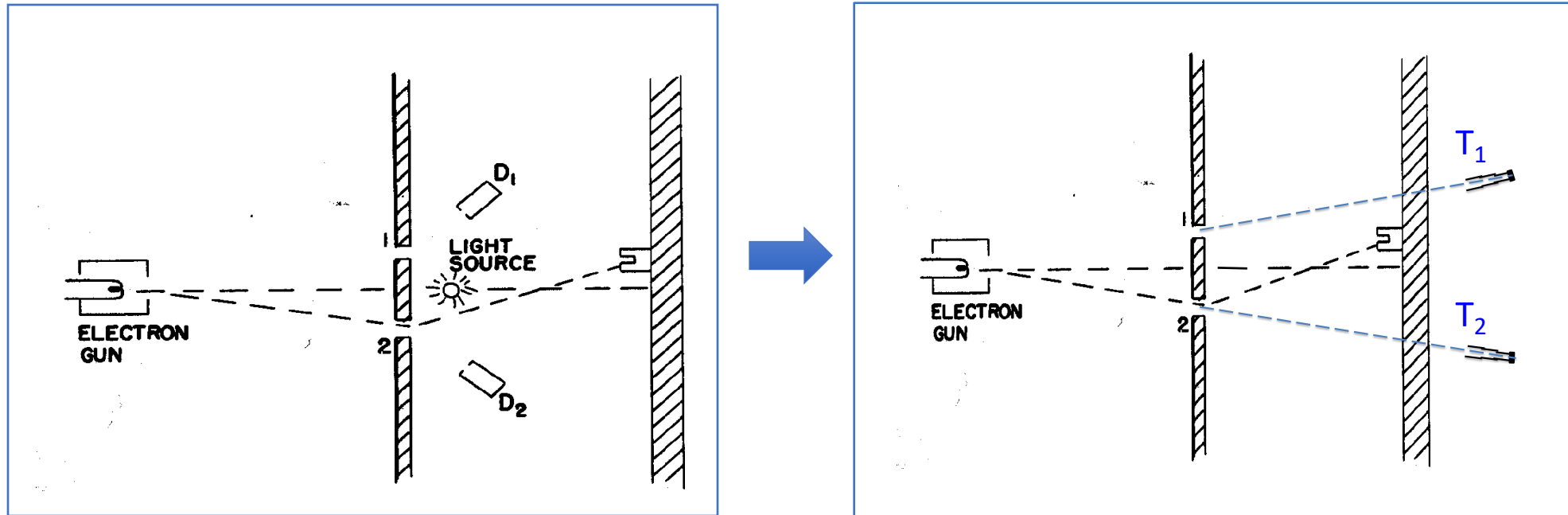
34



John Wheeler (1911 – 2008):
Famous for work on gravitation
(Black holes – quantum gravity)

Replace detectors D_1 and D_2 with telescopes T_1 and T_2 which are focused on slits 1 and 2

What happens if we *afterwards would reconstruct* whether the electron went through slit 1 or slit 2?



Try to out-smart nature one step further... and face the consequences: Schrödinger's cat.

