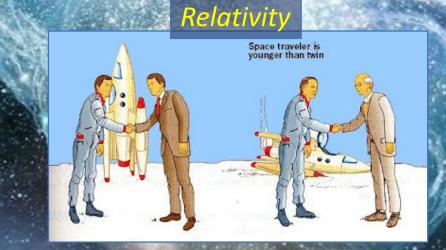
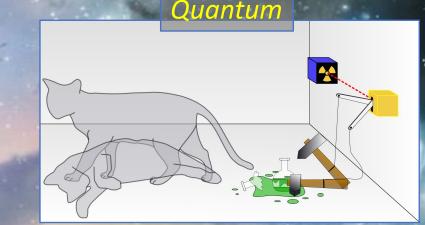
The Relativistic Quantum World

A lecture series on Relativity Theory and Quantum Mechanics





Marcel Merk Studium Generale Maastricht Nov 1 – Nov 29, 2023

The Relativistic Quantum World

Nov. 1:	Lecture 1: The Principle of Relativity and the Speed of Light Lecture 2: Time Dilation and Lorentz Contraction
Nov. 8:	Lecture 3: The Lorentz Transformation and Paradoxes Lecture 4: General Relativity and Gravitational Waves
Nov. 15:	Lecture 5: The Early Quantum Theory Lecture 6: Feynman's Double Slit Experiment
Nov 22:	Lecture 7: Wheeler's Delayed Choice and Schrodinger's Cat Lecture 8: Quantum Reality and the EPR Paradox
Nov. 29:	Lecture 9: The Standard Model and Antimatter Lecture 10: Why is there something rather than nothing?
	Nov. 8: Nov. 15: Nov 22:

Lecture notes, written for this course, are available: <u>www.nikhef.nl/~i93/Teaching/</u> Prerequisite for the course: High school level physics & mathematics.

Lecture 8

Quantum Reality and EPR Paradox

"Philosophy is too important to leave to the philosophers." - John Archibald Wheeler

"When we measure something we are forcing an undetermined, undefined world to assume an experimental value. We are not measuring the world, we are creating it."

- Niels Bohr

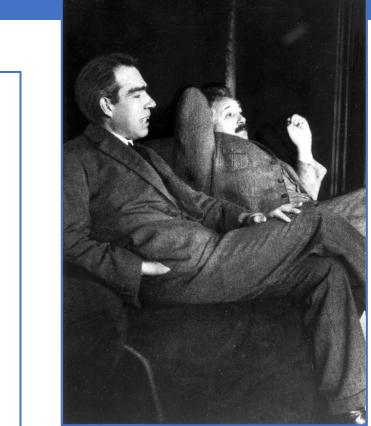
"If all of this is true, it means the end of physics."

- Albert Einstein, in discussion with Niels Bohr

Einstein's Final Objection

Principle of locality:

- An object is only directly influenced by its immediate surroundings.
- An action on a system at one point *cannot* have an *instantaneous* effect on another point.
- To have effect at a distance a field or particle ("signal") must travel between the two points.
- Limit: the speed of light.
 - Otherwise trouble with causality (see relativity: "Bob dies before Alice actually shoots him?!").

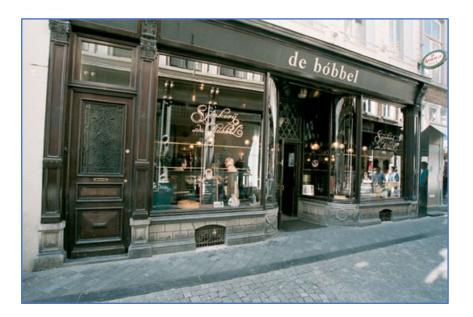


Einstein: Quantum mechanics is *not a local* theory, therefore: it is unreasonable!

The EPR discussion is the last of the Bohr – Einstein discussions. After receiving Bohr's reply Einstein commented that QM is too much in contradiction with his scientific instinct.

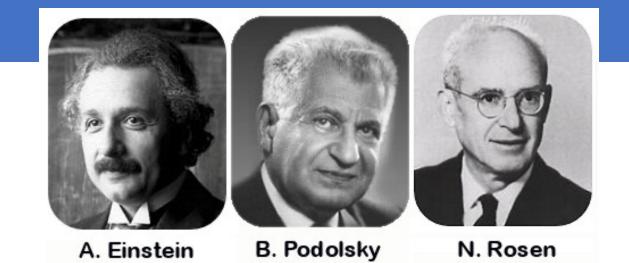
The EPR Paradox





The EPR Paradox (1935)

EPR = Albert Einstein, Boris Podolsky, Nathan Rosen



Bohr et al.: Quantum Mechanics:

The wave function can be precisely calculated, but a measurement of *mutually exclusive quantities* is driven by pure chance.

Einstein et al.: Local Reality:

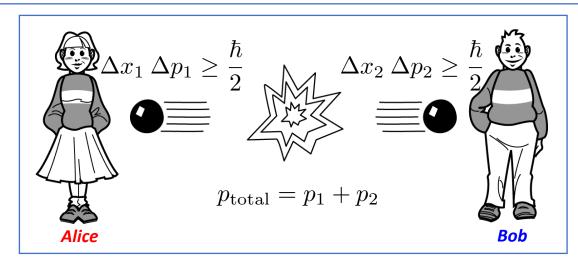
There must exist *hidden variables* (hidden to us) in which the outcome of the measurement is encoded such that effectively *it only looks as* if it is driven by chance.

Local Realism vs Quantum Entanglement:

EPR: What if the wave function is very large and a measurement at one end can influence the other end via some "*unreasonable spooky interaction*". Propose a measurement to test *quantum entanglement* of particles.

The EPR Paradox – the idea

Two particles produced with known total momentum P_{total} , and fly far away. Alice *can not* measure at the same time position (x_1) and momentum (p_1) of particle 1. Bob *can not* measure at the same time position (x_2) and momentum (p_2) of particle 2.



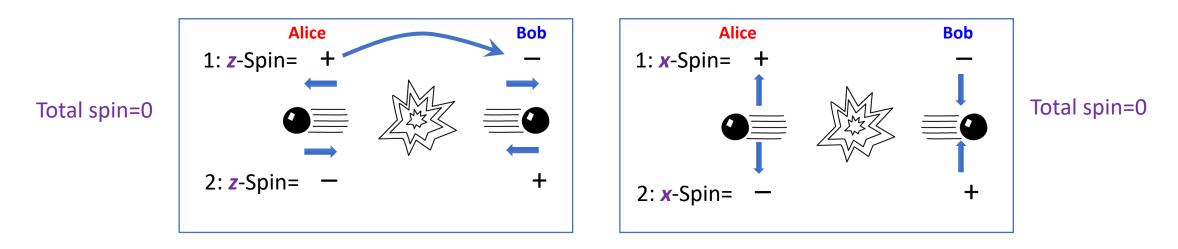
But:

If *Alice* measures p_1 , then automatically p_2 is *known*, since $p_1+p_2=p_{total}$ If *Alice* measures x_1 , then p_1 is unknown and therefore also p_2 is *unknown*.

How can a decision of Alice to measure x_1 or p_1 affect the quantum state of Bob's particle (x_2 or p_2) at the same time over a long distance? Communication with speed faster than the speed of light? Contradiction with causality? Is there "local realism" or "spooky action at a distance"?

An EPR Experiment

Produce two particles with an opposite *spin quantum state*. Heisenberg uncertainty: an electron *cannot* have well defined *spin* at same time along two different directions, eg. **z** and **x** spin is quantized and can only have values " + " or " - " charge



Quantum:

After first measuring *z*, then the probability of +x vs -x = 50%-50%. After subsequently measuring eg. +x, the probability of +z vs -z = 50%-50% etc.!

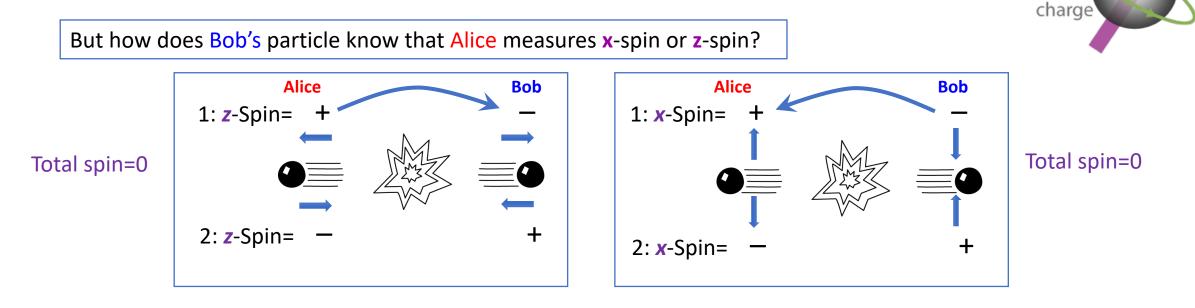
Quantum wave function: total spin = 0. If Alice measures spin of her particle along the z-direction, Then also Bob's particle's spin points (oppositely) along the z-direction! 7

spin

e

An EPR Experiment

Produce two particles with an opposite *spin quantum state*. Heisenberg uncertainty: an electron *cannot* have well defined *spin* at same time along two different directions, eg. *z* and *x*

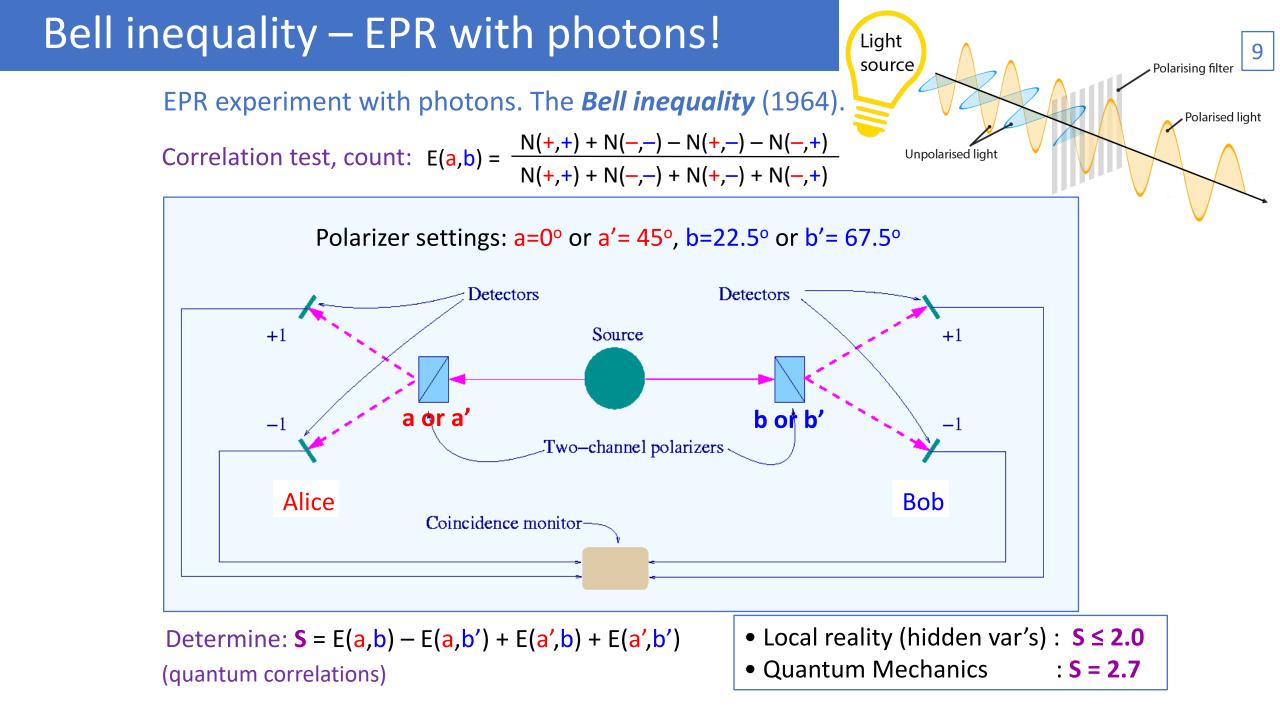


e

spin

Trick: if A_z^+ implies B_z^- , then alternatively: B_x^- implies A_x^+ Does the measurement $A_z^+B_x^-$ means that we have determined **both** x and z spin according to $A_z^+A_x^+$?! (Note that A and B could have lightyears distance!) \rightarrow Local realism: **yes!** \rightarrow QM: **No!** (The first measurement "collapses" the wave function: coherence is lost.)

Either the particles are linked because of some *hidden variable* (local reality) *or* they are QM *"entangled"* until a measurement "collapses" the wave function.



 $E(a,b)=\int {{\underline A}(a,\lambda) {\underline B}(b,\lambda)
ho(\lambda) d\lambda}$

where <u>A</u> and <u>B</u> are the average values of the outcomes. Since the possible values of A and B are -1, 0 and +1, it follows that:

$$|\underline{A}| \leq 1 \quad |\underline{B}| \leq 1$$

Then, if a, a', b and b' are alternative settings for the detectors,

$$egin{aligned} E(a,b)-E(a,b')&=\int\left[\underline{A}(a,\lambda)\underline{B}(b,\lambda)-\underline{A}(a,\lambda)\underline{B}(b',\lambda)
ight]
ho(\lambda)d\lambda\ &=\int\underline{A}(a,\lambda)\underline{B}(b,\lambda)\left[1\pm\underline{A}(a',\lambda)\underline{B}(b',\lambda)
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ho(\lambda)d\lambda\ -\int\underline{A}(a,\lambda)\underline{B}(b',\lambda)\left[1\pm\underline{A}(a',\lambda)\underline{B}(b,\lambda)
ight]
ho(\lambda)d\lambda \end{aligned}$$

Taking absolute values of both sides, and applying the triangle inequality to the right-hand side, we obtain

$$|E(a,b) - E(a,b')| \leq \left|\int \underline{A}(a,\lambda)\underline{B}(b,\lambda)\left[1 \pm \underline{A}(a',\lambda)\underline{B}(b',\lambda)\right]\rho(\lambda)d\lambda\right| + \left|\int \underline{A}(a,\lambda)\underline{B}(b',\lambda)\left[1 \pm \underline{A}(a',\lambda)\underline{B}(b,\lambda)\right]\rho(\lambda)d\lambda\right|$$

We use the fact that $[1 \pm \underline{A}(a', \lambda)\underline{B}(b', \lambda)] \rho(\lambda)$ and $[1 \pm \underline{A}(a', \lambda)\underline{B}(b, \lambda)] \rho(\lambda)$ are both non-negative to rewrite the right-hand side of this as

$$\sum_{i} |\underline{A}(a,\lambda)\underline{B}(b,\lambda)| \left| [1 \pm \underline{A}(a',\lambda)\underline{B}(b',\lambda)] \,
ho(\lambda) d\lambda
ight| + \int |\underline{A}(a,\lambda)\underline{B}(b',\lambda)| \left| [1 \pm \underline{A}(a',\lambda)\underline{B}(b,\lambda)] \,
ho(\lambda) d\lambda
ight|$$

By (4), this must be less than or equal to

$$\int \left[1\pm \underline{A}(a',\lambda) \underline{B}(b',\lambda)
ight]
ho(\lambda) d\lambda + \int \left[1\pm \underline{A}(a',\lambda) \underline{B}(b,\lambda)
ight]
ho(\lambda) d\lambda$$

which, using the fact that the integral of $\rho(\lambda)$ is 1, is equal to

$$2\pm\left[\int \underline{A}(a',\lambda)\underline{B}(b',\lambda)
ho(\lambda)d\lambda+\int \underline{A}(a',\lambda)\underline{B}(b,\lambda)
ho(\lambda)d\lambda
ight]$$

which is equal to $\ 2\pm \left[E(a',b')+E(a',b)
ight]$.

Putting this together with the left-hand side, we have:

 $|E(a,b)-E(a,b')| \ \leq 2 \ \pm [E(a',b')+E(a',b)]$

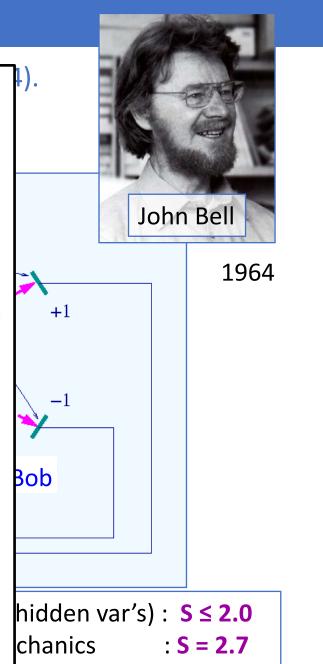
which means that the left-hand side is less than or equal to both 2 + [E(a',b') + E(a',b)] and 2 - [E(a',b') + E(a',b)]. That is:

$$|E(a,b)-E(a,b')| \ \leq \ 2-|E(a',b')+E(a',b)|$$

from which we obtain

 $2 \ \geq \ |E(a,b)-E(a,b')|+|E(a',b')+E(a',b)| \ \geq \ |E(a,b)-E(a,b')+E(a',b')+E(a',b)|$

(by the triangle inequality again), which is the CHSH inequality.



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(by the triangle inequality again), which is the CHSH inequality.

hyse that:

$$a', \lambda)\underline{B}(b, \lambda)]\rho(\lambda)d\lambda$$

 $(a', \lambda)\underline{B}(b, \lambda)]\rho(\lambda)d\lambda$
the the right-hand side of this as
 $d\lambda|$
 $E(a', b)] \cdot That is:$
• Local reality (hidden var's) : $S \le 2.0$
• Quantum Mechanics : $S = 2.7$

EPR experiment with photons. Testing the *Bell inequality*. Correlation test, count: $E(a,b) = \frac{N(+,+) + N(-,-) - N(+,-) - N(-,+)}{N(+,+) + N(-,-) + N(+,-) + N(-,+)}$ $\left|\Psi(v_1,v_2)\right\rangle = \frac{1}{\sqrt{2}} \left\{ \left|x,x\right\rangle + \left|y,y\right\rangle \right\}$ Source х Coincidences Detector



Determine: S = E(a,b) - E(a,b') + E(a',b) + E(a',b') • L (quantum correlations) • C

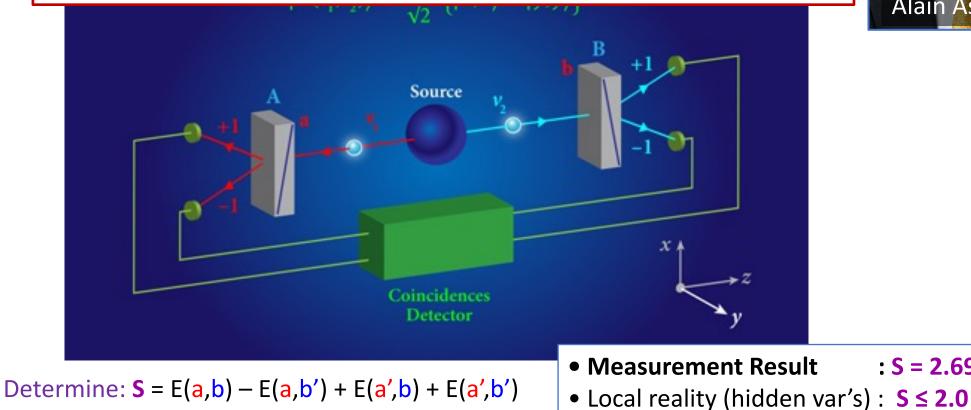
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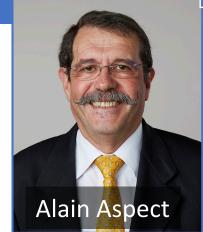
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Observations agree with quantum mechanics and not with local reality!





• Quantum Mechanics : S = 2.7

: S = 2.697 +- 0.015

EPR experiment with photons. Testing the *Bell inequality*.

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Observations agree with quantum mechanics and not with local reality!

There were two "loopholes" (comments of critics):

1. Locality loophole:

The particles and detectors were so close to each other that *in principle* they could have communicated with each other during the Bell test.

2. <u>"Detection loophole":</u>

The detectors only measured *some* of the entangled particles, and they could be a *non-representative* selection of all.

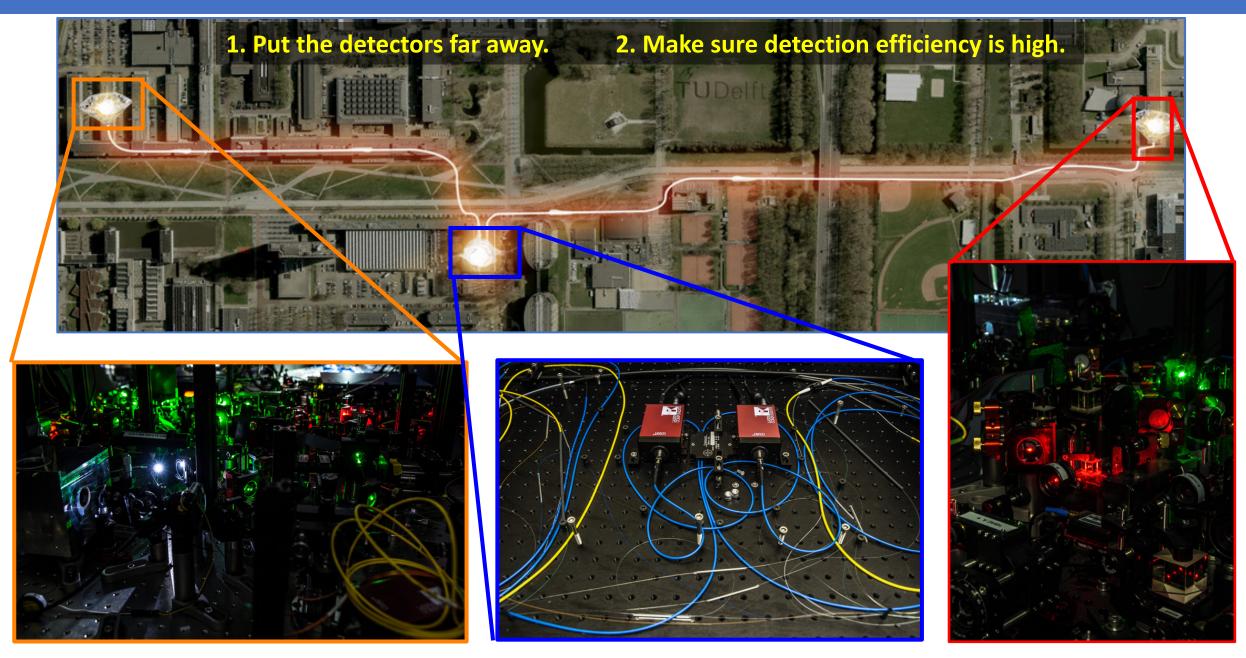
Determine: S = E(a,b) - E(a,b') + E(a',b) + E(a',b')(quantum correlations) Measurement Result

: S = 2.697 +- 0.015

• Local reality (hidden var's) : S ≤ 2.0

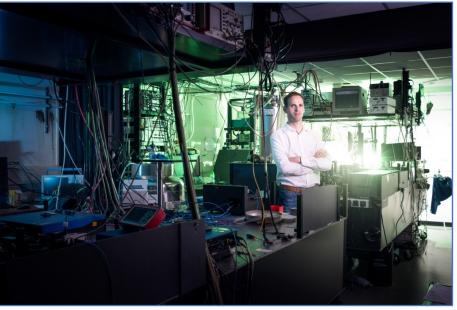
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Closing the loopholes: Delft 2015



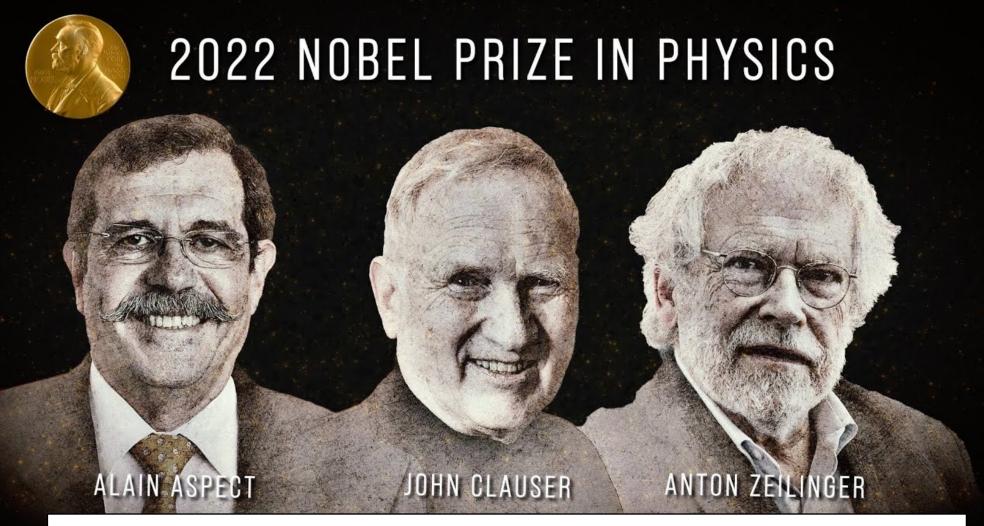
Closing the loopholes: Delft 2015





- Ronald Hanson and his group performed the first EPR experiment without loopholes.
- Measurement of photons that are entangled with electron spins.
- Quantum entanglement again passes the test.
- 🏓 No hidden variables!

2022 Nobel Prize



"for experiments with entangled photons, establishing the violation of Bell inequalities and pioneering quantum information science"

Interpretations of Quantum Mechanics

The Wave function.

- $\psi(x,t)$ contains all information of a system (eg. electron).
- Wave function includes the fundamental laws of physics and describes all types of matter particles and their interactions

Copenhagen Interpretation.

- There is *no physical interpretation* for the wave function.
- As long as *no measurement* is done the *wave-function includes all possible outcomes*. "Nature tries everything".
- When a measurement is done, nature realizes one of the possibilities by the *collapse of the wavefunction* (particle or wave, **x** or **p**, σ_x or σ_z) according to probabilistic laws. "Nothing exists until it is measured".

The Measurement Problem.

- But what is a measurement? Is it an irreversible process? Does it require consciousness?
- There are many interpretations apart from the Copenhagen Interpretation.
 - Objective collapse theory, consciousness causes collapse, Bohm's pilot-wave, QBism, many worlds, many minds, participatory anthropic principle, quantum information ("it from bit"), ...

OUANTUM THEORY AND MEASUREMENT

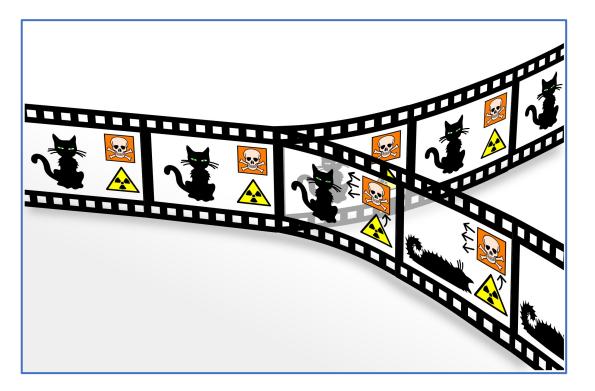
Edited by John Archibald Wheeler and Wojciech Hubert Zurek



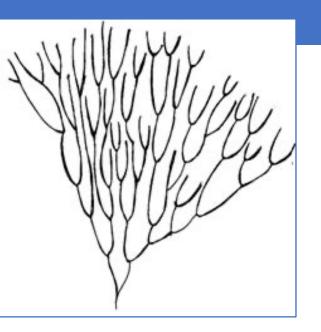
Princeton Series in Physics

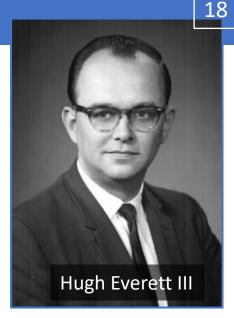
Many Worlds Interpretation

Hugh Everett III (PhD Student of John Wheeler) formulated the Many Worlds Interpretation of quantum mechanics in 1957



The wave function does *not* collapse, but at each quantum measurement *both states continue to exist in a decoupled world*.



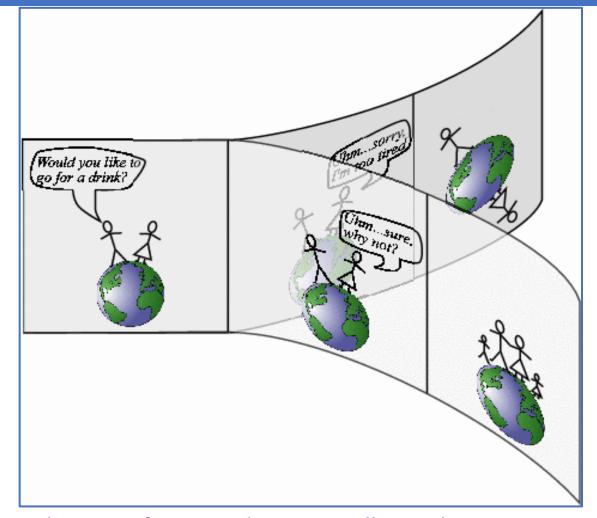


Multiverse:

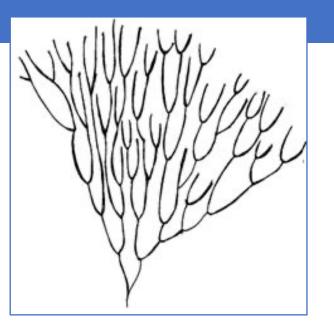
Very large tree of quantum worlds for each quantum decision. The total wave function of complete multiverse is deterministic

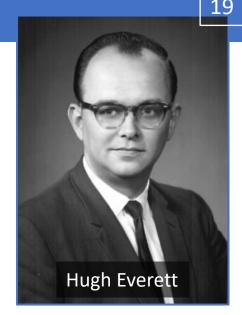
Triggered science fiction stories with "parallel universes".

Many Worlds Interpretation



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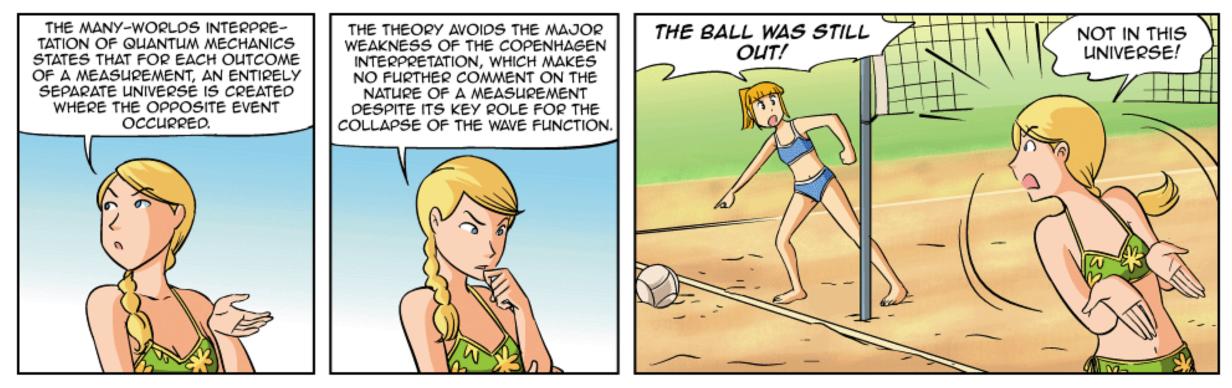




Multiverse:

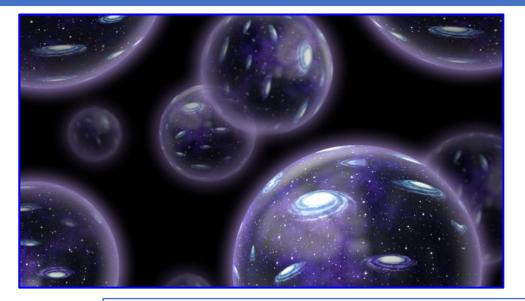
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Sandra and Woo by Oliver Knörzer (writer), Powree (artist) and Lisa Moore (colorist) - www.sandraandwoo.com

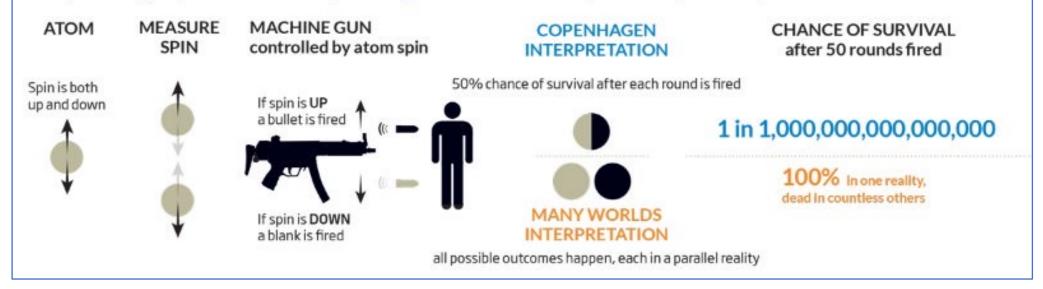
Many Worlds test



- Incredibly many alternative versions of us exist in the multiverse.
- To prove validity of the multiverse:
 - Shoot yourself with 50%-50% quantum probability in russian roulette.
 - Repeat it 50 times.
 - In many worlds survival will *always* happen.
 - You will never have the luck to survive in single universe

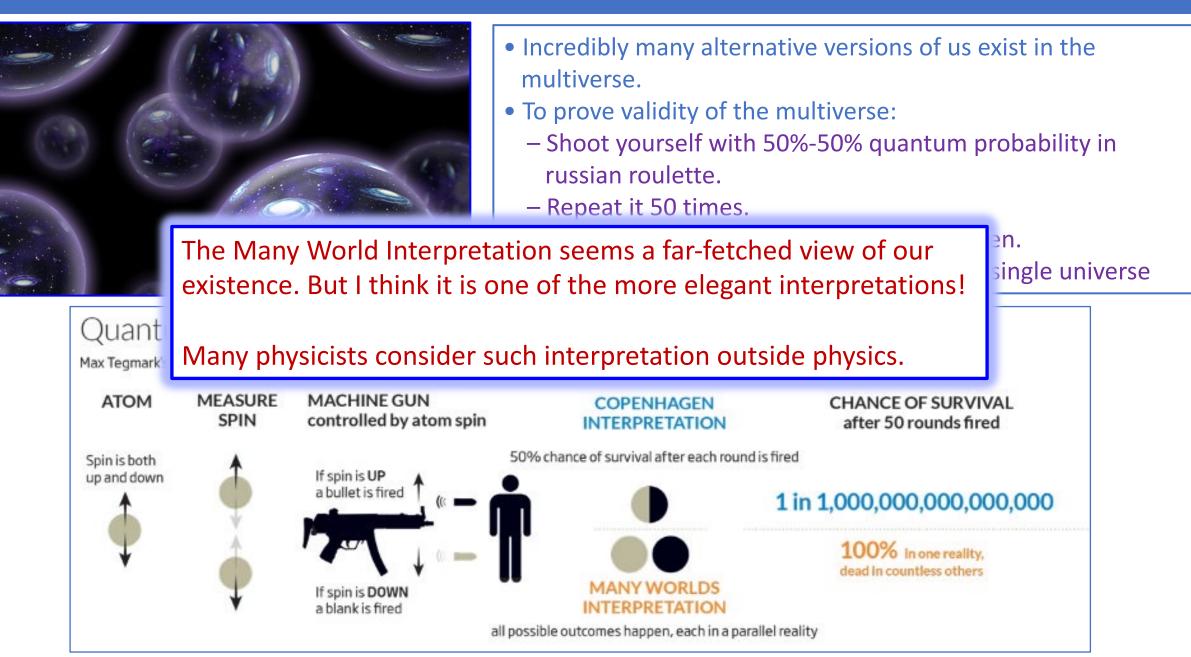
Quantum Russian roulette

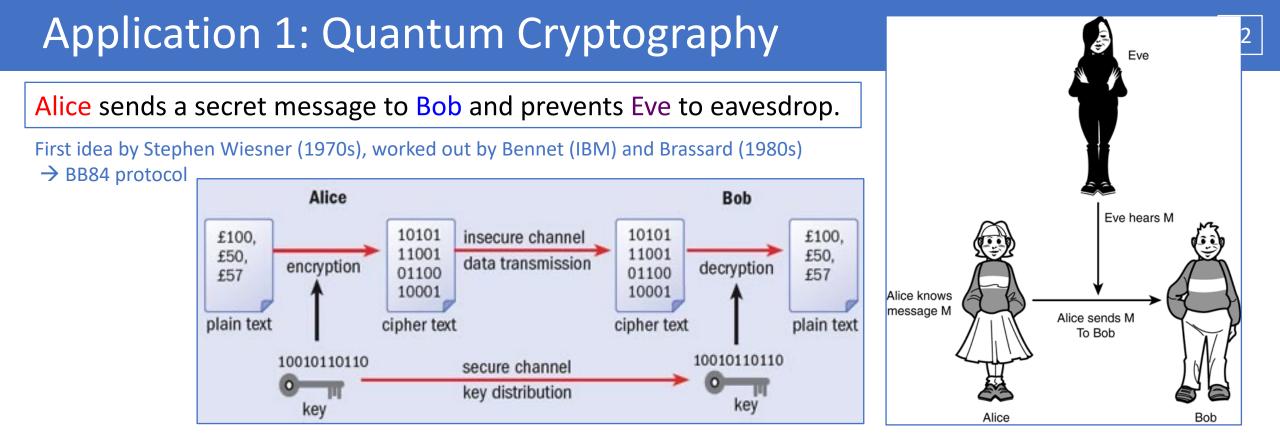
Max Tegmark's thought experiment to test the many-worlds hypothesis involves a machine gun controlled by an atom's spin



21

Many Worlds test





Quantum Key Distribution (QKD):

- 1. Public Channel (Internet, email): send an encrypted message.
- 2. Quantum Channel (Laser + fiber optics) send key to decode the public message
- 3. Eve cannot secretly eavesdrop. She destroys quantum information and is detected.

Application 1: Quantum Cryptography

Alice sends a secret message to Bob and prevents Eve to eavesdrop.

First idea by Stephen Wiesner (1970s), worked out by Bennet (IBM) and Brassard (1980s) → BB84 protocol

10101

11001

01100

10001

cipher text

insecure channel

data transmission

secure channel key distribution

Alice

encryption

10010110110

key

Quantum Key Distribution (QKD):

1. Public Channel (Internet, email): send an encrypted message.

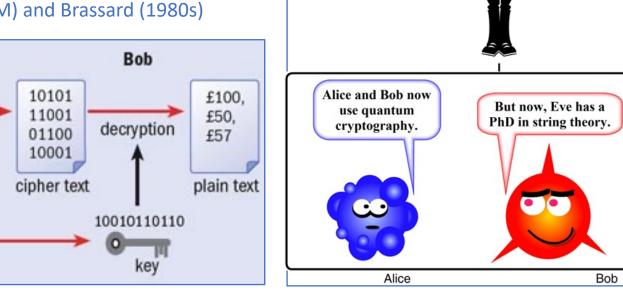
£100.

£50,

£57

plain text

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Eve

Application 1: Quantum Cryptography

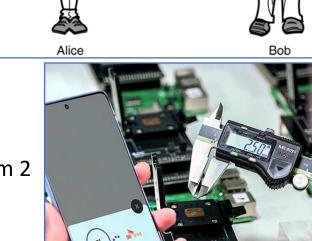
Alice sends a secret message to **Bob** and prevents Eve to eavesdrop.

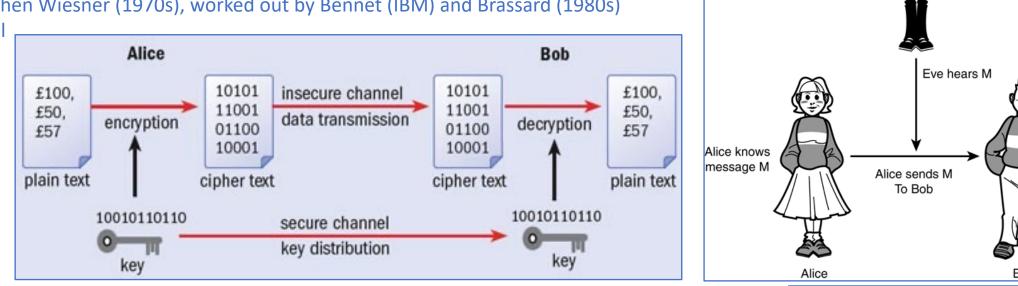
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2021: Samsung' Galaxy Quantum 2 uses quantum cryptography \rightarrow future secure mobile banking





Eve

Application 2: Quantum Computer

<u>Idea</u>: Yuri Manin and Richard Feynman: use superposition and entanglement of quantum states to make a super-fast computer.

Normal computer : bits are either 0 or 1 Quantum computer: qubits are coherent super-positions of states 0 and 1 at the same time. (Eg. Electron spin up and spin down)



Compute with quantum logic. With 2 bits it can do 4 calculations simultaneously. With 3 bits 8 calculations, with n bits 2ⁿ !

Qubit Technologies: Electron spin, Photon polarization, Nuclear spin, quantum dots, ...

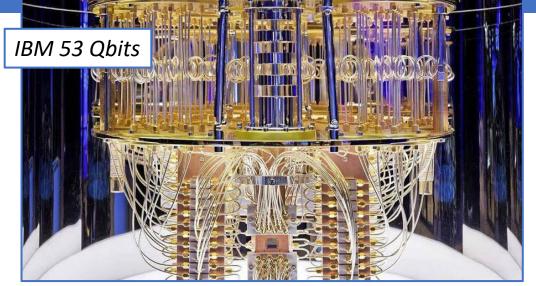
Difficulty: prevent "decoherence".

Application 2: Quantum Computer

"Hardware" technological difficulty:

- Prevent "decoherence"
- IBM, Google, Microsoft competing for the largest quantum computers
- Some devices publicly available in the cloud





Software technological difficulty:

- Prepare system in known state
- Let it evolve according to the algorithm into large simultaneous state.
- Correct solution results from constructive interference of states (→ think double slit)
- Only few algorithms recently existed:
 - Shor factorization
 - Grover's search algorithm
- Now a fast developing science in itself!

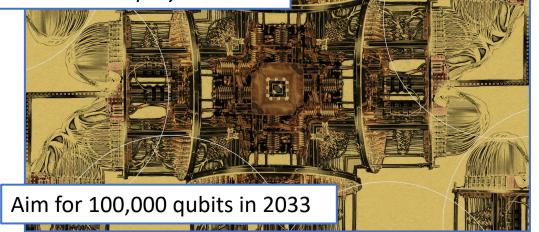
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2023: IBM Osprey 433 Qbits

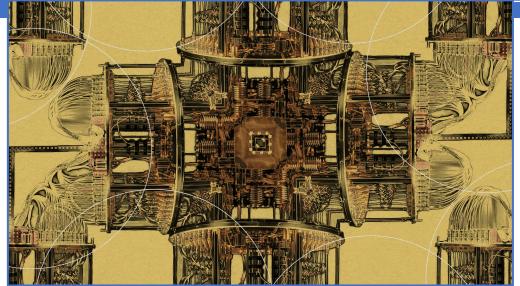


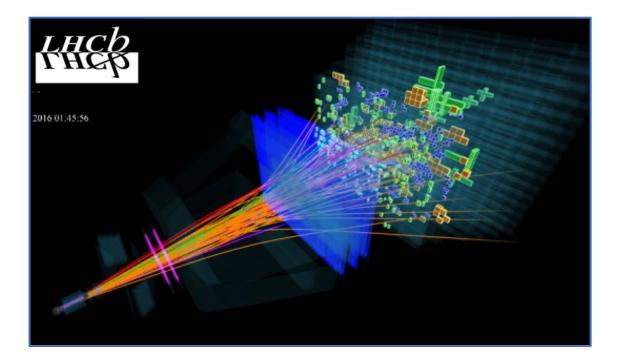
Software technological difficulty:

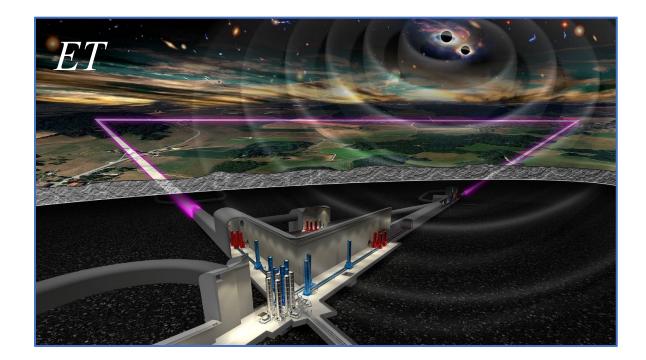
- Prepare system in known state
- Let it evolve according to the algorithm into large simultaneous state.
- Correct solution results from constructive interference of states (→ think double slit)
- Only few algorithms recently existed:
 - Shor factorization
 - Grover's search algorithm
- Now a fast developing science in itself!

2020 – 2023: Joint research IBM and UM

- In 2020, IBM and UM started project on quantum computing ("QC@UM")
 - Departments of Gravitational Wave and Fundamental Physics (GWFP) and Department of Advanced Computing (DACS) @ UM
- Two projects to be ready at ~ 2035:
 - Quantum computing for the High-Luminosity Large Hadron Collider at CERN (HL-LHC)
 - Quantum computing for the Einstein Telescope







2020 – 2023: Joint research IBM and UM

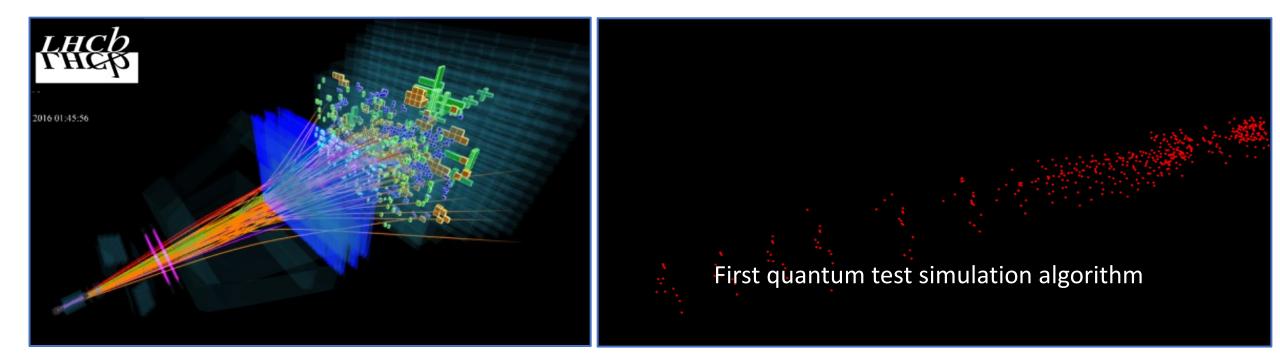
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A quantum algorithm for track reconstruction in the LHCb vertex detector

D. Nicotra,^{*a*} M. Lucio Martinez,^{*a*} J. A. de Vries,^{*a*} M. Merk,^{*a*,*b*} K. Driessens,^{*a*} R. L. Westra,^{*a*} D. Dibenedetto^{*a*} and D. H. Cámpora Pérez^{*a*}

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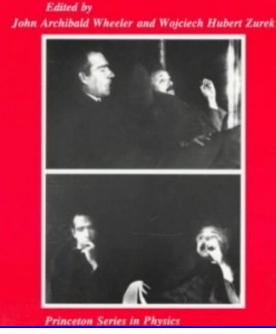
E-mail: d.nicotra@maastrichtuniversity.nl



Summary: Quantum Reality and the Measurement Problem 28

- Quantum reality differs from the classical world.
- Einstein brought a revolutionary way of thinking with relativity theory, but could not accept the revolution of quantum mechanics.
- Bohr never managed to convince Einstein.
- Einstein's objections have been disproven in many tests while the quantum view is always confirmed.
- The Copenhagen interpretation does not provide a meaning for what the wave function is and what the role of the observer (i.e. a measurement) is.

QUANTUM THEORY AND MEASUREMENT



Philosophical:

Would the universe exist if there would be no "observers" to see it? Is the universe perhaps created by acts of observation?

Summary: some further food for thought?

<u>Relativity theory:</u> The finite speed of light means that there is no sharp separation between space and time. (Think of different observers) Universal constant: c = 300 000 km/s

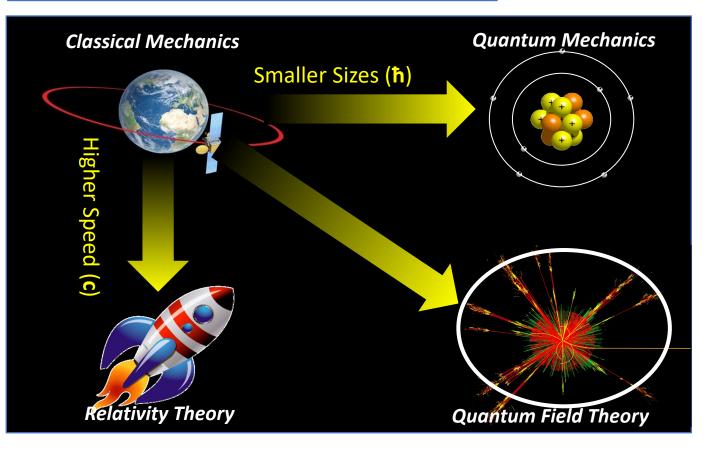
<u>Quantum Mechanics:</u> The finite value of the quantum of action means that there is no sharp separation between a system and an observer Universal constant: $\hbar = 6.6262 \times 10^{-34}$ Js

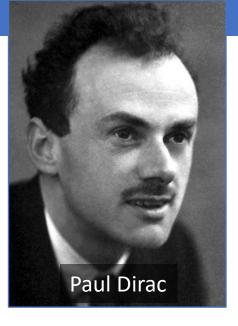
John Wheeler: "Bohr's principle of complementarity is the most revolutionary scientific concept of the century."

Next Week

Next week:

- Matter and Antimatter particles
- Forces and the The Standard Model
- The Large Hadron Collider:
 - Higgs and possible new force?









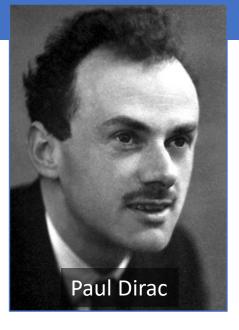


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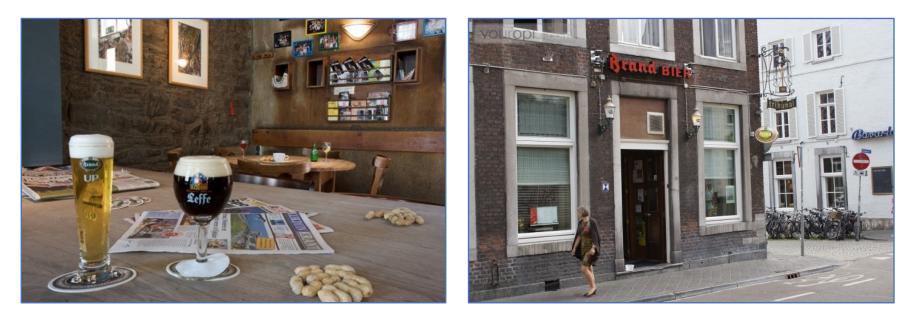








Perhaps time for...



A Table of Quantum Interpretations

Interpre- tation 🗘	Year pub- ≑ lished	Author(s) ÷	Determ- inistic?	Ontic wave- + function?	Unique history? ^{\$}	Hidden variables? ^{\$}	Collapsing wave- + functions?	Observer role?	Local dyna- + mics?	Counter- factually \$ definite?	Extant universal wave- function?
Ensemble interpretation	1926	Max Born	Agnostic	No	Yes	Agnostic	No	No	No	No	No
Copenhagen interpretation	1927	Niels Bohr, Werner Heisenberg	No	Some ^[59]	Yes	No	Some ^[60]	No ^{[61][62]}	Yes	No	No
De Broglie– Bohm theory	1927– 1952	Louis de Broglie, David Bohm	Yes	Yes ^[a]	Yes ^[b]	Yes	Phenomen- ological	No	No	Yes	Yes
Quantum logic	1936	Garrett Birkhoff	Agnostic	Agnostic	Yes ^[c]	No	No	Interpre- tational ^[d]	Agnostic	No	No
Time- symmetric theories	1955	Satosi Watanabe	Yes	No	Yes	Yes	No	No	No ^[63]	No	Yes
Many-worlds interpretation	1957	Hugh Everett	Yes	Yes	No	No	No	No	Yes	III-posed	Yes
Consciousness causes collapse	1961– 1993	John von Neumann, Eugene Wigner, Henry Stapp	No	Yes	Yes	No	Yes	Causal	No	No	Yes
Many-minds interpretation	1970	H. Dieter Zeh	Yes	Yes	No	No	No	Interpre- tational ^[e]	Yes	III-posed	Yes
Consistent histories	1984	Robert B. Griffiths	No	No	No	No	No ^[f]	No ^[g]	Yes	No	Yes
Transactional interpretation	1986	John G. Cramer	No	Yes	Yes	No	Yes ^[h]	No	No ^[i]	Yes	No
Objective- collapse theories	1986– 1989	Ghirardi– Rimini– Weber, Roger Penrose	No	Yes	Yes	No	Yes	No	No	No	No
Relational interpretation	1994	Carlo Rovelli	No ^[64]	No	Agnostic ^[j]	No	Yes ^[k]	Intrinsic ^[1]	Possibly ^[m]	No	No
QBism	2010	Christopher Fuchs, Rüdiger Schack	No	No ^[n]	Agnostic ^[0]	No	Yes ^[p]	Intrinsic ^[q]	Yes	No	No