

PHY3004: Nuclear and Particle Physics Marcel Merk, Jacco de Vries



The Standard Model



<u>Recap</u>: "Seeing the wood for the trees"

The Standard Model

- Lecture 1: "Particles"
 - Zooming into constituents of matter
 - Skills: distinguish particle types, Spin
- Lecture 2: "Forces"
 - Exchange of quanta: EM, Weak, QCD
 - Skills: 4-vectors, Feynman diagrams
- Lecture 3: "Waves"
 - Quantum fields and gauge invariance
 - Dirac algebra, Lagrangian, co- & contra variant
- Lecture 4: "Symmetries"
 - Standard Model, Higgs, Discrete Symmetries
 - Skills: Lagrangians, Chirality & Helicity
- Lecture 5: "Scattering"
 - Cross section, decay, perturbation theory
 - Skills: Dirac-delta function, Feynman Calculus
- Lecture 6: "Detectors"
 - Energy loss mechanisms, detection technologies











Lecture 1: "Particles" - Nuclear





Lecture 1: "Particles" - subatomic



let

Lecture 1: "Particles"

Classification of particles

- Lepton: fundamental particle
- Hadron: consist of quarks
 - Meson: 1 quark + 1 antiquark (π^+ , B_s^0 , ...)
 - Baryon: 3 quarks (*p* ,*n* , Λ, ...)
 - Anti-baryon: 3 anti-quarks

• Fermion: particle with half-integer spin.

- Antisymmetric wave function: obeys Pauliexclusion principle and Pauli-Dirac statistics
- All fundamental quarks and leptons are spin-1/2
- Baryons (S=1/2, 3/2)
- Boson: particle with integer spin
 - Symmetric wave function: Bose-Einstein statistics
 - Mesons: (S=0, 1), Higgs (S=0)
 - Force carriers: *γ*, *W*, *Z*, *g* (S=1); graviton(S=2)



- Electromagnetism
- Weak Interaction
- Strong Interaction
- No Gravitation

Lecture : "Forces"

	North Contraction			Q Cope
	Gravity	Weak (Electro	Electromagnetic weak)	Strong
Carried By	Graviton (not yet observed)	w* w z°	Photon	Gluon
Acts on	All	Quarks and Leptons	Quarks and Charged Leptons and W ⁺ W ⁻	Quarks and Gluons
Strength	0.000000000000000 0000000000000000 000000	0.001	1	100

Attractive and Repulsive forces and the quantum exchange





There is no "action at a distance"

EM: photon Weak: W, Z bosons Strong: gluons Gravitation: graviton(?)

Example of a quantum process: $e^+ + e^- \rightarrow q \ \overline{q} \ g$



- Electron-positron annihilation
- Produce a "virtual" photon
- Photon produces a quark + antiquark
- Quark can radiate a gluon

Example of a quantum process: $e^+ + e^- \rightarrow q \ \overline{q} \ g$





Feynman diagram

<u>Note:</u>

- Electron-positron annihilation
- Produce a "virtual" photon
- Photon produces a quark + antiquark
- Quark can radiate a gluon

This is a *graphic* representation of a *calculation* that represents a quantum event. We use it to *talk* about it.

Do not take it literally as what happens

Another example

- Kaon decay with *weak* interaction mediated by a *W*-boson
- Quark anti-quark produced by the *strong* interaction mediated by a gluon



Part 1

The Electromagnetic Interaction Quantum Electrodynamics (QED)

Quantum Electrodynamics (QED)



- "strength" of the "vertex coupling" is equal to the elementary charge *e*
- Note: this vertex can only be part of a process since energy and momentum cannot be conserved at the same time in this "2-to-1" process
 - This is an off-shell or virtual photon

A Real QED Process: Möller scattering



A Real QED Process: Möller scattering



A Real QED Process: Möller scattering



A Real Process: Bhabha Scattering

- Scattering of electron and positron, two quantum processes ("Feynman diagrams") in one real process:
 - Spacelike "s-channel" exchange
 - e^- and e^+ annihilate into a photon, which converts back to a e^- and e^+ pair
 - Timelike "t-channel" exchange
 - e^- and e^+ scatter in each others EM field



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Feynman Diagram



Scattering with photons



Perturbation Theory

Feynman diagrams we use describe the lowest order "Perturbation Theory". Calculations with Feynman diagrams are never exact, always an approximation.

- We simply do not know how to do exact calculations in particle physics
- QED is extremely precise because many complicated diagrams have been calculated



given external lines represents the actual physical process. Of course, there's a vee problem here: there are infinitely many Feynman diagrams for any particular reaction! Fortunately, each vertex within a diagram introduces a factor of $a = e^2/\hbar c = 1/137$, the *fine structure constant*. Because this is such a small number, diagrams with more and more vertices contribute less and less to the final result, and, depending on the accuracy you need, may be ignored. In fact, in QED it is rare to see a calculation that includ

vertices. The answers are only approximate, + mation is valid to six significant digits, only complain.

The Feynman rules enforce conservation of vertex, and hence for the diagram as a whole vertex by itself does not represent a possible he diagram, but calculation would assign to i burely kinematical: $e^- \rightarrow e^- + \gamma$ would viola tenter-of-mass frame the electron is initially at a lecay into a photon plus a recoiling electron become energy greater than mc^2 .) Nor, for instance possible, although it is easy enough to draw the

2.2 Quantum Electrodynamies (QED)

travel at the spece of light: an electron-positron pair can annihilate to make two photons, but not one. Within a larger diagram, however, these figures are perfectly acceptable, because, although energy and momentum must be conserved at each vertex. a virtual particle does not carry the same mass as the corresponding free particle. In fact, a virtual particle can have any mass.* In the business, we say that virtual particles do not lie on their mass shell. External lines, by contrast, represent real particles, and these do carry the 'correct' mass.^t

I have been assuming that the charged particle in question is an electron,[‡] but it possible, although it is easy enough to draw de COM bind ust as well be a muon, ity, or a quark. What would you make of the following

of the fundamental QED vertex:

е m е



The background of Feynman Diagrams

- More about scattering and Feynman diagrams in Lecture 5
- For an intuitive approach to Feynman diagrams, see wikipedia: <u>https://en.wikipedia.org/wiki/Quantum_electrodynamics</u> and references therein, or the booklet of Feynman:
 - "The strange theory of light and matter"

Part 2 The Weak Interaction

Historical: Fermi 4-point interaction

- Becquerel discovered radioactivity based on the weak force • $n \rightarrow p + e + \overline{\nu}$
- The original model for the weak interaction is from Fermi
 - For obvious reasons it is called the 4-point 'contact' interaction (1933).
 - The strength of the interaction was given by Fermi's constant $G_F = 10^{-5}$

$$n + \nu \to p + e$$
 $n \to p + e + \overline{\nu}$



Quantum zoom-in on Fermi 4-point interaction



Maastric Stippilzer toyelectrodynamics the weak interaction has at propagator

- W spin-1 boson
- At quark level it involves a $d \rightarrow u$ transition

The Weak Interaction

• Feynman rules



- W-boson has electric charge
 - The process is called a *charged current*
- q^2 is the momentum transfer from the hadronic to leptonic vertex
 - Here due to mass difference $m_n m_p$
- Effect of propagator is encodicately of when q² ~ M_W²
 If q² is large: *resonance* energy of W
 In that case weak force is storig 2 > effe
 If q² is small: then effectively a 4-point Fermi coupling Note: if M_W large
 - Propagator ~ $1/M_W^2$ → weak force

•
$$G_F = \frac{g^2}{8M_W^2}$$
 ; $\alpha_W = \frac{g^2}{2\pi} = \frac{1}{30} > \alpha_{QED}$

 The weak coupling generative is large!
 Interaction is weak due to large W mass, but also propagator'

W and Z bosons

- Glashow, Salam, Weinberg (GSW model, 1968) predict three weak mediators
 - W^+ , W^- , Z bosons
- Discovery of the W and Z bosons at CERN, 1983, UA1 and UA2 experiments
 - Look at high energy proton antiproton collisions
 - $M_W = 80 \ GeV/c^2$, $M_Z = 91 \ GeV/c^2$ as predicted by GSW model





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P+P→ Z°+X Lµ⁺µ Virtuality

• How can be a decay $n \rightarrow p + e + \overline{\nu}$ work, if the W has a mass of 80 GeV??



- Exchange of "virtual" particles, also called "off-shell": $q^2 = E^2 \vec{p}^2 \neq m^2$
- Heisenberg: E is undetermined as $\Delta E \Delta t \geq h/2$ with $|0\rangle = \Delta E = \sqrt{\vec{q}^2 + m^2} (Q^2 = \text{`energy' of V})$ For small q ($\Delta E = i n q^2 \geq m q^2$) force R : eff $R \sim c \Delta t \approx \frac{\hbar}{2mc} \sim 1 q^2 \Delta t = 18$
- Notice the resonance behaviour for $q^2 \approx M_W^2$ Not just 'vertex', but also 'propagator'

Precision studies with Z bosons: "Electroweak Force"

• The LEP collider did many precision studies of the weak interaction with e^+e^- annihilation collisions at collision energy around 91 GeV/c^2 .



Similarity of Electromagnetic (γ) and Weak (Z) force



Examples of processes: "neural currents"

• Electromagnetic: couples to electric charge: '+ and -'



• Weak "Neutral Currents": couples to weak charge: isospin 'up' and 'down'



Examples of processes that *do not exist*

• Electromagnetic:



• Weak "Neutral Currents":



 γ and Z only couple to particles within one generation and only to quark or lepton pairs

Self coupling

- In electromagnetism a photon has no electric charge
- In the weak interaction the force carriers have weak charge themselves
 - The weak charge is called "weak isospin": W^- : $I_3 = -\frac{1}{2}$; $Z^0: I_3 = 0$; $W^+: I_3 = +\frac{1}{2}$
 - The following diagrams are possible



The *W* weak force: "charged currents"

- The *W*-boson carries electric charge
- The W connects the weak *isospin* (I_3) 'up' and 'down' type particles of a generation
 - W^+ and W^- do the opposite
- 2nd and 3rd generation muon and tau can decay because neutrino's are light!





- How does a kaon decay?
 - $K^- = s\overline{d}$
- The c-quark is heavier than the s quark:
 - $s \rightarrow c \ e \ \overline{\nu_e}$ is not possible
Generations

- Does the *W* only couple between particles of one generation?
 - Leptons: yes
 - Quarks: no!
 - Couplings between generations are possible for the *W*!
- Kaon decays



• "Hadronic": $K^+ \rightarrow \pi^+ \pi^+ \pi^-$





The Strong Interaction Quantum Chromodynamics (QCD)

Color singlets

- Quarks are "locked-up" in hadrons
 - Technical term: confinement
- Quarks carry color charge: r, g, b
- All physical objects are color neutral or color singlets: confinement!
 - Baryons: rgb or $\overline{r} \overline{g} \overline{b}$
 - Mesons: $r \overline{r}$ or bb or $g \overline{g}$
- The color force, transmitted by gluons, is very strong
 - Requires a lot of energy to separate a color charge from a color neutral object
 - Trying to do so will produce another color neutral object



Gluon color: *g b* There are 8 gluons + 1 colorless singlet



• Animation of a color neutral neutron:



Are quarks and gluons real or a bookkeeping devise?

Proton Substructure: discovery of "partons" or "quarks" (1968)

• Similarly to Rutherford scattering ("substructure of the nucleus") deep inelastic scattering of electrons on protons show the proton substructure



Discovery of the Gluon (1979)

- The gluon was discovered in e^+e^- collisions at DESY in Hamburg
 - "3-jet events"



• Feynman diagram for

quark-quark interaction

• At LHC





3-Jet event at LEP - Delphi (1989 – 2000)



Yukawa's pion exchange vs gluon exchange

- Yukawa: Nuclear force is carried by massive gluon
- QCD: Strong force is mediated by massless gluon









Fundamental Vertices of the strong interaction

- QED: photon couples to charge
- Weak: W couples to isospin
- Strong gluon couples to color
 - 3 colors and anti-colors
 - Gluon carries charge itself!
 - 8 different gluons (9 1 symmetric)





• Leptons carry no color: leptons do not feel strong (nuclear) interaction

Abelian and non-Abelian

- Photons have no electric charge:
 - Photons do not interact with each other ("Abelian" in group theory)
- Gluons carry color charge:
 - Gluons do interact with each other ("non-Abelian" in group theory)

QED, QCD 00000000 www 000000000etc.

QCD

Vacuum behaves like dielectric: by QED and even more so by QCD...

Screening

- Charge screening effect:
 - Around a charge q(+) dipoles align
 - Halo of negative charge





Fig. 2.1 Screening of a charge q by a dielectric medium.

triumphs of quantum chromodynamics (QCD) was the discovery that in this theory







Anti-screening

- Anti-screening:
 - gluon self coupling opposite effect
 - Crucial parameter: $a \equiv 2f - 11c$

where: f = number

- c = number
- In case a > 1 (QED *increases* for short
- In case *a* < 1 (QCD decreases for short

effective charge, as a function of distance, it would look something like F The effective charge increases at very small distances.

Now, it so happens that in quantum electrodynamics the vacuum itsel like a dielectric; it sprout such as these:

The virtual electron in each 'bubble' is attracted toward q, and the virtual

and reduces its field. Once again, however, if you get too close to a, the

QED, QCD

charge.

So much for electrodynamics. The important added ingredient. Not onl (which, by itself, would again lead distances), but now there are also the



It is not clear a priori what influence is repelled away; the resulting manufience pately treat tharge Ista SGC heir effect is the opposite

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- disappears. What plays the role of the $\alpha_{s} > \sim 1$ Compton wavelength of the electron, • Asymptotic freedom: astranount tos stance:chai
 - Coupling $\alpha_s \sim 0$ at very smalling the unscreened ('close-up similar the unscreened similar th
 - Quarks and gluons become "free"
 - →Quark gluon plasma

Running coupling constants and unification?

- Running couplings: 'beta'-function
- Higher energy means shorter distance
- Lines do not cross in one point



Running coupling constants and unification?

- Unification with SUSY?
- 10¹⁵ GeV
 - Grand Unified Theory
- 10¹⁹ GeV:
 - Planck scale → quantum gravity?



- 10¹⁵ GeV -> Grand Unified Theory?
- Planck scale (~10¹⁹ GeV) —> Gravity! —> Theory of Everything?

Standard Model of particles and forces



Standard Model of Elementary Particles

Summary Forces: Intermediate Vector Bosons

- SM: forces are transmitted by vector mesons, particles with spin-1:
 - Electromagnetism:
 - Long range : photon γ , $M_{\gamma} = 0$
 - Photon carries no E.M. charge
 - Weak interaction:
 - Very short range: W and Z bosons, $M_W = 80 \text{ GeV}$, $M_Z = 91 \text{ GeV}$
 - Weak isospin charge. W and Z have I-charge.
 - Strong interaction:
 - Very short range: gluon g , $M_g = 0$
 - Gluons carry color \rightarrow confinement \rightarrow very short range
 - Pairs of quarks can transmit strong force: Yukawa's mesons
 - Short range
- Gravitation: transmitted by spin-2 particle?
 - Graviton
 - Long range: $M_g = 0$





Discussions Topics belonging to Lecture 2

<u>Topic-4</u>: Flavour changing Weak interaction

- What are neutral currents?; what are charged currents?
- Which transitions are allowed by the charged current?
- What is the consequence for stability of 2nd and 3rd generation particles?

Topic-4; El-Topic Havors of the Standard Model W-



Topic-4 ne Charles Contraction and Model W-



Topic-4; Flaten Representation and Representation of the second s



Topic-4; Flat Charge Big Out Statistic Model



Topic-4; Elapour Charge Ouark Interactions MCB / iolation



<u>Topic-5</u>: The CKM and PMNS matrices

- What is different and what is the same for quarks and lepton in the charged current weak interaction?
- Explain how possibly a matter antimatter asymmetry can be implemented?
 - Think of complex coupling constants

- Mass eigenstates $|q\rangle$ are the eigenstate solutions of the free Hamiltonian
- Weak or flavour eigenstates $|q'\rangle$ are the eigenstate solutions of the weak interaction Hamiltonian.
 - They are unitary linear combination, or "rotation" of mass eigenstates.
- The the weak interaction can be written as:



Topic-5: Flavour eigenstates and Mass eigenstates



Topic-5: Why a matrix notation?

• Model:

- Charged weak current does **not** couple to $\begin{pmatrix} u \\ d \end{pmatrix}, \begin{pmatrix} c \\ s \end{pmatrix}, \begin{pmatrix} t \\ b \end{pmatrix}$
- but instead to
 - $\begin{pmatrix} u \\ d' \end{pmatrix}$, $\begin{pmatrix} c \\ s' \end{pmatrix}$, $\begin{pmatrix} t \\ b' \end{pmatrix}$
- Where

$$\begin{pmatrix} d'\\s'\\b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub}\\V_{cd} & V_{cs} & V_{cb}\\V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

CKM matrix: Cabibbo, Kobayashi Maskawa



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Three Generations of Matter





Topic-5: The CKM matrix V_{CKM} - 3 vs 2 Generations



Wolfenstein parametrization: V_{CKM} =

 $\begin{pmatrix} 1 - \frac{1}{2}\lambda^{2} & \lambda & A\lambda^{3}(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^{2} & A\lambda^{2} \\ A\lambda^{3}(1 - \rho - i\eta) & -A\lambda^{2} & 1 \end{pmatrix}$ $\rightarrow 1 \text{ CP violating phase}$



• 3 generations is the minimal particle content to generate CP violation (In Standard Model).

Topic-5: The Flavour Puzzle

- Why 3?
- Why are the couplings what they are?
- Is there a relation with the masses of the quarks?





Topic-5: Flavour in the leptons!

- It turns out neutrino's have mass, too!
 - The mass is very tiny
- The generation mixing also occurs for neutrino's
 - Slightly different nomenclature:

• Quarks (CKM):
$$\binom{u'}{s'}_{b'} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

• Leptons (PMNS):
$$\begin{pmatrix} v_1 \\ v_2 \\ v_3 \end{pmatrix} = \begin{pmatrix} U_{1e} & U_{1\mu} & U_{1\tau} \\ U_{2e} & U_{2\mu} & U_{c\tau} \\ U_{3e} & U_{3\mu} & U_{3\tau} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

- U_{PMNS} : Pontecorvo, Maki, Nakagawa, Sakata mixing matrix
- (Difficult) Question: why is lepton mixing not seen in decays?
 - It is only seen in neutrino oscillations





Topic-6: Variational calculus and Lagrangians

- Explain the idea behind variational calculus?
- What is a conservative Force?
- Define a Lagrangian: $\mathcal{L} = T V = \frac{1}{2}m(\dot{x}^2 + \dot{y}^2 + \dot{z}^2) V(x, y, z)$
- Show how Newton's law in one dimension: $F = m\ddot{x}$ leads to the Euler Lagrange equation (in case of a conservative force):

$$\frac{d}{dt} \left(\frac{\partial \mathcal{L}}{\partial \dot{x}} \right) = \frac{\partial \mathcal{L}}{\partial x}$$

Topic-6: Lagrange Formalism classical

- Griffiths §10.1
- Classical Mechanics: The Lagrangian leads to equations of motion
 - $L(q_i, \dot{q}_i) = T V$ where q_i and \dot{q}_i are the generalized coordinates and velocities.
 - The path of a particle is found from *Hamilton's principle of least action*

$$S = \int_{t_1}^{t_2} dt \, L(q, \dot{q}) = 0 \qquad \qquad \delta S = 0$$

From this the *Euler Lagrange equations* follow and provide the equations of motion:

$$\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q_i}} \right) = \frac{\partial L}{\partial q_i}$$
 See: https://en.wikipedia.org/wiki/Lagrangian_mechanics

- Example: Ball falls from height y = h : q = y, $\dot{q} = dy/dt = v_y$
 - $E_{pot} = V = mgq$ • $E_{kin} = T = \frac{1}{2}m\dot{q}^2$ $L = T - V = \frac{1}{2}m\dot{q}^2 - mgq$
- Euler Lagrange: $\partial L/\partial q = mg$; $\partial L/\partial \dot{q} = m\dot{q}$
 - $\frac{d}{dt}\left(\frac{\partial L}{\partial \dot{q}_i}\right) = \frac{\partial L}{\partial q_i}$ gives $m\ddot{q} = mg \rightarrow \dot{q} = gt + v_0 \rightarrow q = y = \frac{1}{2}gt^2 + v_0t + y_0$

Exercises belonging to Lecture 2

Exercise-4: Variational calculus Lagrange Formalism classical

- Example of variational calculus and least action principle: what is the shortest path between two points in space?
 - Distance of two close points:

$$dl = \sqrt{dx^2 + dy^2} = \sqrt{dx^2 \left(1 + \left(\frac{dy}{dx}\right)^2\right)} = \sqrt{1 + {y'}^2} dx \quad \text{with } y' = dy/dx$$

• Total length from (x_0, y_0) to (x_1, y_1) :

$$l = \int_{x_0}^{x_1} dl = \int_{x_0}^{x_1} \sqrt{1 + {y'}^2} dx = \int_{x_0}^{x_1} f(y, y') dx$$

- Task is to find a function y(x) for which l is minimal
- In general assume the path length is given by: $I = \int_{x_0}^{x_1} f(y, y') dx$
- Variational principle: shortest path is stationary: $\delta I = 0$ a) Write $\delta f(y, y') = \frac{\partial f}{\partial y} \delta y + \frac{\partial f}{\partial y'} \delta y'$ where $\delta y' = \delta \left(\frac{dy}{dx}\right) = \frac{d}{dx} (\delta y)$ Show using partial integration that $\delta I = 0$ leads to the Hamilton Lagrange equation $\frac{\partial f}{\partial y} - \frac{d}{dx} \frac{\partial f}{\partial y'} = 0$
 - Here for the shortest path we have $f(y') = l = \sqrt{1 + {y'}^2}$. Then $\partial f / \partial y = 0$ and $\partial f / \partial y' = y' / \sqrt{1 + {y'}^2}$ b) Show that the variational principle leads to a straight line path: $\frac{d}{dx}\left(\frac{y'}{\sqrt{1+y'^2}}\right) = 0$ or that y' is a constant: dy/dx = a; y = ax + b



- a) Start with the expression for a Lorentz transformation along the x^1 axis. Write down the *inverse* transformation (i.e. express (x^0, x^1) in $(x^{0'}, x^{1'})$)
- b) Use the chain rule to express the derivatives $\partial/\partial x^{0'}$ and $\partial/\partial x^{1'}$ in $\partial/\partial x^{0}$ and $\partial/\partial x^{1}$
- c) Use the result to show that $(\partial/\partial x^0, -\partial/\partial x^1)$ transforms in the same way as (x^0, x^1)
- d) In other words the derivative four-vectors transform inversely to the coordinate four-vectors:

$$\partial^{\mu} = \left(\frac{1}{c}\frac{\partial}{\partial t}, -\vec{\nabla}\right) \text{ and } \partial_{\mu} = \left(\frac{1}{c}\frac{\partial}{\partial t}, \vec{\nabla}\right)$$

Note the difference w.r.t. the minus sign!

e) Explicit 4-vectors: (ct, x, y, z) and $(E/c, p_x, p_y, p_z) \rightarrow$ use next $c \equiv 1$

Griffiths: chapter 3



Note that the minus sign is "opposite" to the case of the coordinate four-vectors.

Exercises 6, 7, 8

- 6. [Griffiths exercise 2.2] "Crossing lightsabers"
 - Draw the lowest-order Feynman diagram representing Delbruck scattering: $\gamma + \gamma \rightarrow \gamma + \gamma$
 - This has no classical analogue. Explain why.
- 7. [Griffiths exercise 2.4]
 - Determine the invariant mass of the virtual photon in each of the lowest-order Feynman diagrams for Bhabha scattering. Assume electron and positron at rest.
- 8. [Griffiths exercise 2.7]
 - Examine the processes in *the left column* of Griffiths exercise 2.7 and state which one is possible or impossible, and why / with which interaction.
 Hint: draw the corresponding Feynman diagrams if needed.