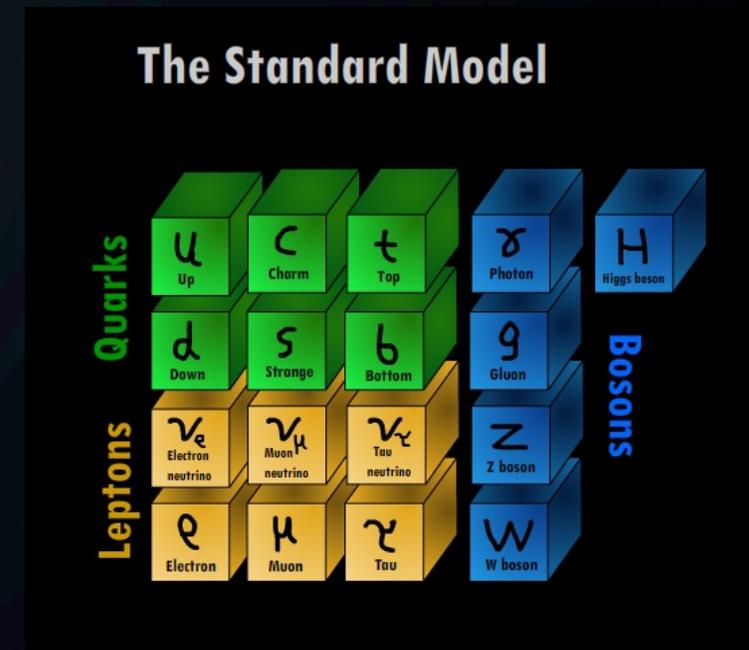




PHY3004: Nuclear and Particle Physics
Marcel Merk, Jacco de Vries



Introducing the lecturers

Lecturers:

Marcel Merk

Jacco de Vries



Tutors:

Lex Greeven

Robbert Geertsema

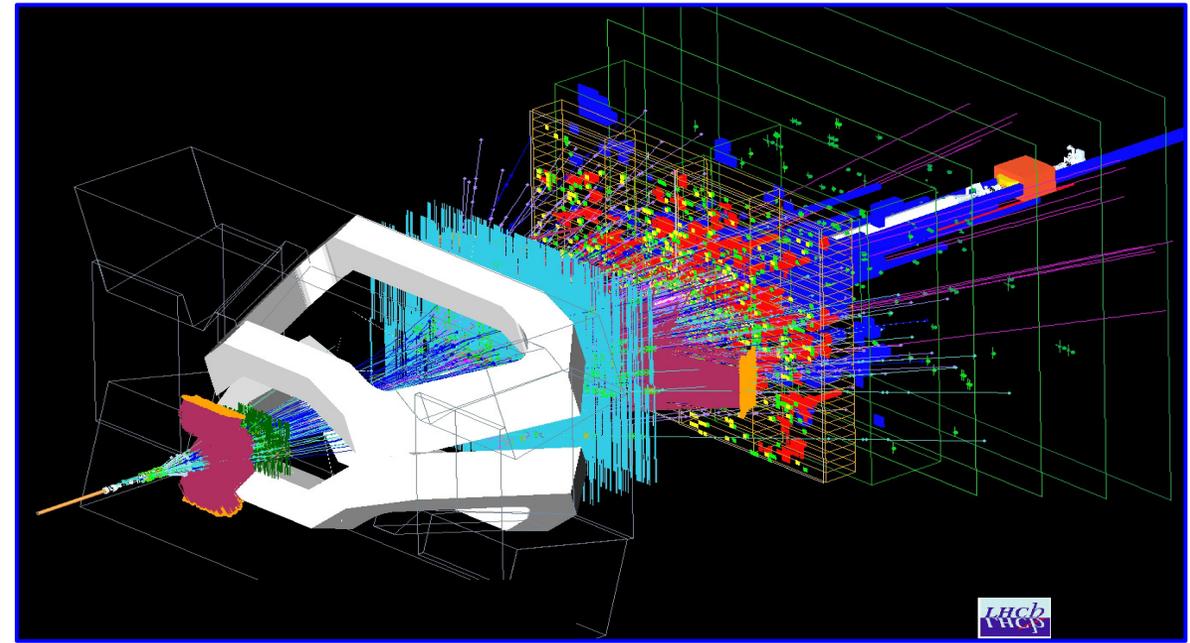
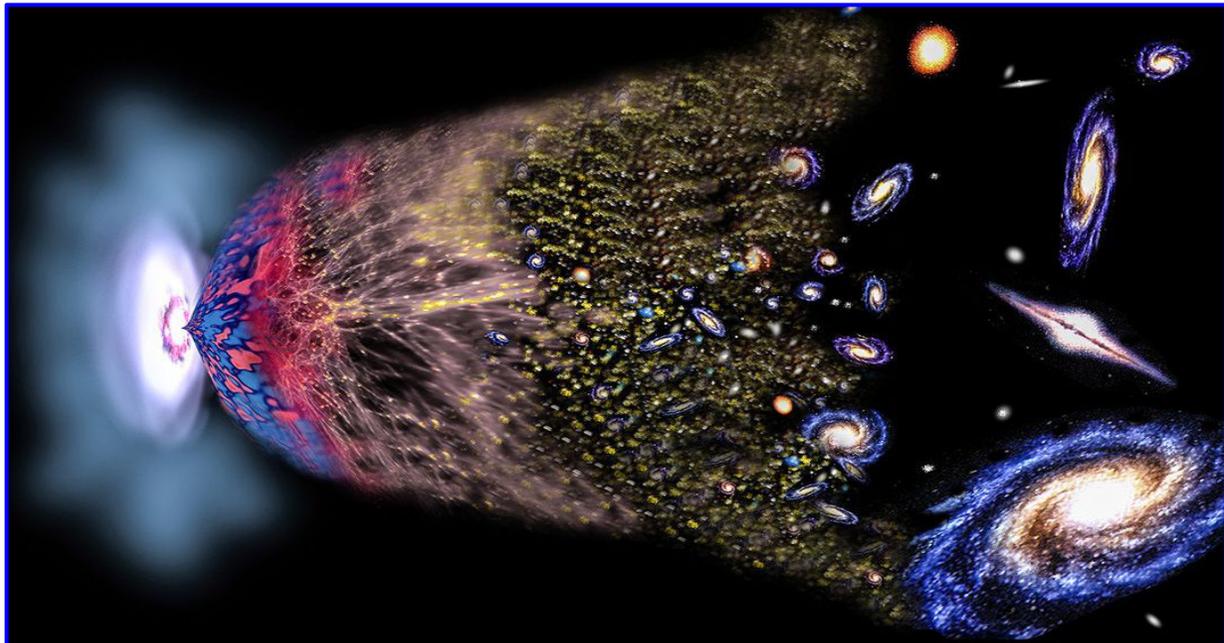


Research (theoretical):

- Why a matter-vs-antimatter asymmetry in nature?
- Why do we have three generations of particles?

Research (experimental):

- Detector technology at the Large Hadron Collider.
- Measurements of CP violation rare decays



The Goal of these Lectures

- A first course in particle physics theory and experiment
 - Solid preparation for a master on particle physics
- Various topics introduced
 - Cannot go to “deep” in each topic
 - Aim is to give you a “feel” for the subject
 - Quite some mathematics later on, but focus on the concept if you find the math difficult!
- Follow-up possibilities in master education:
 - Theoretical Particle Physics: Field theory courses
 - Theoretical and Experimental Particle Physics: Advanced particle physics courses
 - Experimental Particle Physics: Detection techniques for particles

Particle Physics – contents of the course

- Week 1: “Particles”
 - Nuclear Physics and Particle Physics
- Week 2: “Forces”
 - Electromagnetism, Weak force, Strong force
- Week 3: “Waves”
 - Wave Equations
 - Schrodinger, Klein – Gordon, Dirac, Photon-field
 - Lagrange Hamilton mechanics and Gauge Invariance
- Week 4: “Symmetries”
 - The Standard Model gauge symmetry
 - Discrete symmetries
 - Symmetry breaking: the Higgs Mechanism
- Week 5: “Scattering”
 - Scattering Theory
 - Feynman Calculus
- Week 6: “Experiments”
 - Experimental techniques, LHC detectors

- Week 1 – 5:
 - Homework exercises 1 exam “bonus”
- Week 6: Research Project
 - Written paper 5 points
 - Presentation 5 points
- Week 7: Exam 10 points

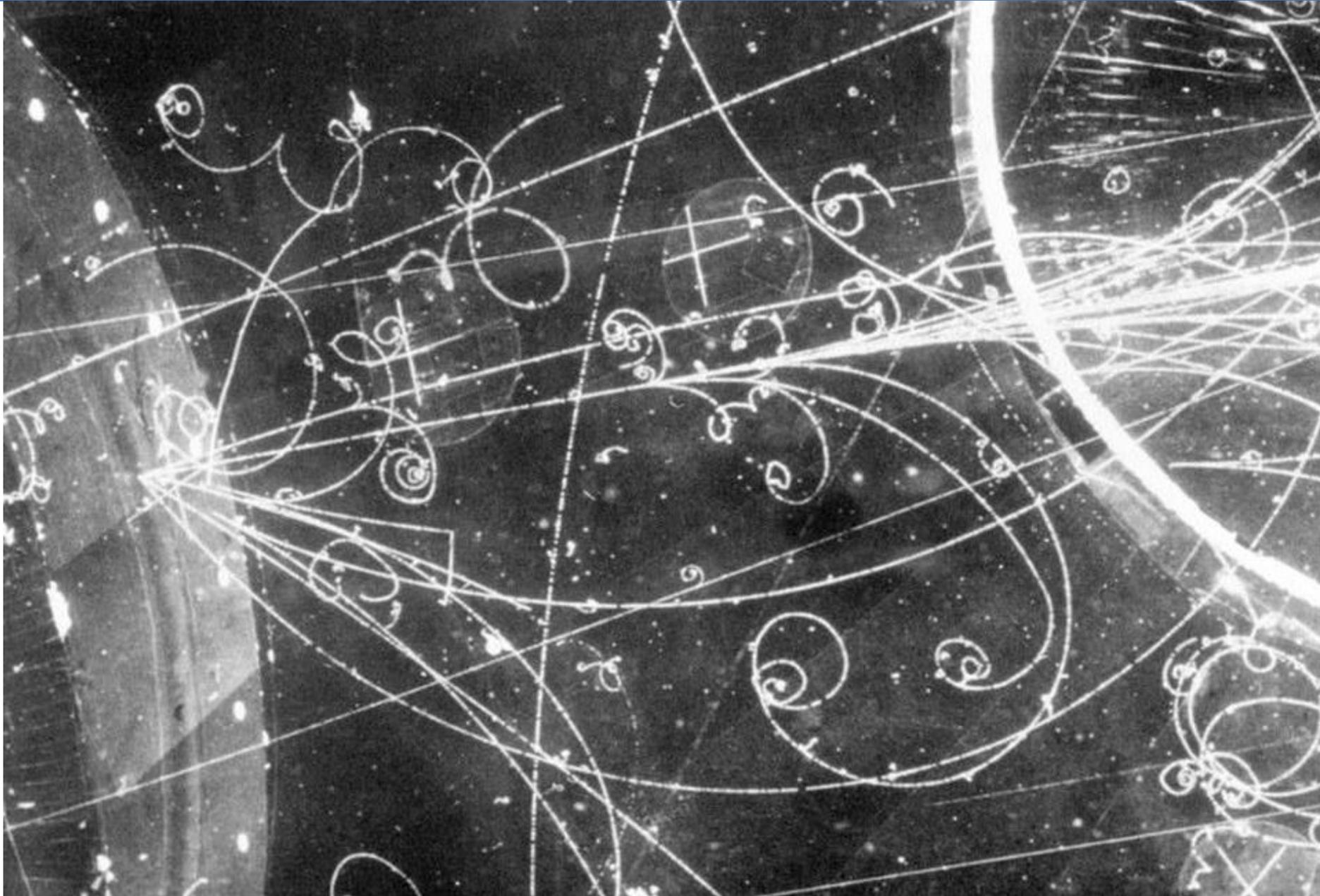
Literature belonging to the lectures:

- Griffiths: “Introduction to Elementary Particles”
- Lecture notes PP1 master course from Nikhef:
<https://www.nikhef.nl/~i93/Master/PP1/2017/Lectures/Lecture2017.pdf>

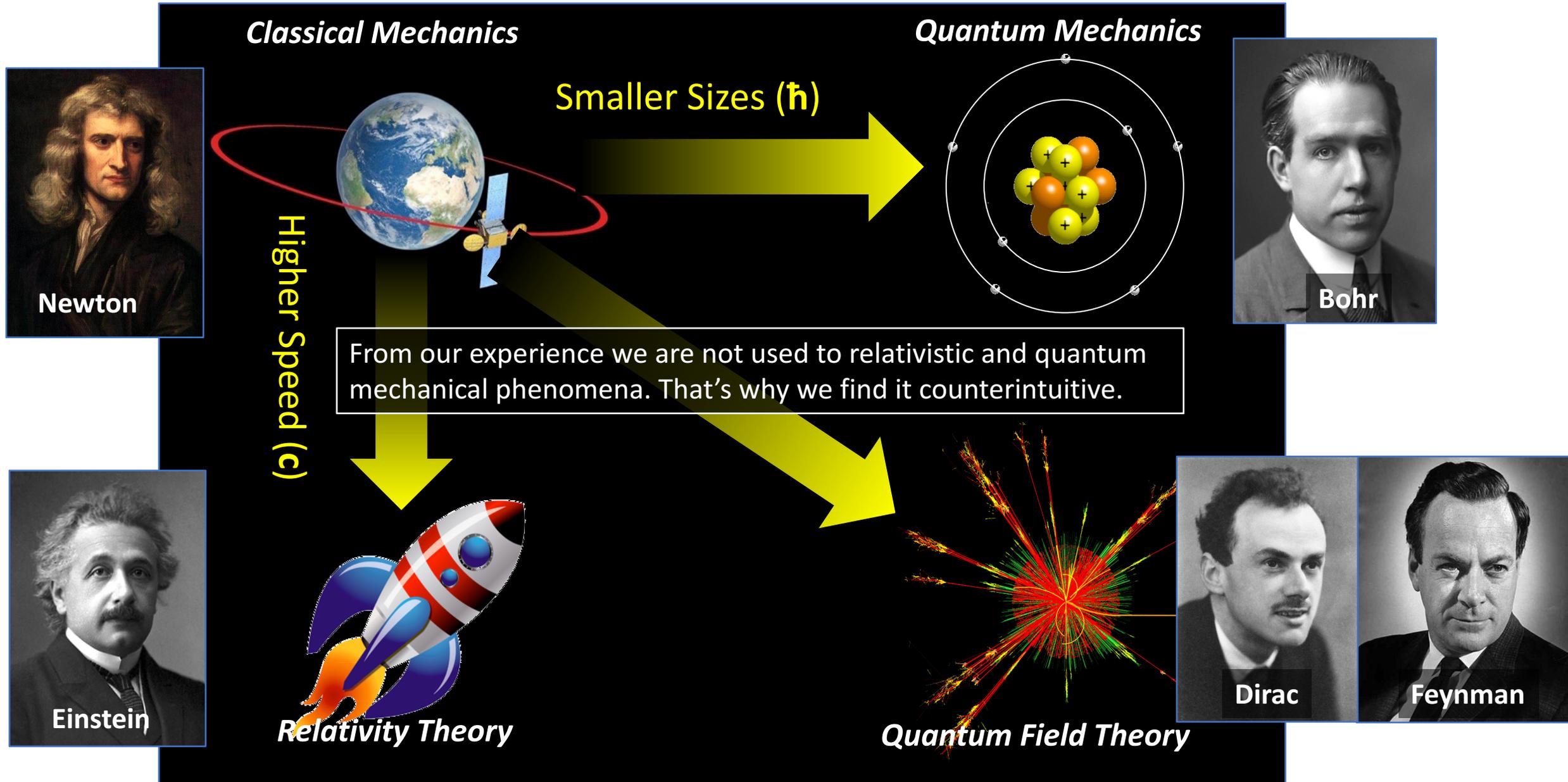
Other good books:

- Mark Thomson: “Modern Particle Physics”
- Halzen and Martin: “Quarks & Leptons: An Introductory Course in Modern Particle Physics”
- Aitchison and Hey: “Gauge Theories in Particle Physics” – 2 volumes

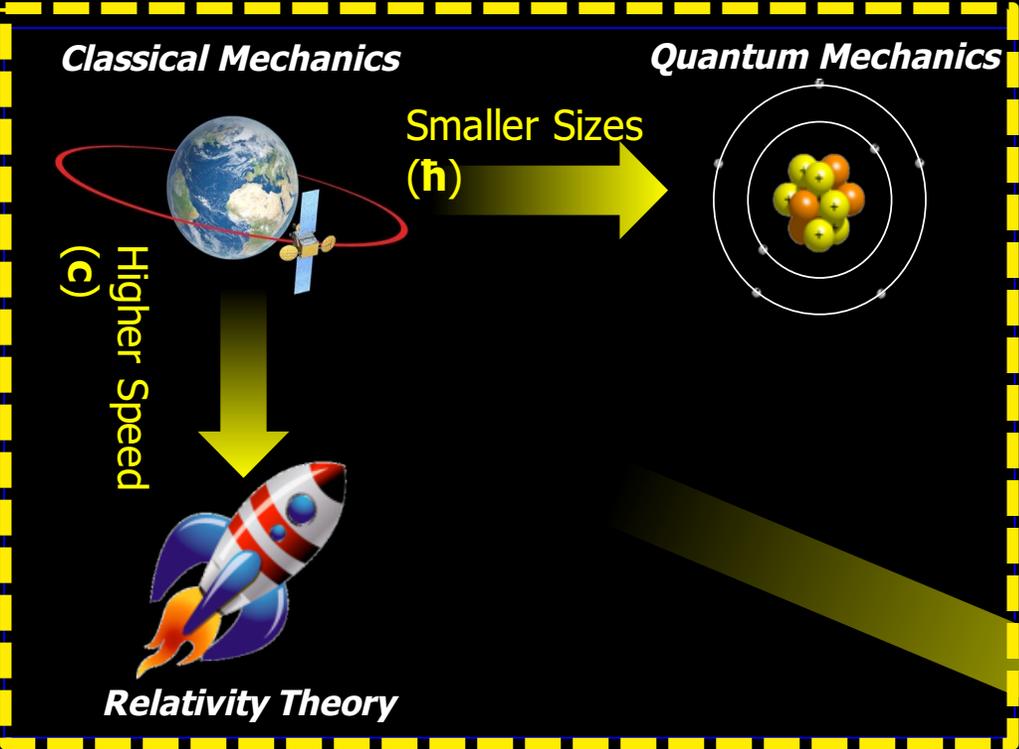
Lecture 1: "Particles"



Tools: Relativity and Quantum Mechanics



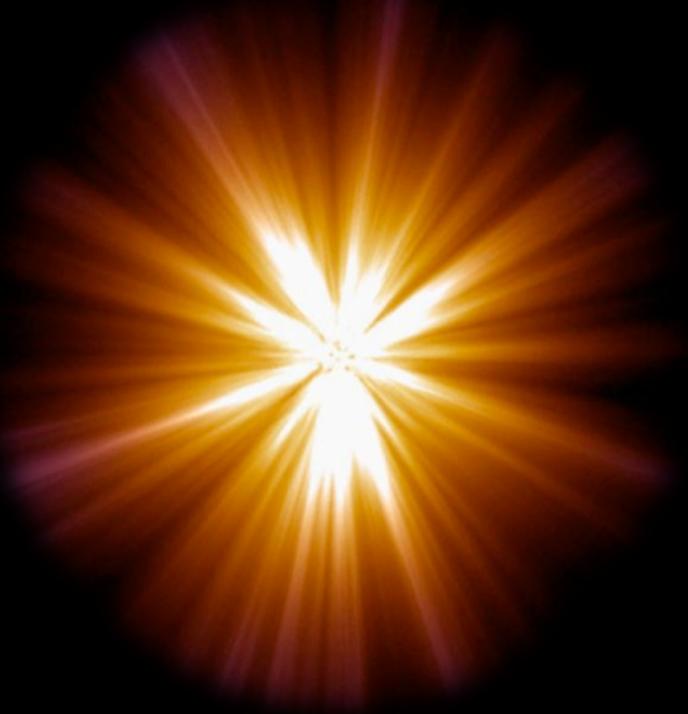
How does nature behave in extreme conditions?



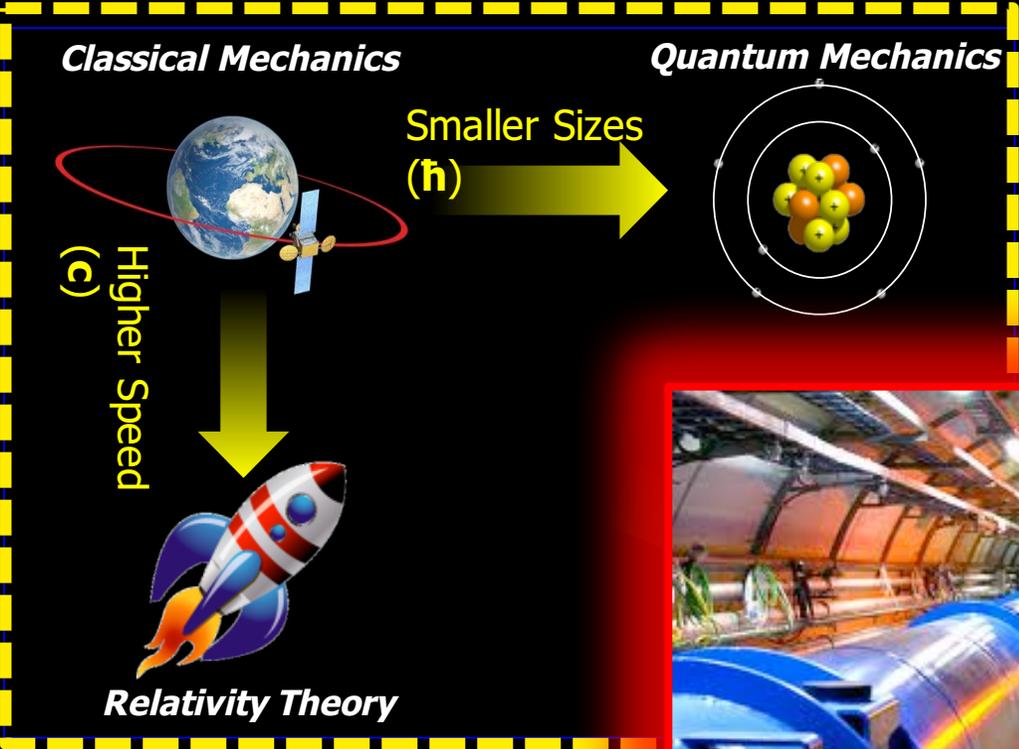
← Experimentally tested domain of the Standard Model

Big Bang

↑ ↑
← Do we understand the physics also here? →



How does nature behave in extreme conditions?

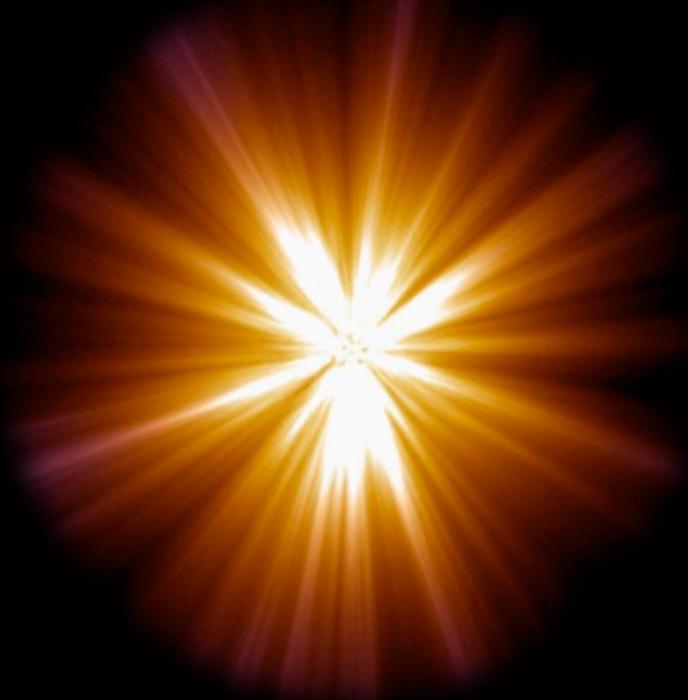


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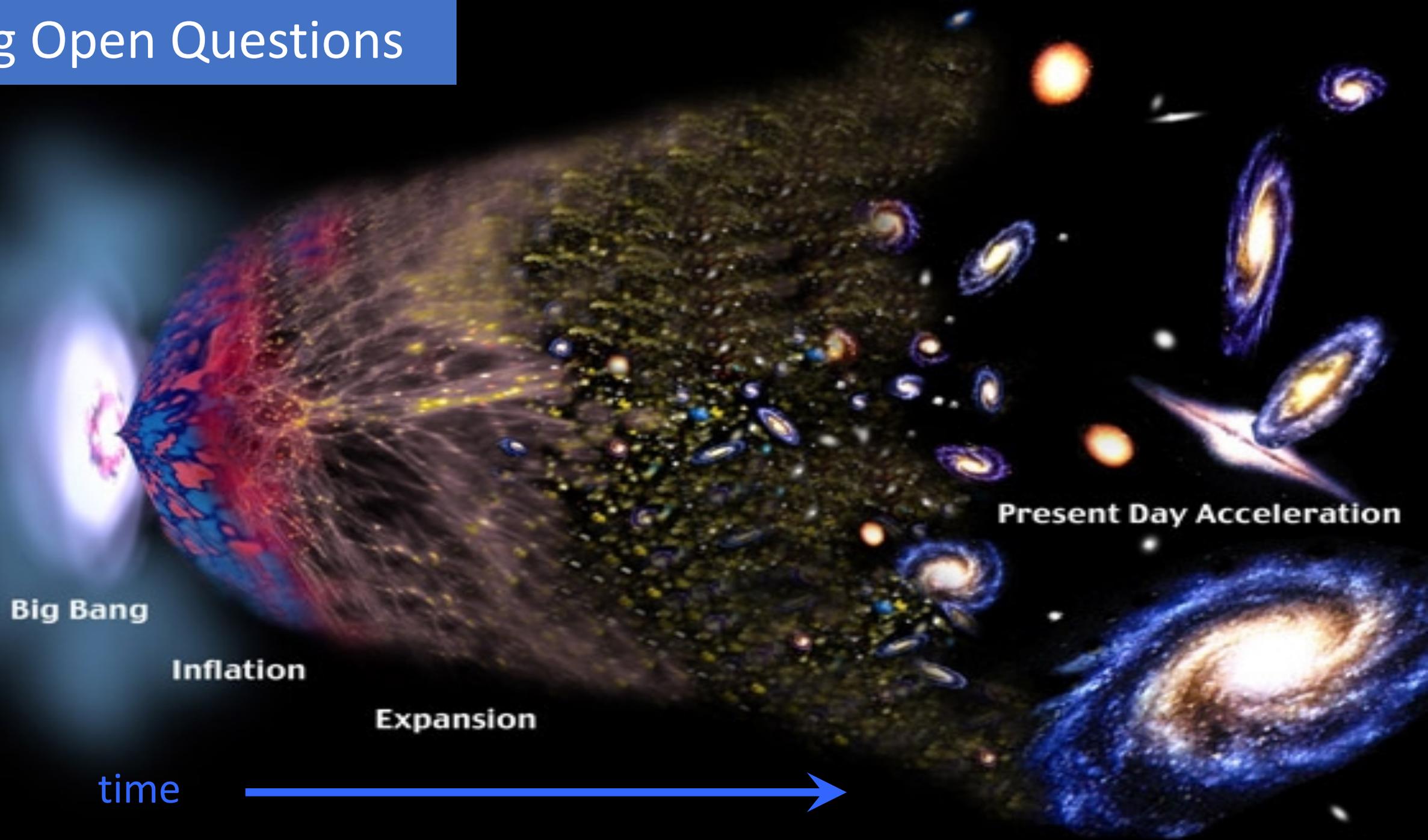


The Large Hadron Collider

Big Bang



Big Open Questions



Big Bang

Inflation

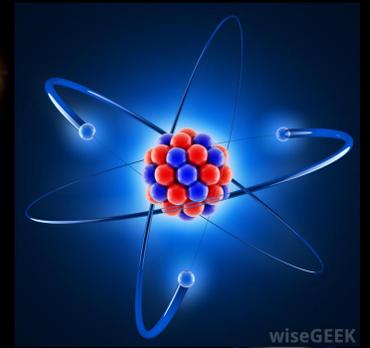
Expansion

time

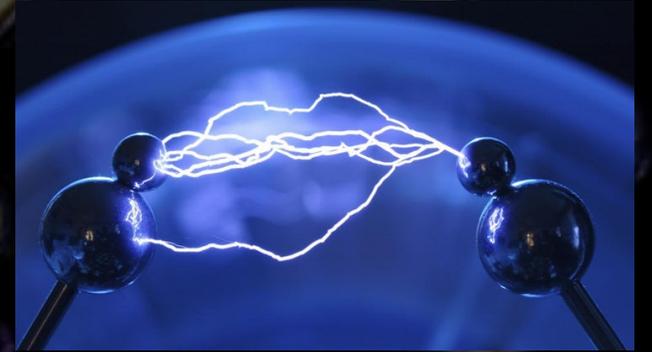
Present Day Acceleration

Big Open Questions

1. Which are the elementary **building blocks** of matter?



2. Which **forces** exist in nature and what are their essential differences?



3. Is **empty space** ('the vacuum') truly empty?

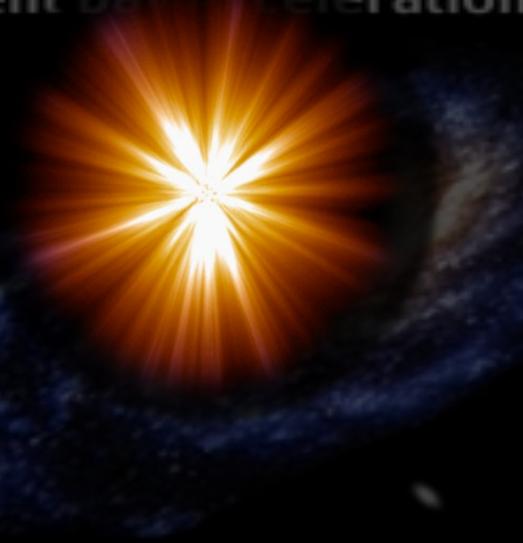
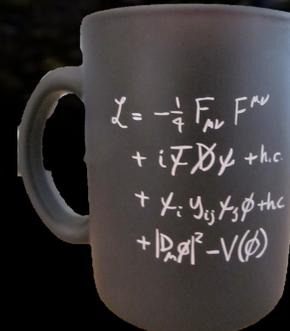
Present Day Acceleration

4. Can we explain the existence of **our universe** from the *big bang* using the known laws of nature?

Big Bang

Inflation

- *Wanted: a consistent theory that can answer these questions*

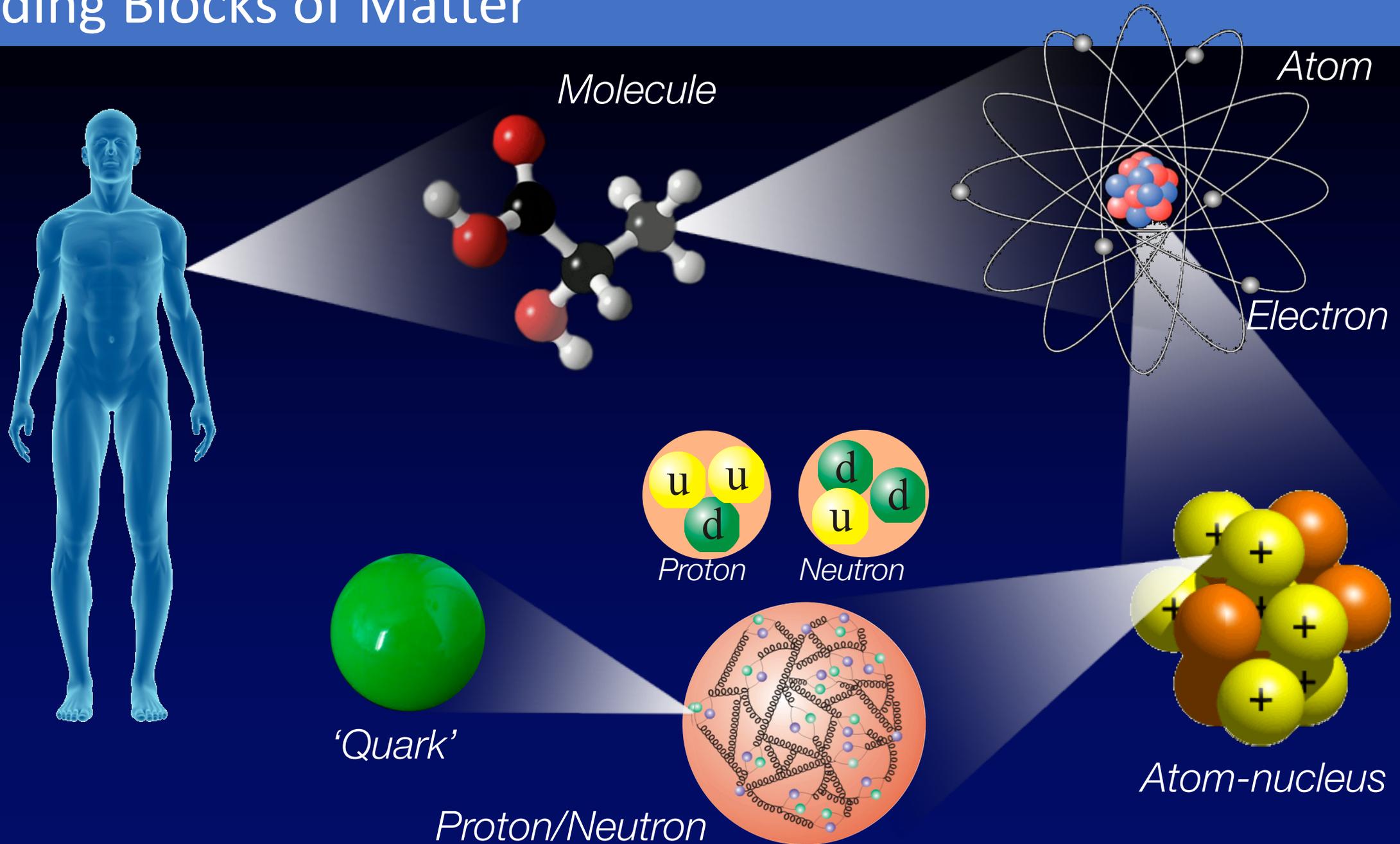


Lecture 1: Particles

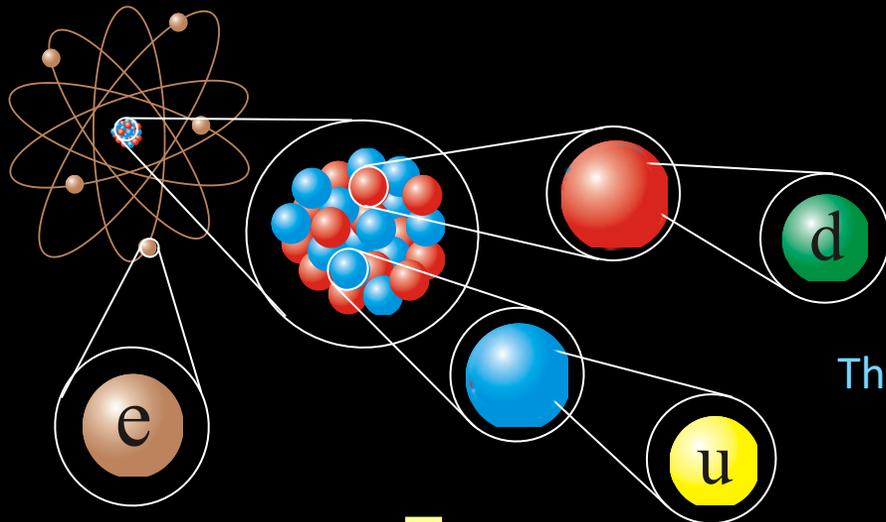
Part 1

The Structure of Matter (Nuclear Physics)

Building Blocks of Matter



Stable Matter on Earth



The Lego blocks of nature

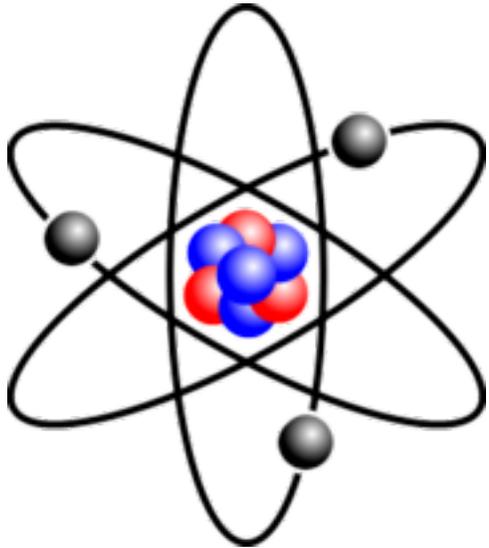
↓

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| | 1 1a | | | | | | | | | | | | | | | | | 18 0 | |
| 1 | 1 H | 2 He | | | | | | | | | | | | | | | | | |
| 2 | 3 Li | 4 Be | | | | | | | | | | | | | | | | | |
| 3 | 11 Na | 12 Mg | 3 B | 4 C | 5 N | 6 O | 7 F | 8 Ne | | | | | | | | | | | |
| 4 | 19 K | 20 Ca | 21 Sc | 22 Ti | 23 V | 24 Cr | 25 Mn | 26 Fe | 27 Co | 28 Ni | 29 Cu | 30 Zn | 31 Ga | 32 Ge | 33 As | 34 Se | 35 Br | 36 Kr | |
| 5 | 37 Rb | 38 Sr | 39 Y | 40 Zr | 41 Nb | 42 Mo | (43) Tc | 44 Ru | 45 Rh | 46 Pd | 47 Ag | 48 Cd | 49 In | 50 Sn | 51 Sb | 52 Te | 53 I | 54 Xe | |
| 6 | 55 Cs | 56 Ba | · | 72 Hf | 73 Ta | 74 W | 75 Re | 76 Os | 77 Ir | 78 Pt | 79 Au | 80 Hg | 81 Tl | 82 Pb | 83 Bi | 84 Po | 85 At | 86 Rn | |
| 7 | 87 Fr | 88 Ra | · | (104) Rf | (105) Db | (106) Sg | (107) Bh | (108) Hs | (109) Mt | (110) Ds | (111) Rg | (112) Cn | (113) Uut | (114) Fl | (115) Uup | (116) Lv | (117) Uus | (118) Uuo | |
| 1a | Lanthaniden | | 57 La | 58 Ce | 59 Pr | 60 Nd | (61) Pm | 62 Sm | 63 Eu | 64 Gd | 65 Tb | 66 Dy | 67 Ho | 68 Er | 69 Tm | 70 Yb | 71 Lu | | |
| 2a | Actiniden | | 89 Ac | 90 Th | 91 Pa | 92 U | (93) Np | (94) Pu | (95) Am | (96) Cm | (97) Bk | (98) Cf | (99) Es | (100) Fm | (101) Md | (102) No | (103) Lr | | |



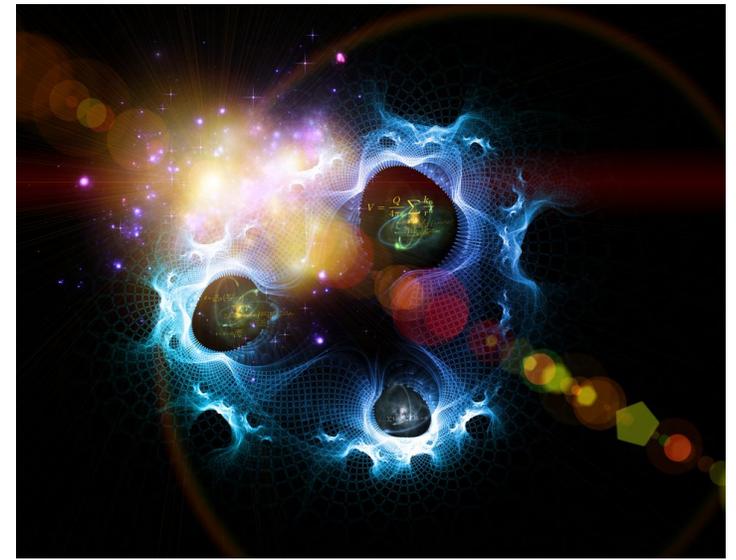
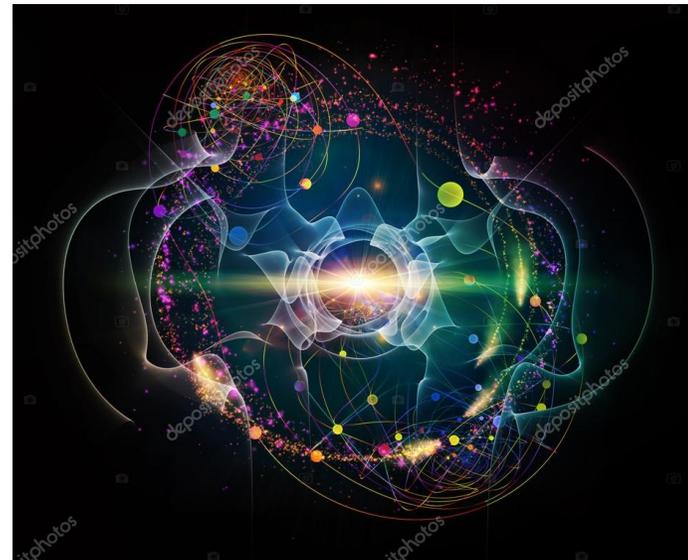
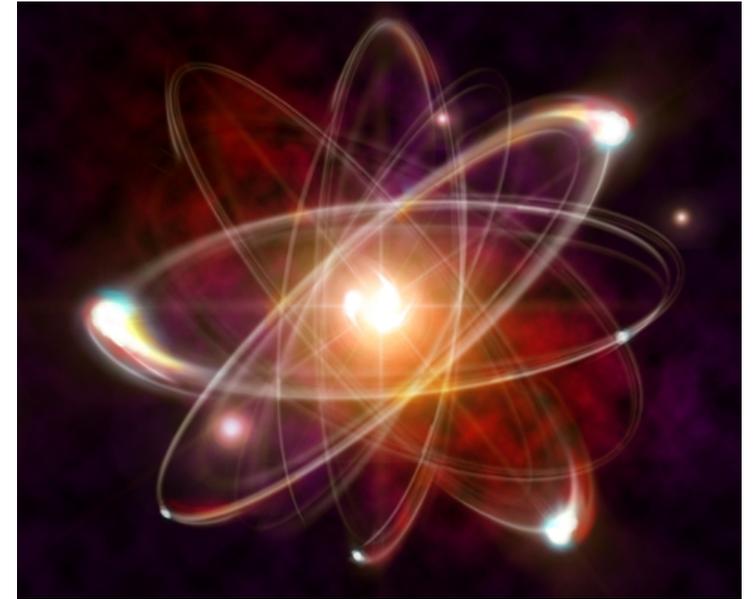
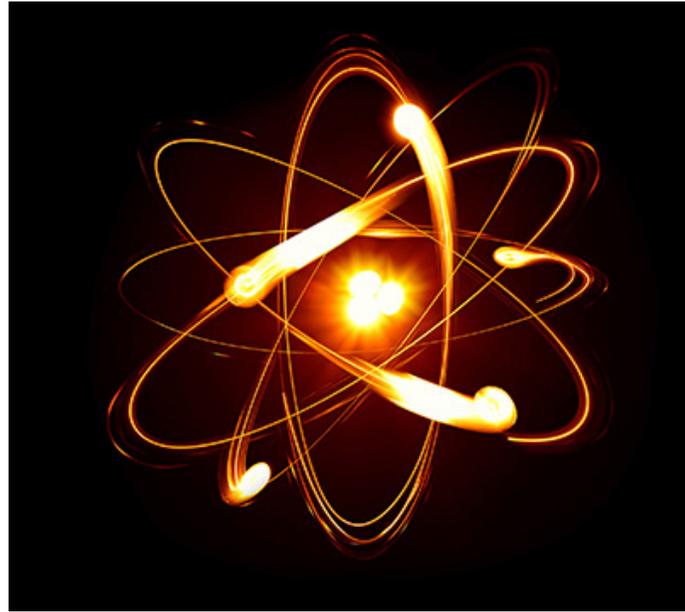
Exercise-1: Which mental picture do you make of an atom?

Classic picture of the atom



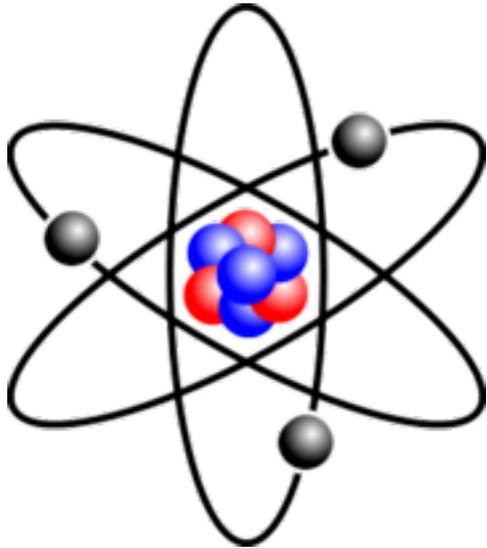
- Does something “move”?
- How empty is it?
- How does an electron “exist”?

➔ Consider QM interpretations



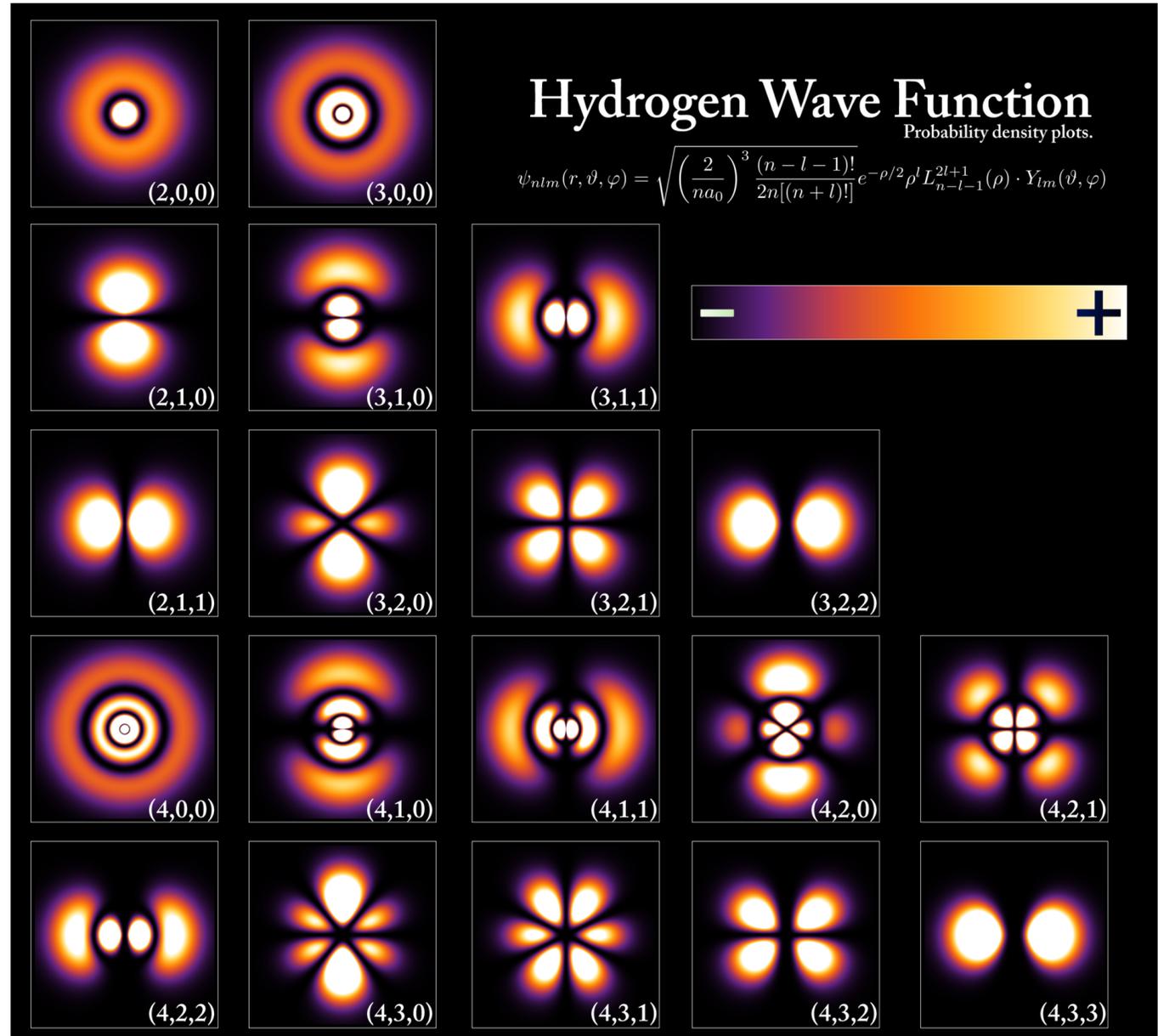
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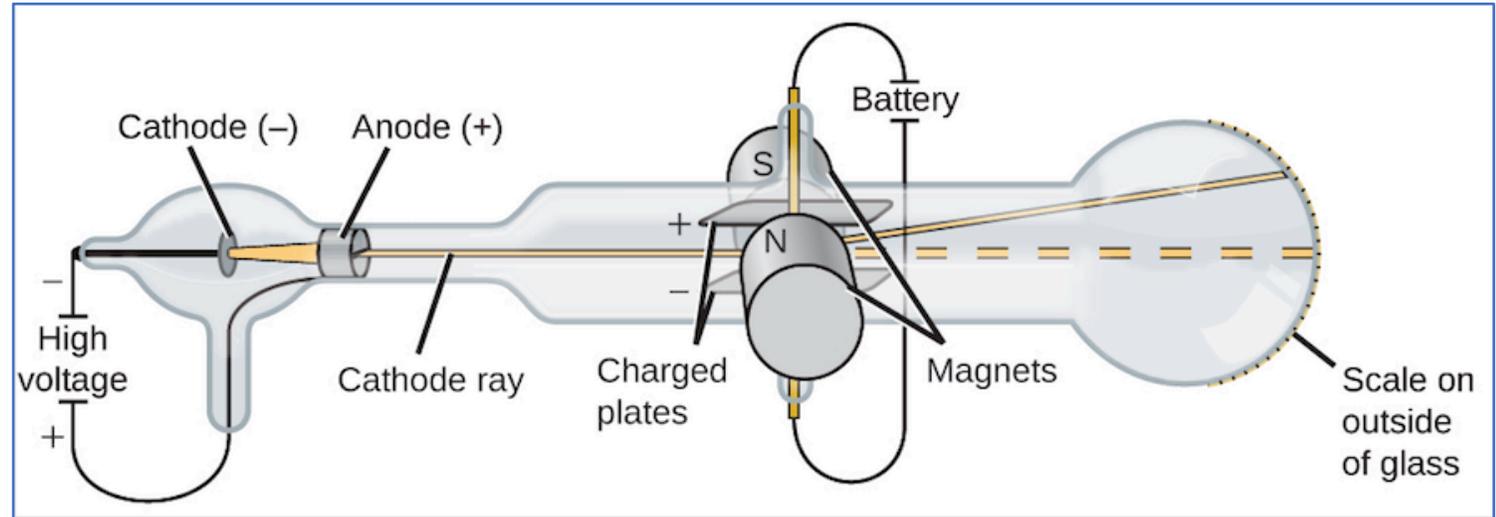
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➔ Consider QM interpretations



Discovery of the Electron

- JJ Thomson (1897):
Cathode rays are bent by electric and magnetic field
- Charged particles



1. Compensate Electric and magnetic deflection:

$$F_E = F_B$$

$$qE = qvB ; v = E/B$$

2. Only B-field, cycle orbit:

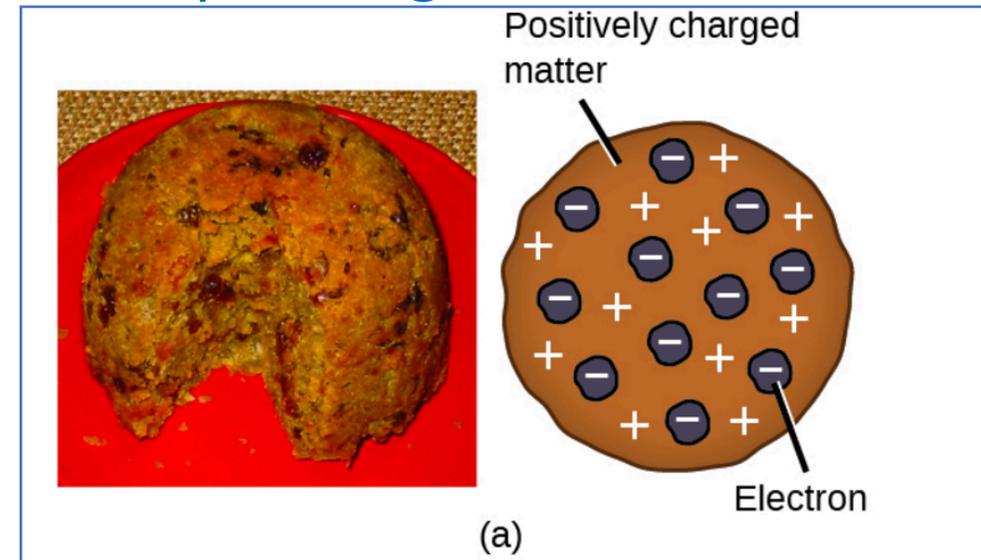
$$F_c = F_B$$

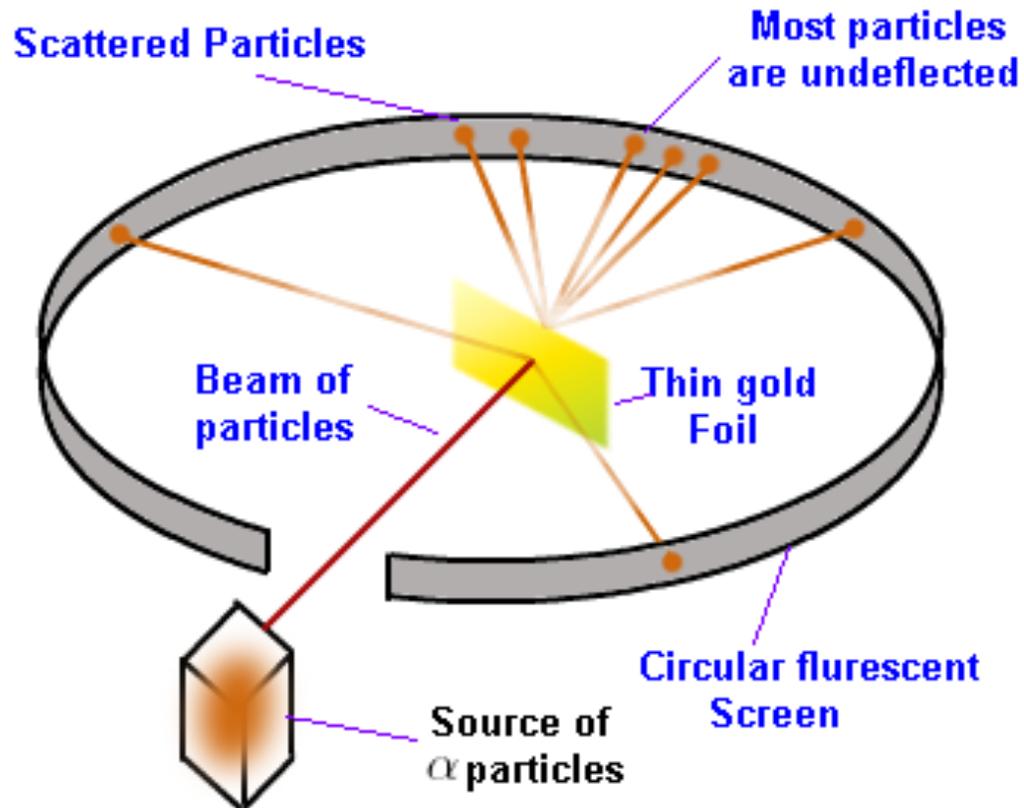
$$\frac{mv^2}{r} = qvB$$

$$\frac{q}{m} = \frac{E}{rB^2}$$

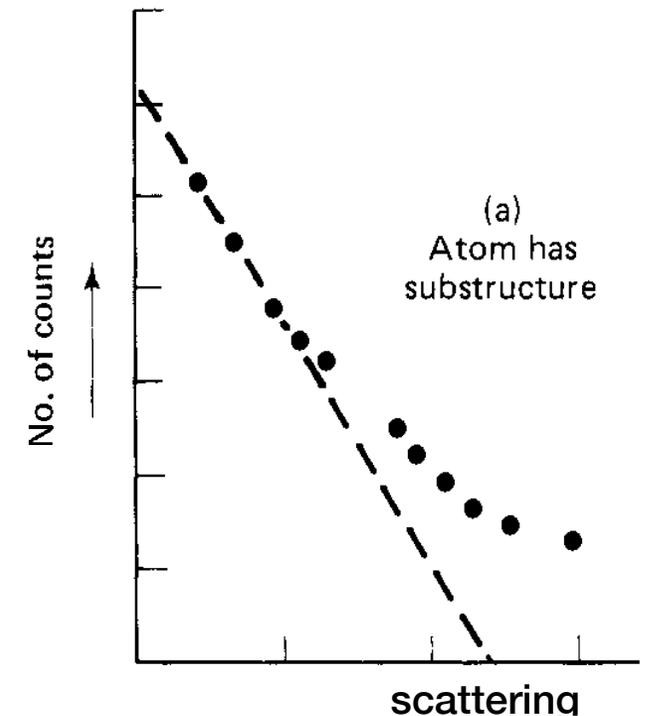
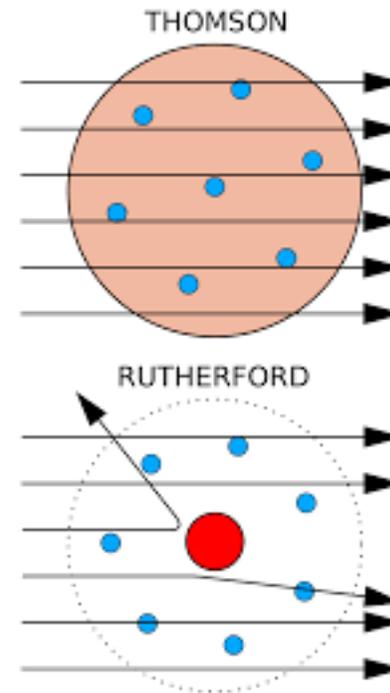
Electrons are much lighter than ions of same charge!

- Plum-pudding model of atoms:





- Rutherford (1911)
 - α -particles at gold target
 - Most particles pass undisturbed, few have a “hard” collision
 - Atom has substructure: small heavy nucleus



- Atom is basically just vacuum:
 - Atom size: $\sim 10^{-10} m$
 - Nucleus size: $\sim 10^{-15} m$

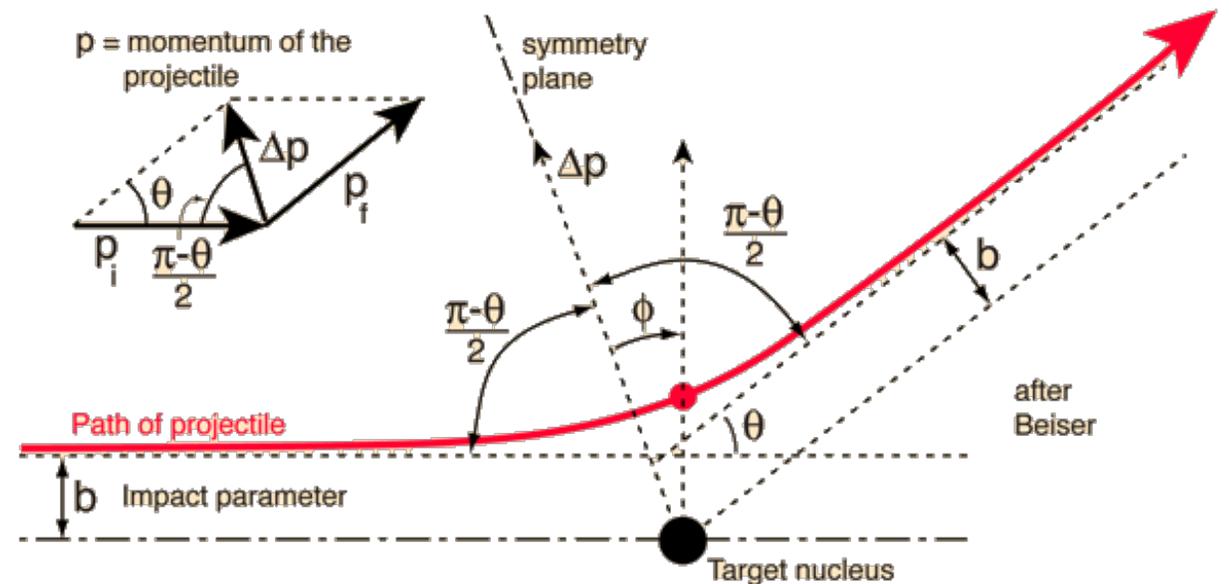
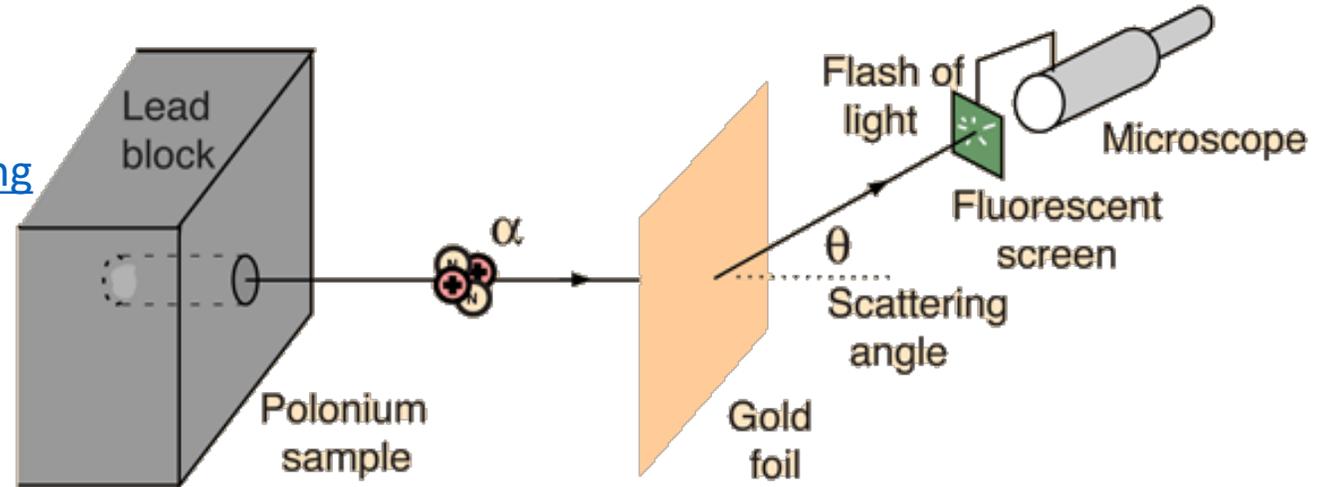
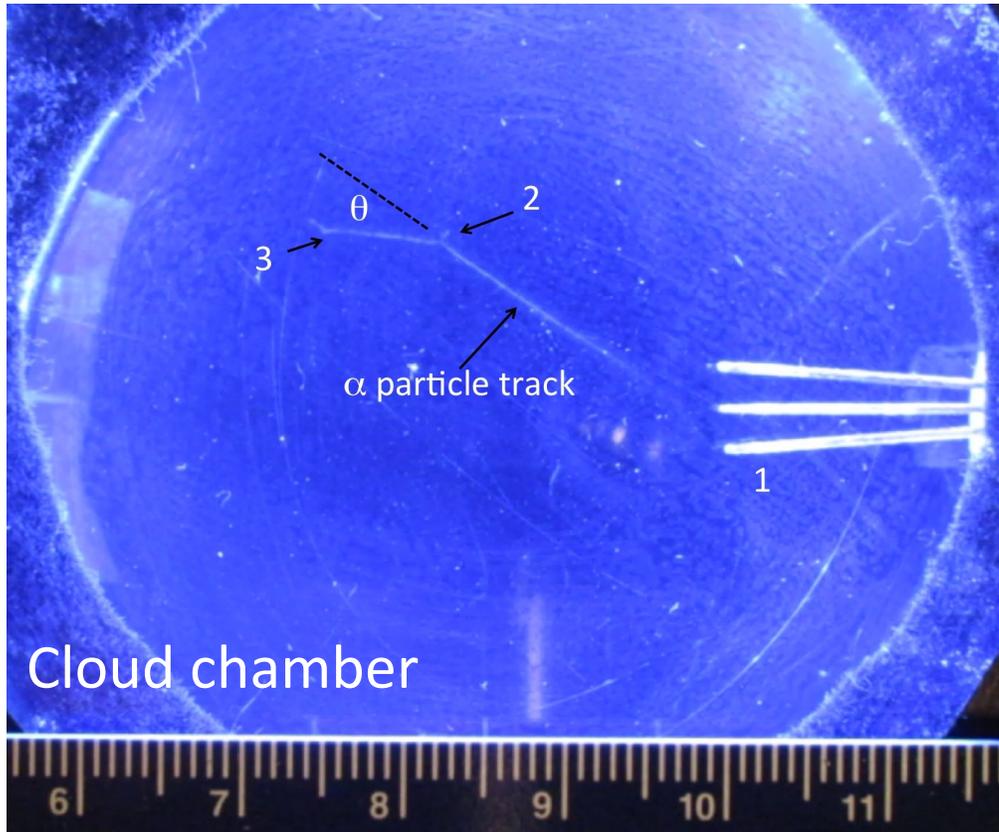
Example Rutherford scattering

- Rutherford scattering

- Formula derivation:

- https://en.wikipedia.org/wiki/Rutherford_scattering

- → not required



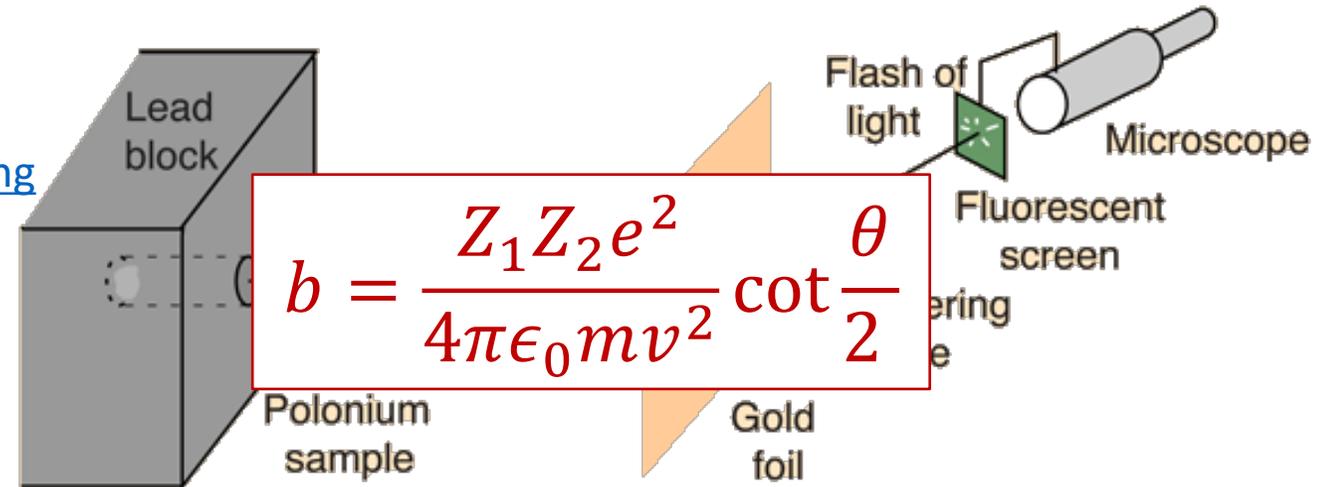
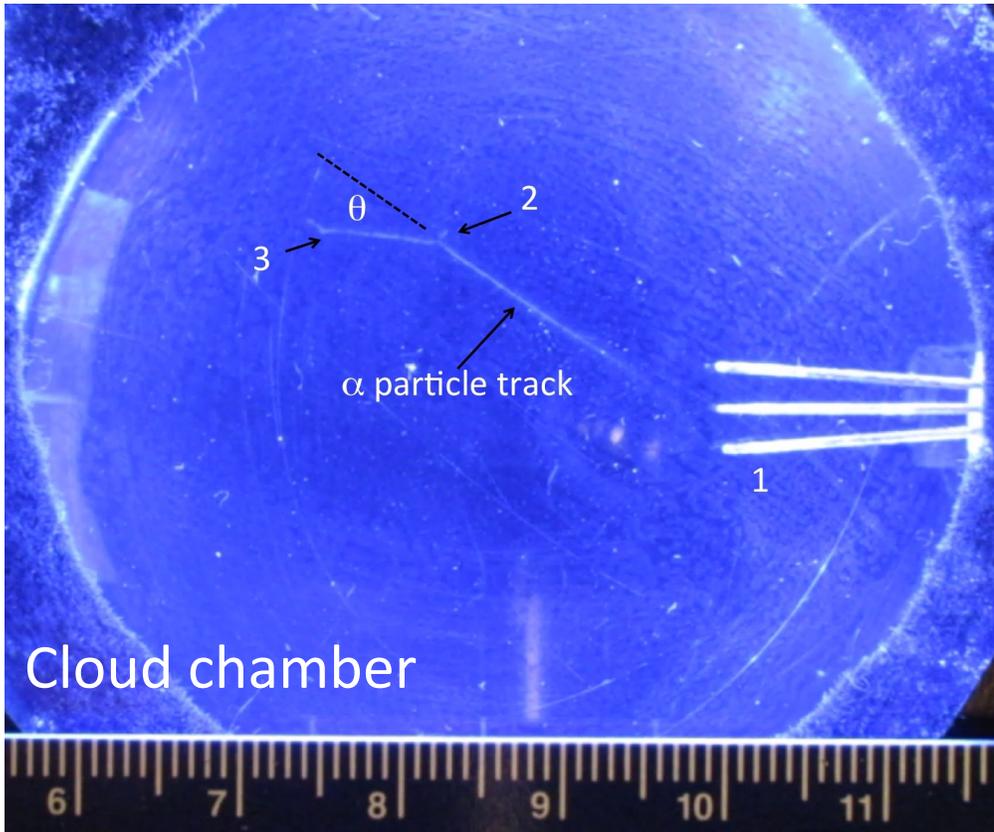
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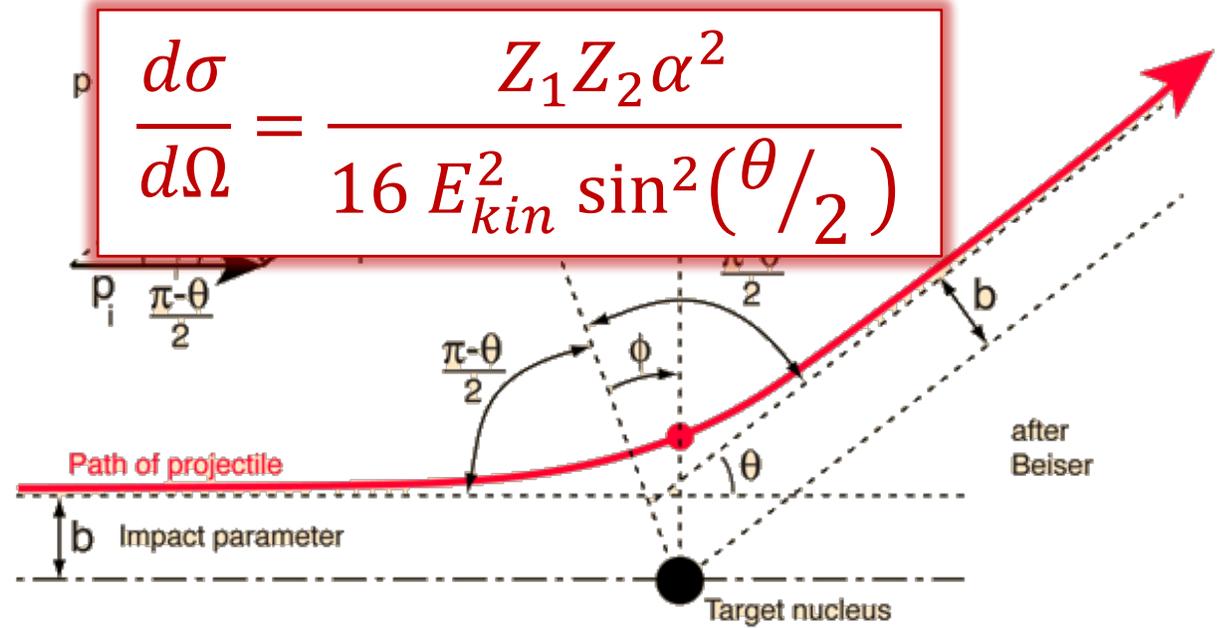
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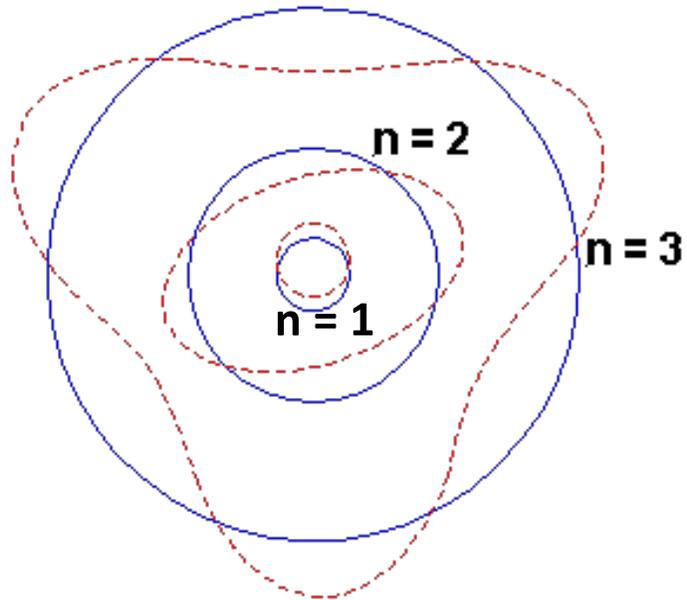


$$b = \frac{Z_1 Z_2 e^2}{4\pi\epsilon_0 m v^2} \cot \frac{\theta}{2}$$

$$\frac{d\sigma}{d\Omega} = \frac{Z_1 Z_2 \alpha^2}{16 E_{kin}^2 \sin^2(\theta/2)}$$

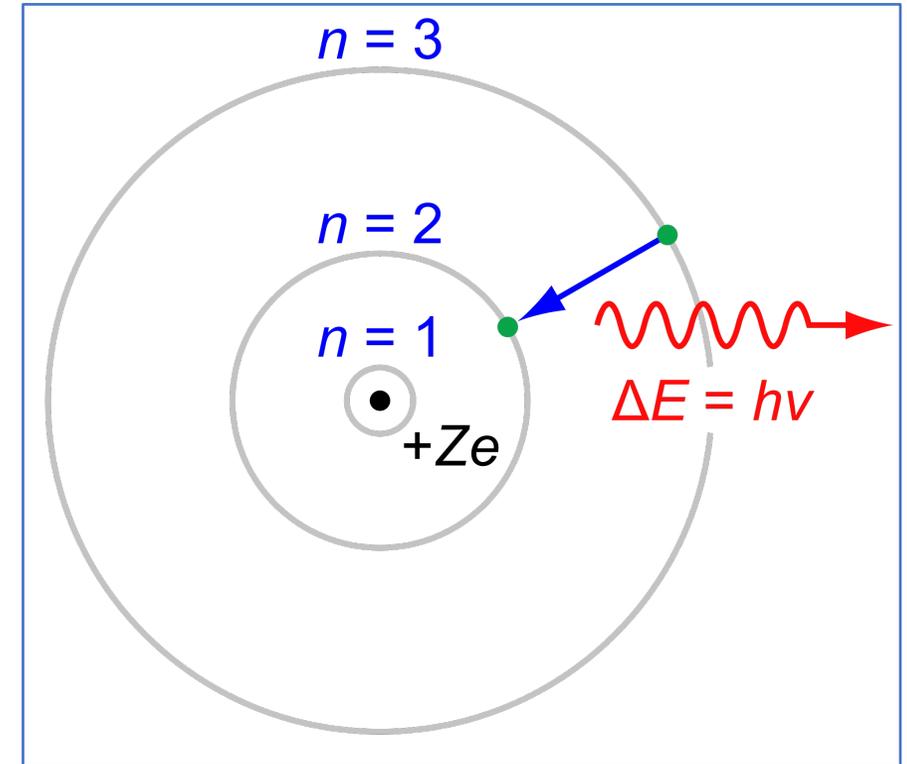


- Niels Bohr, 1914:
 - Calculate atomic energy levels using semi classical method

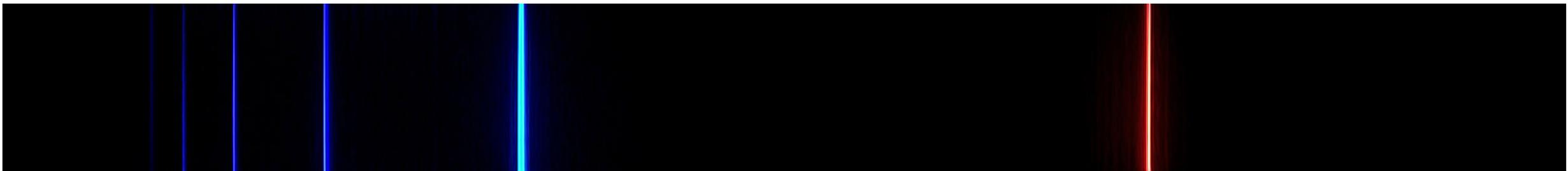


de Broglie: $\lambda = h / p$

$$\begin{aligned} L &= r p \\ L &= r h / \lambda \\ L &= r n h / (2 \pi r) \\ L &= n h / (2\pi) = n \hbar \end{aligned}$$



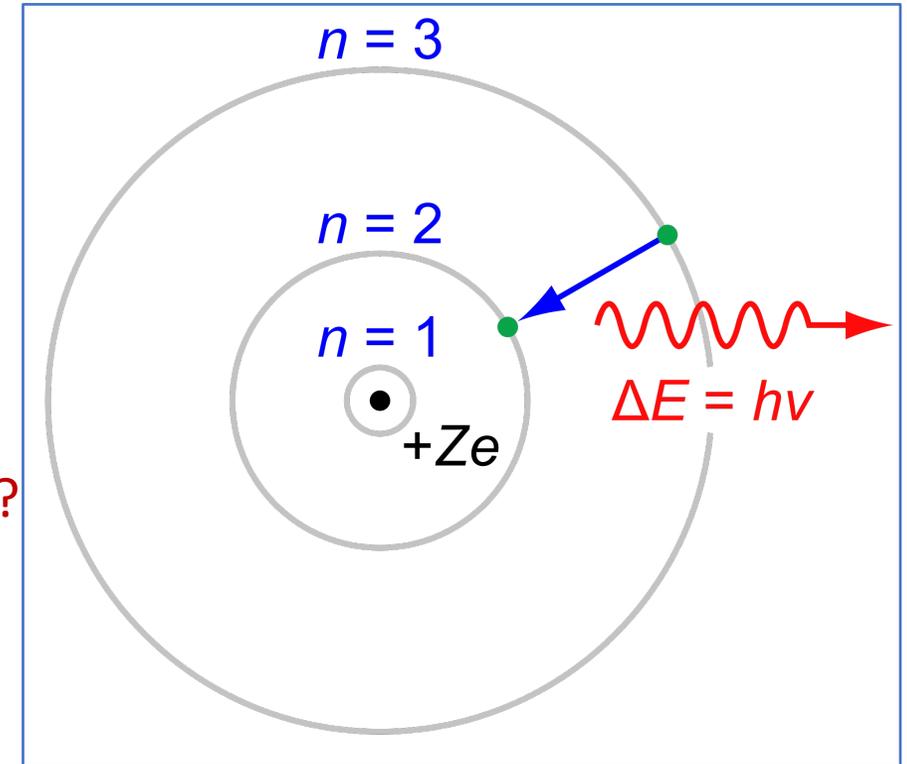
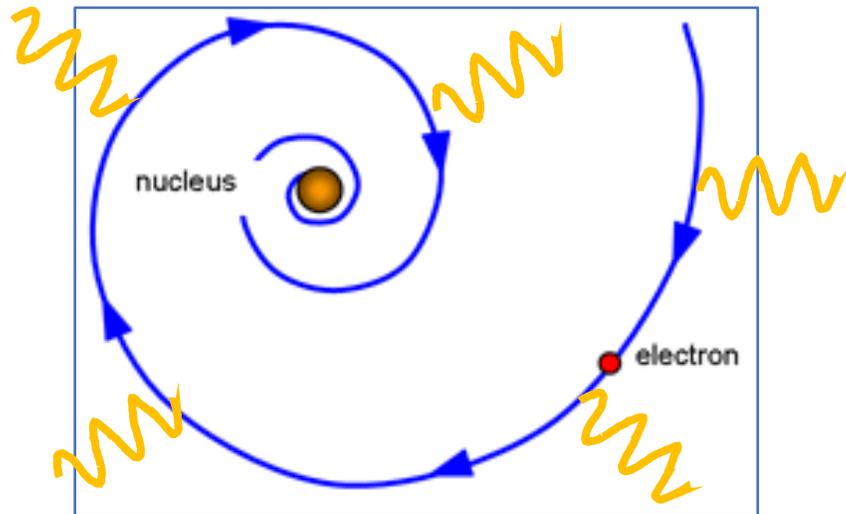
- Balmer spectrum of visible wavelengths in hydrogen:



- Niels Bohr, 1914:
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Exercise-2 “Pub Quiz”:

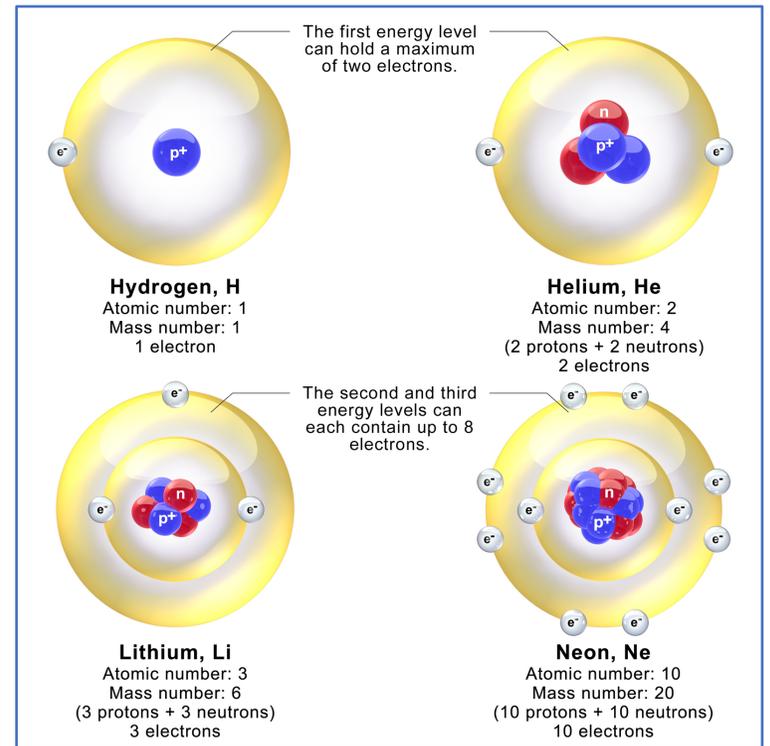
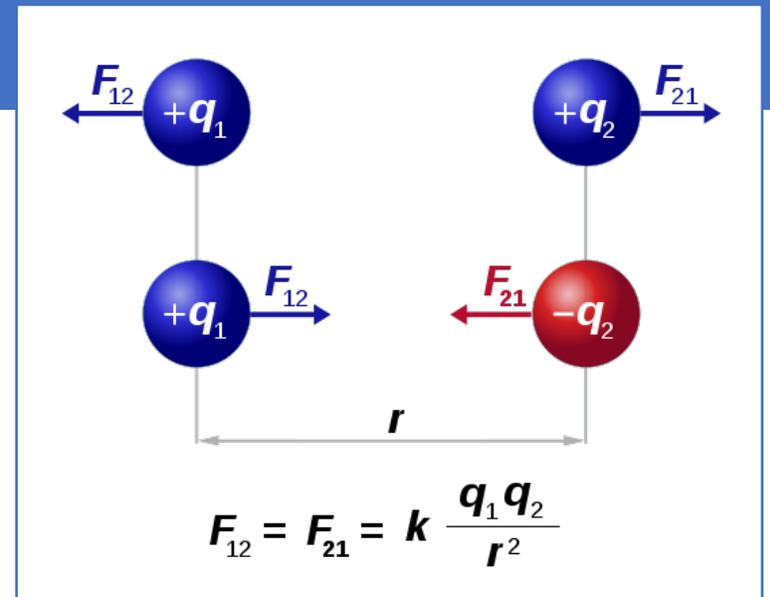
- 1: How come an atom is stable?
- 2: What hits each other when you clap your hands?
- 3: Why does a hydrogen electron not interact with the proton?



?

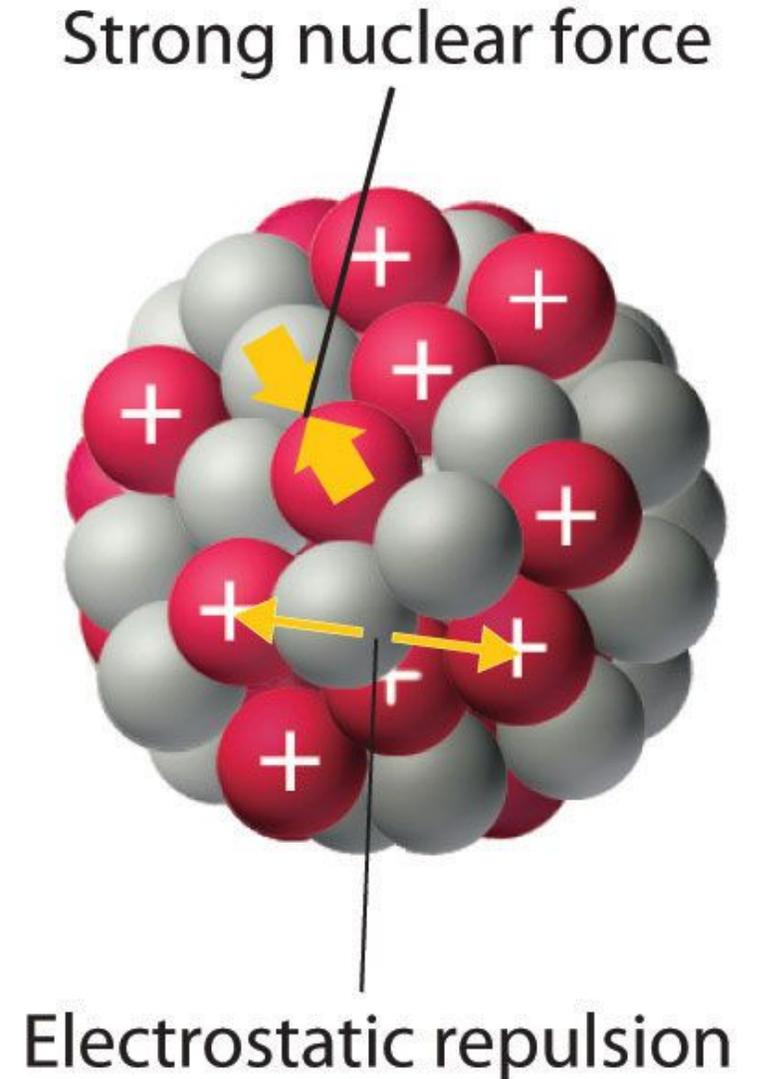
Nuclear Physics

- Nuclei include protons, p
 - Masses of nuclei studies in chemistry (Avogadro)
 - Hydrogen = 1 proton: $M_H = 1 \text{ GeV}/c^2 = 200 M_e$
- Study q/m of nuclei:
 - Masses of nuclei do not scale with charge, but with $A \approx 2 \times Z$
 - A = mass number, Z = atomic number = nucleus charge
 - What keeps heavy nuclei together?
- Chadwick 1932: Discovery of neutron, n
 - Neutron has almost same mass as proton
 - Neutrons act as a glue to nucleons in the nucleus
 - Later we will see it is due to the gluon color force
- Notation: ${}^A_Z\text{MyAtom}$, with $Z = \#p$, $A = \#(p + n)$
 - Isotopes: same $\#p$, different $\#n$



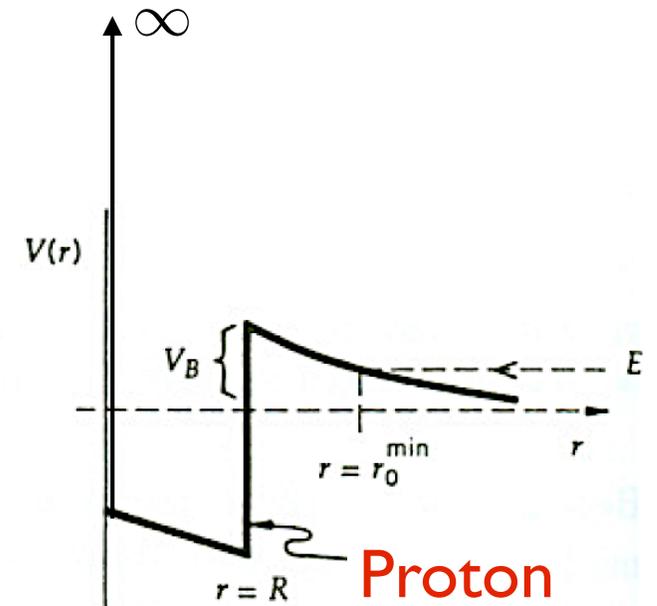
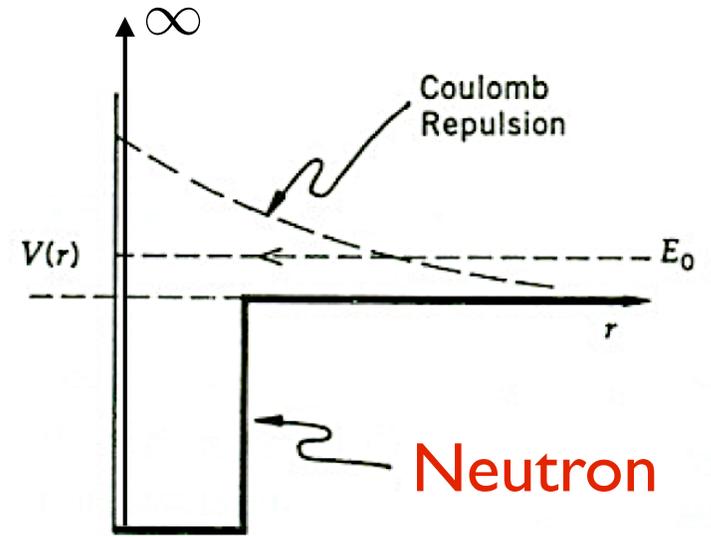
Electric Force vs Nuclear Force

- Electric Force: inverse square law
 - Generated by exchange of massless photon quanta
- Nuclear Force
 - must be (much) stronger than electric force in the nucleus
 - must be (much) weaker than electric force outside the nucleus
- Pauli exclusion principle: Two fermions (protons, neutrons) cannot be at the same position
 - The potential must have a very strong repulsive core at small r
- Potential square well model
 - For protons there is a “Coulomb barrier” V_B
 - Beyond the range R it is negligible
 - With Rutherford scattering the range can be determined
 - $R \propto A^{1/3}$
- Nuclear force generated by exchange of massive pion



Electric Force vs Nuclear Force

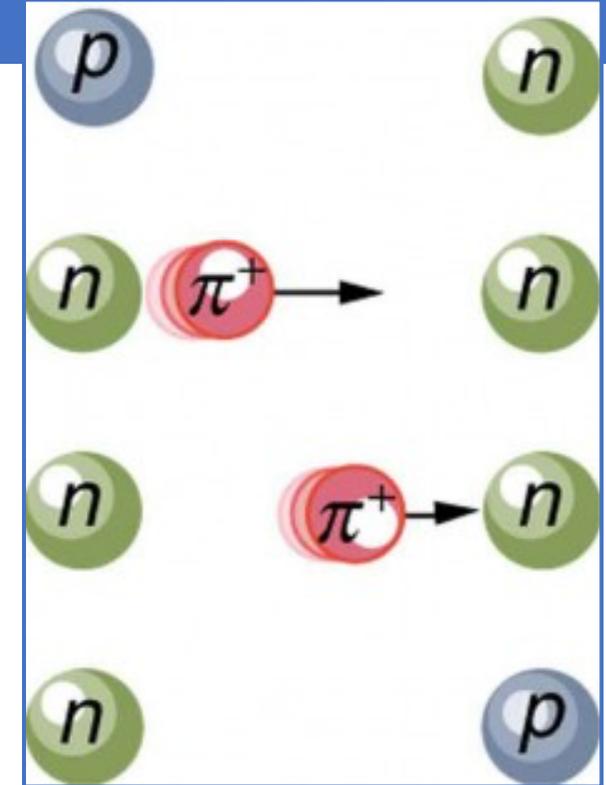
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Yukawa's pion

Griffiths: problem 1.2, PP1 §i.2

- Yukawa (1934) pi-meson gives attractive force between nucleons
- Heisenberg operator uncertainty in QM: $\Delta E \Delta t \geq \frac{\hbar}{2}$
- Translated to popular language:
 - You can violate energy conservation as long as:
 - time is shorter than: $\Delta t \leq \frac{\hbar}{2\Delta E}$ or energy is less than $\Delta E \leq \frac{\hbar}{2\Delta t}$
- Electromagnetic force is transmitted by photon quanta
 - $E = hf = \frac{hc}{\lambda}$ such that: $\Delta t \sim \frac{\lambda}{c}$ and the range $R \sim c\Delta t = \lambda$ is infinite
- Nuclear (“strong”) force is transmitted by massive pions:
 - $E = mc^2$ such that $\Delta t \sim \frac{\hbar}{2mc^2}$ and $R \sim c\Delta t = \frac{\hbar}{2mc}$
 - The heavier the particle, the more difficult to “violate energy conservation”, the shorter the range
- In 1937 a particle with the correct mass was found in cosmic rays, but it did not interact with nuclei!
 - “Who ordered that?” (Isidor Rabi). It was the muon.
- In 1947 the pion was discovered



Exercise-2 : The Yukawa Potential

- The electric force is transmitted by a photon with $m = 0$. The wave equation for a static electric field caused by pointlike charge e is: $\nabla^2 V(r) = 0$ (Laplace equation)
 - a) Show that the Coulomb potential $V(r) = -e^2 \frac{1}{r}$ fulfills this equation.
 - Note that the potential is **spherical symmetric**, ie. use spherical coordinates.
- The nuclear force is transmitted by a pi-meson with $m = m_\pi$. The wave equation for a static nuclear field caused by a pointlike color charge g is: $\nabla^2 U(r) = m^2 U(r)$ (Klein-Gordon equation)
 - b) Show that the Yukawa potential $U(r) = -g^2 \frac{e^{-r/R}}{r}$ fulfills this equation for a certain value of R , the **range** of the force. What is the relation between R and m_π ?
 - Again note that the potential is **spherical symmetric**.
 - This value is between the electron and proton mass, hence the particle was called a pi-meson or pion.
 - c) Calculate the range of the force from Heisenberg's uncertainty relation, using $R = c\Delta t$ and $\Delta E \Delta t \leq \frac{\hbar}{2}$ and $\Delta E = mc^2$.
 - d) The weak force is mediated by W (80 GeV) and Z (91 GeV) bosons. What is the estimated range of the weak force?

The nucleon-nucleon potential

- Woods Saxon Potential, 1954

- $V(r) = -\frac{V_0}{1+\exp\left(\frac{r-R}{a}\right)}$

- Nuclear Radius: $R = 1.25 \text{ fm} \times A^{1/3}$
 A is mass number, $V_0 \approx 50 \text{ MeV}$, $a \approx 0.5 \text{ fm}$

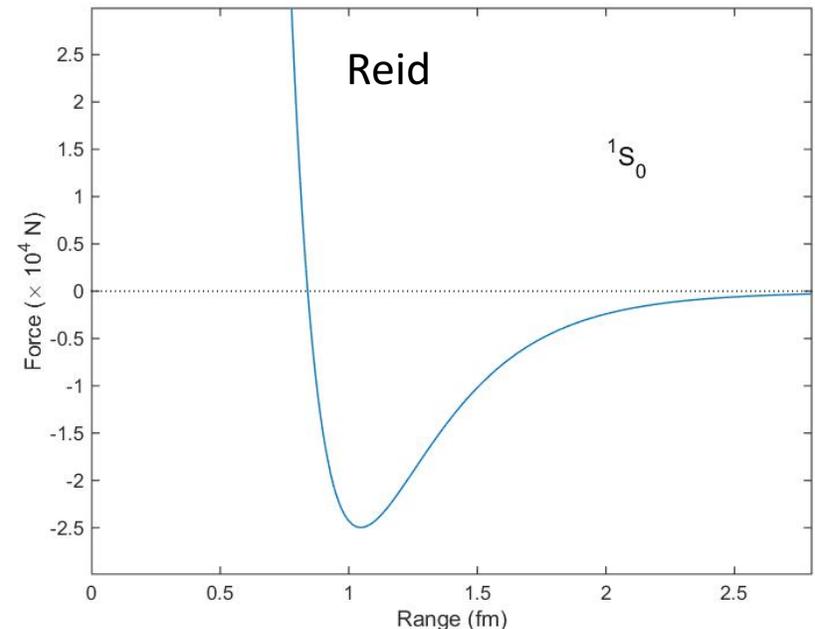
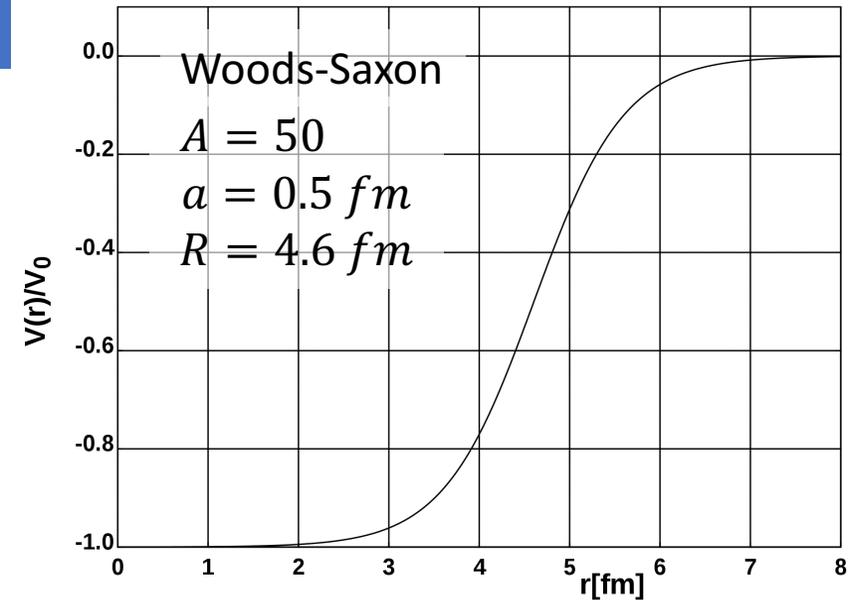
- Many models in 1970 – 1990

- Reid Potential, 1968, (semi-empirical) implements repulsive core:

- $V_{Reid}(R) = -10.463 \frac{e^{-\mu r}}{\mu r} - 1650.6 \frac{e^{-4\mu r}}{\mu r} + 6482.2 \frac{e^{-7\mu r}}{\mu r}$
in MeV with $\mu = 0.7 \text{ fm}^{-1}$

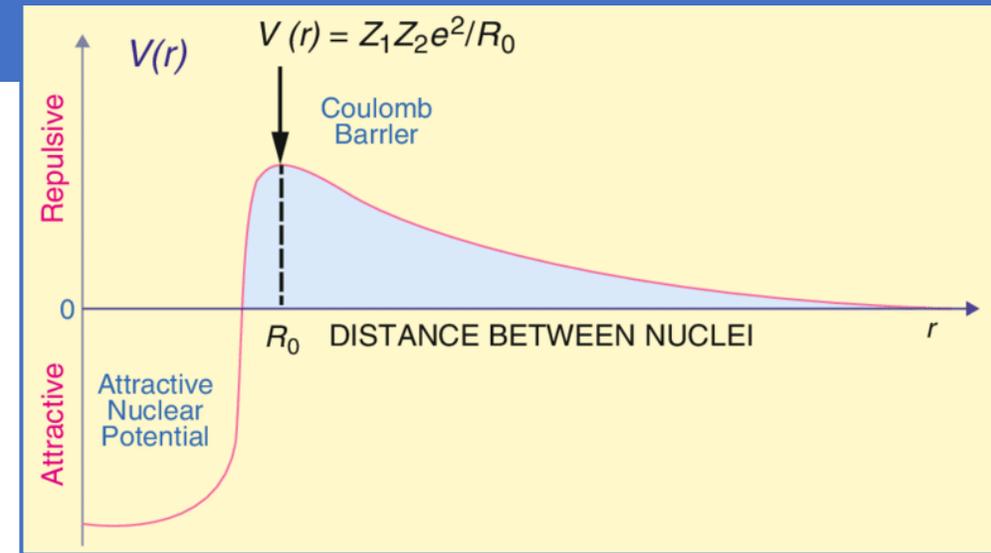
- Famous nucleon-nucleon potential is the Nijmegen potential:

- De Swart, Rijken et al., 1980 - 1990
 - <https://arxiv.org/pdf/nucl-th/9509024.pdf>

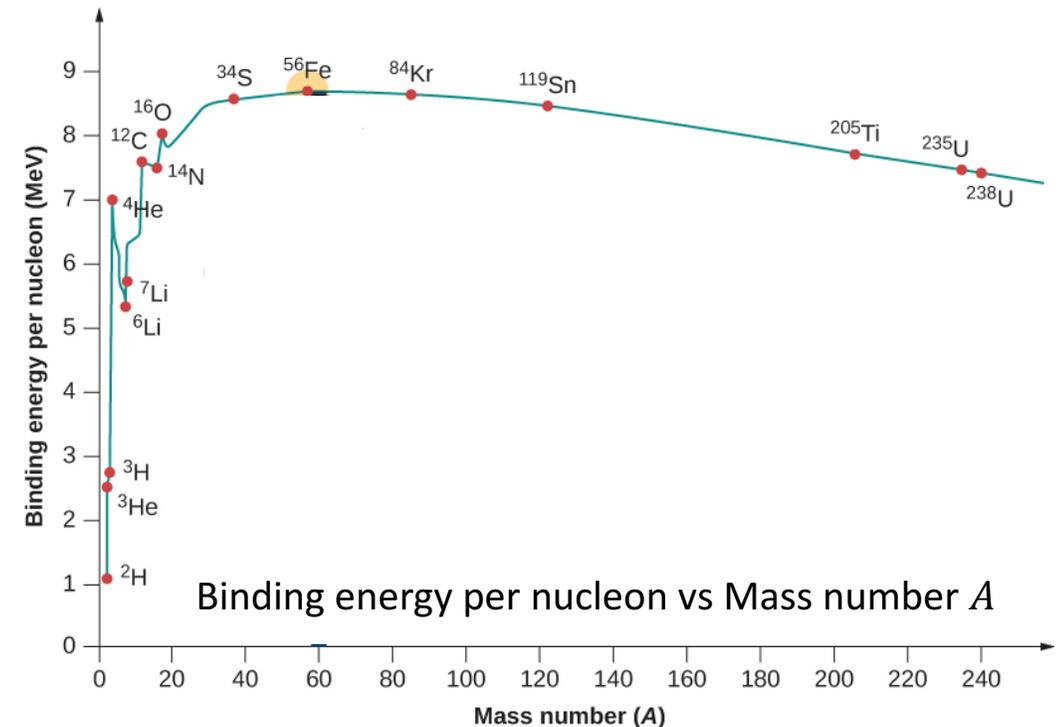


Binding Energy

- The energy of the state inside the potential well is lower than the energy of free particles
- If you “build” a nucleus from free particles energy becomes available: “binding energy”
- This appears by a reduction of mass: the nucleus is lighter than the sum of its components.



- Binding energy: $E = \Delta m c^2$
- $\Delta m = m_{nucleus} - (N_p M_p + N_n M_n)$
 $= m_{nucleus} - (Z M_p + (A - Z) M_n) < 0$
 - This holds for all bound systems
 - Hydrogen: $m_p + m_e = m_H + 13.6 \text{ eV}/c^2$
 - Deuterium: $m_p + m_n = M_D + 1.7 \text{ MeV}/c^2$
- ^{56}Fe has the highest binding energy

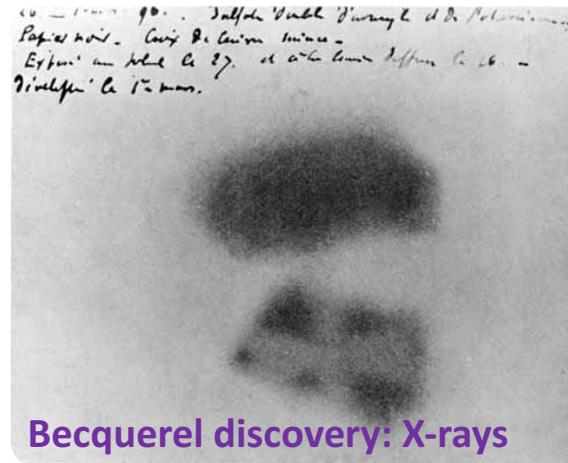


Nuclear decay (Radioactivity)

- Radioactivity (1896)

Henri Becquerel, Pierre and Marie Curie:

- Unstable nucleus
- Quantum tunneling process



Becquerel discovery: X-rays

- Rutherford classification into: alpha, beta, gamma decays
 - alpha and beta decay changes chemical element (Z)

- In nature things decay exponentially:

- Equal probability per unit time:

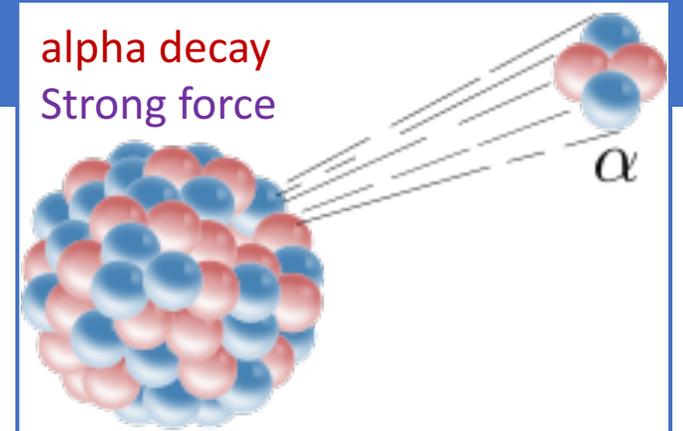
$$-dN = \lambda N dt$$

$$N(t) = N_0 e^{-\lambda t} = N_0 e^{-t/\tau}$$

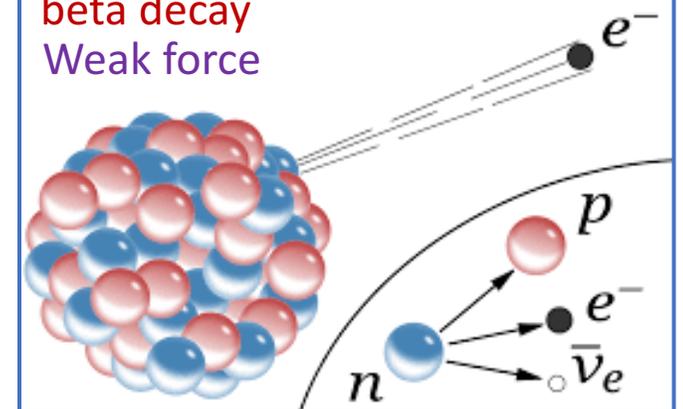
- Half-life:

$$N_{1/2} = N_0/2 \rightarrow e^{-t_{1/2}/\tau} = \frac{1}{2} \rightarrow -t_{1/2}/\tau = \ln \frac{1}{2} \rightarrow t_{1/2} = \tau \ln 2$$

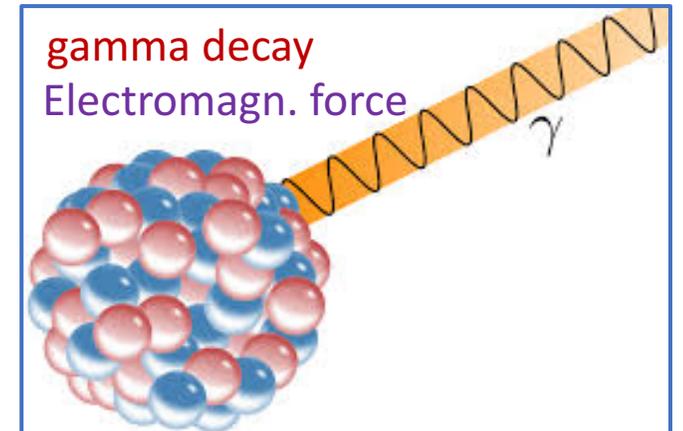
alpha decay
Strong force



beta decay
Weak force



gamma decay
Electromagn. force

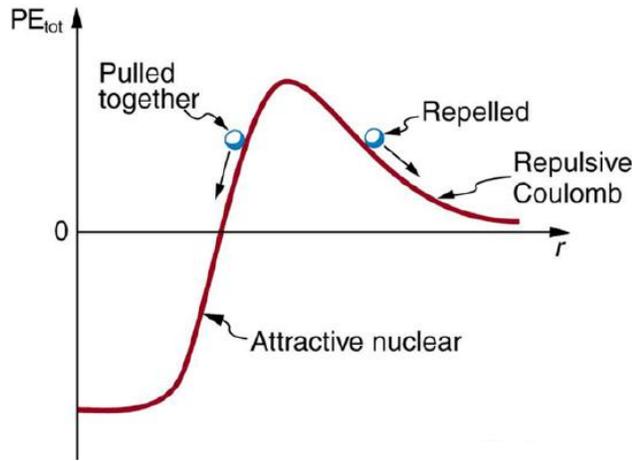


Nuclear decay (Radioactivity)

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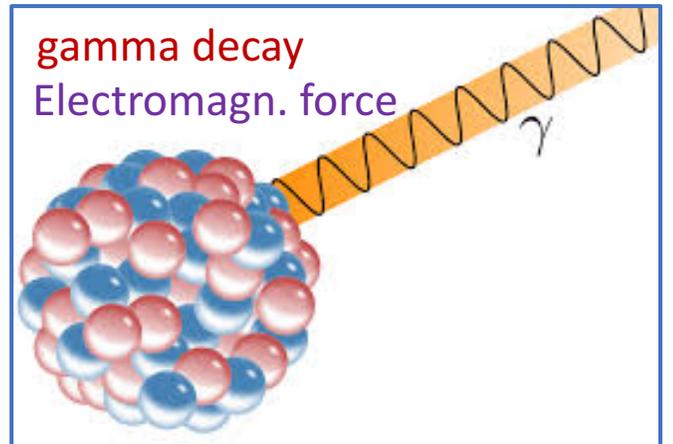
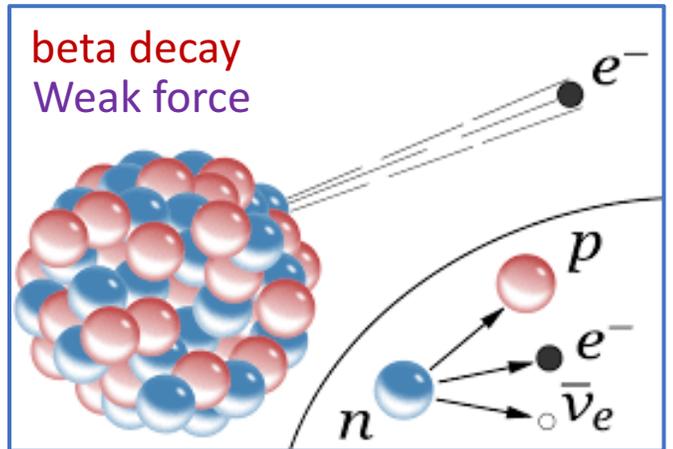
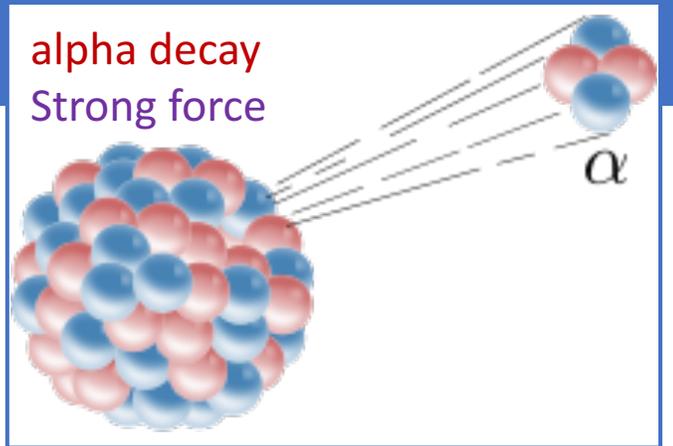
- Equal probability per unit time:

$$-dN = \lambda N dt$$

$$N(t) = N_0 e^{-\lambda t} = N_0 e^{-t/\tau}$$

- Half-life $t_{1/2}$ vs decay time τ :

$$N_{1/2} = N_0/2 \rightarrow e^{-t_{1/2}/\tau} = \frac{1}{2} \rightarrow -t_{1/2}/\tau = \ln \frac{1}{2} \rightarrow t_{1/2} = \tau \ln 2$$



Penetrating power

- Alpha particles stopped by piece of paper

α



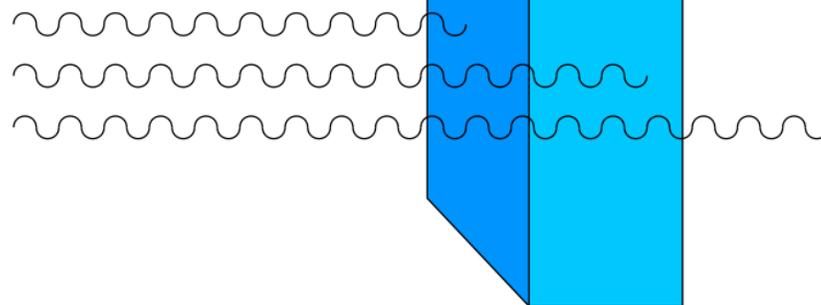
- Beta particles stopped by sheet of aluminium

β

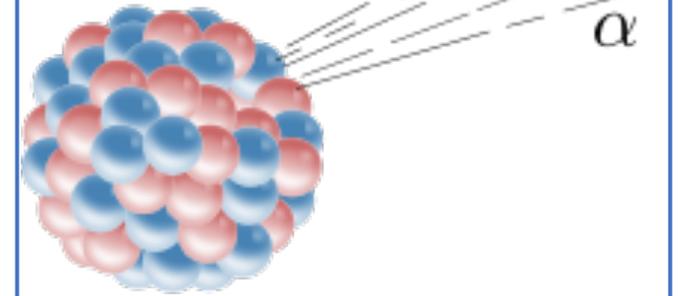


- Gamma particles stopped by layer of lead

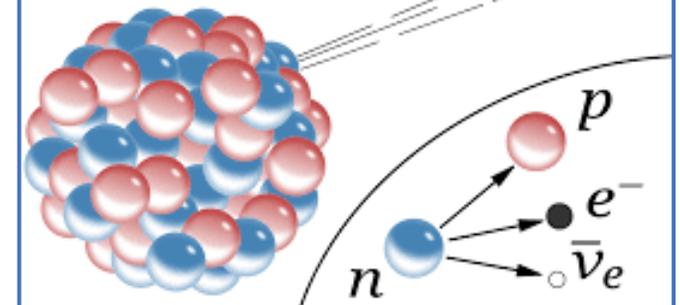
γ



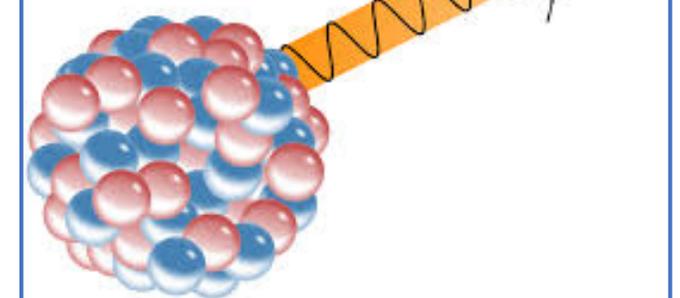
alpha decay
Strong force



beta decay
Weak force

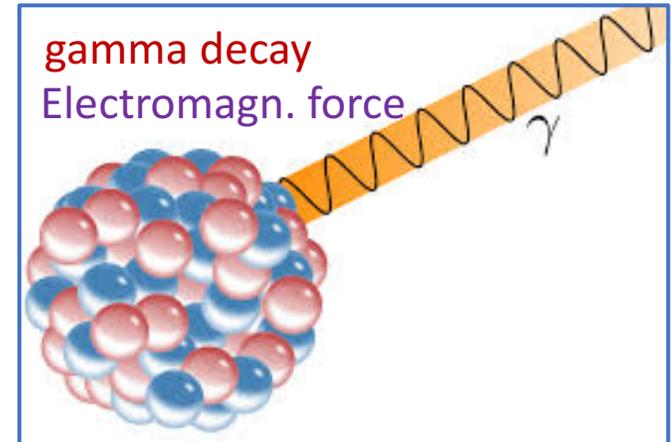
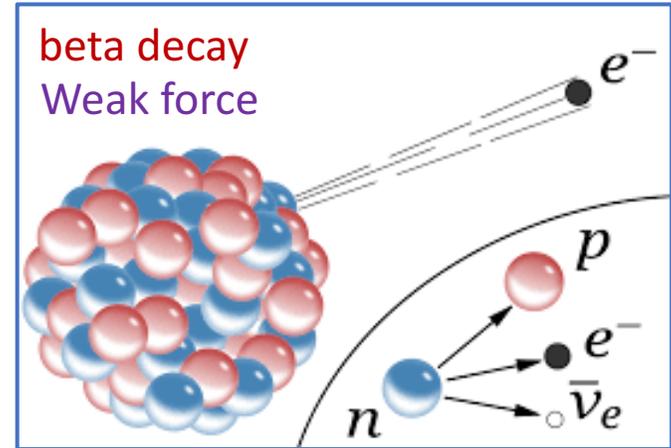
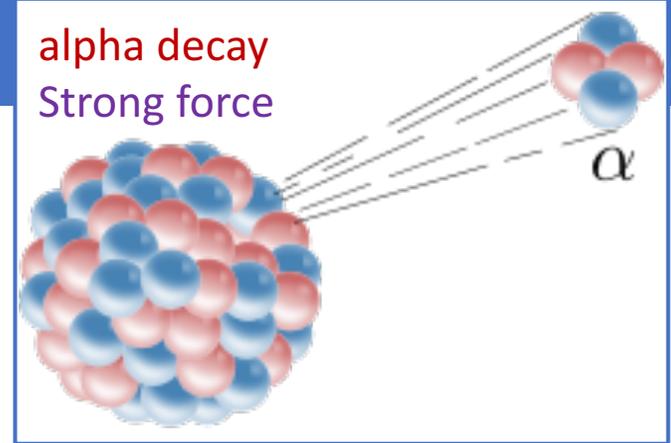
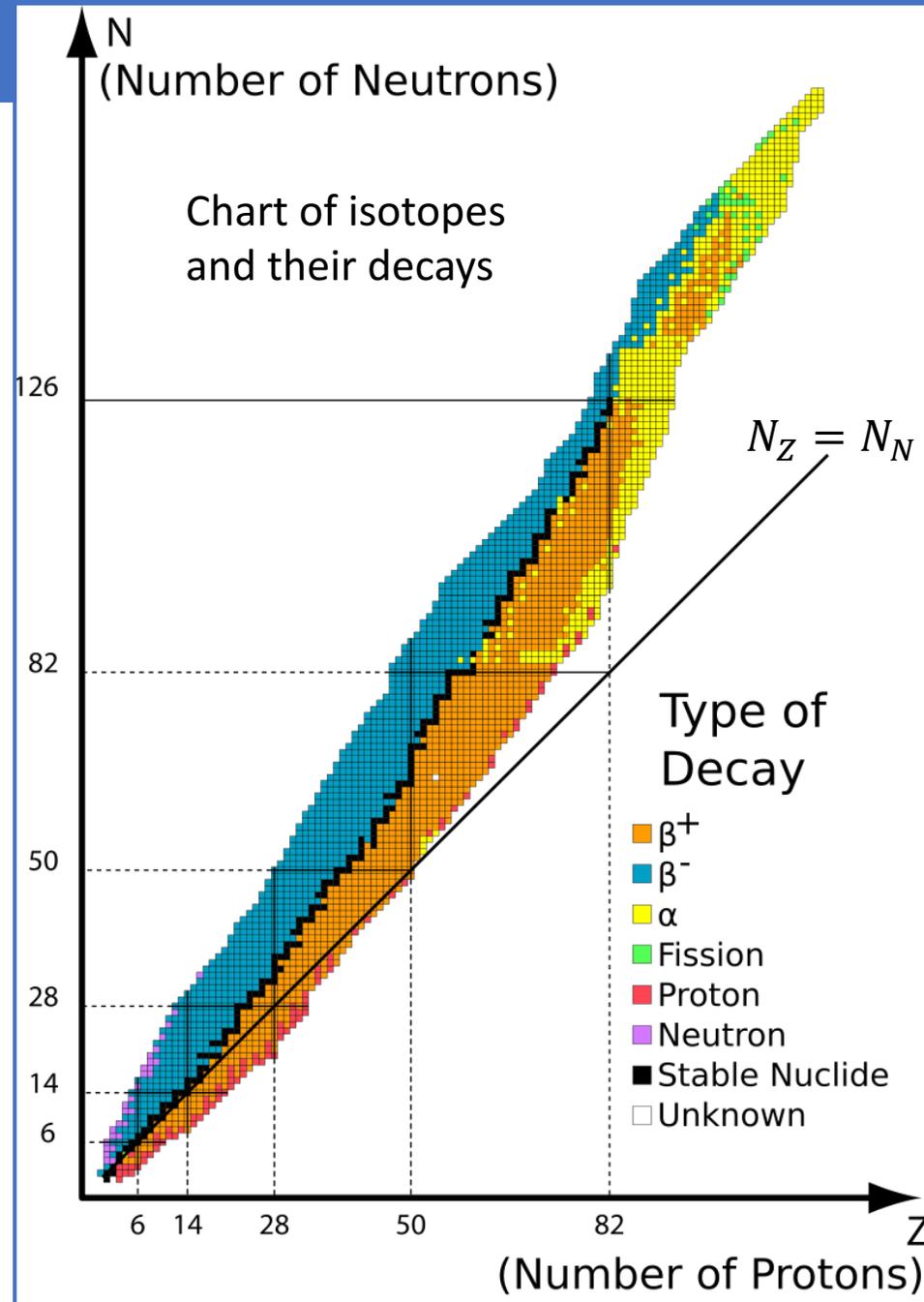


gamma decay
Electromagn. force



Nuclear Decays

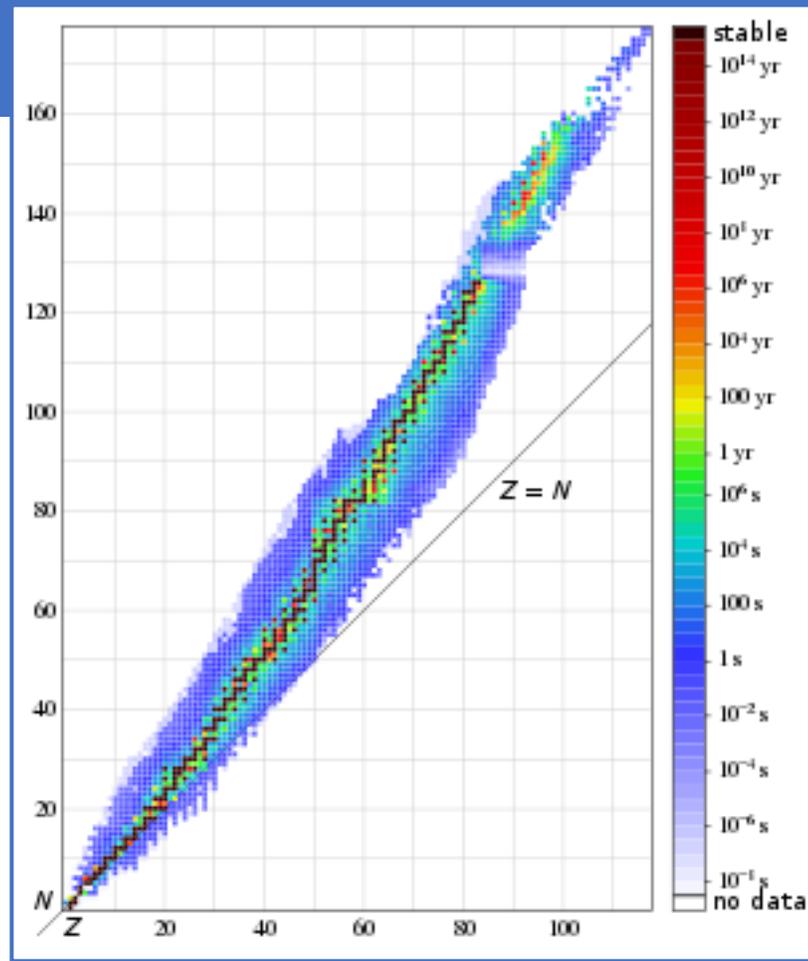
- Alpha particles stopped by piece of paper
- Beta particles stopped by sheet of aluminium
- Gamma particles stopped by layer of lead



Radioactive Elements

- Half-lives vary enormously

- At least one stable element exists
- Slightly radioactive $\tau_{1/2} \sim$ millions of years
- Radioactive: $\tau_{1/2} \sim$ thousands of years
- Highly radioactive: $\tau_{1/2} \sim$ minutes to weeks
- Extremely radioactive: $\tau_{1/2} \sim$ seconds



| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|------------|-----------|------------|-----------|------------|------------|----------|----------|
| | I | | II | | | | | | | | | | | | | | | | | | III | IV | V | VI | VII | VIII | | | | | | | | |
| 1 | 1 H | | | | | | | | | | | | | | | | | | | | | | | | | | | 2 He | | | | | | |
| 2 | 3 Li | 4 Be | | | | | | | | | | | | | | | | | 5 B | 6 C | 7 N | 8 O | 9 F | 10 Ne | | | | | | | | | | |
| 3 | 11 Na | 12 Mg | | | | | | | | | | | | | | | | | 13 Al | 14 Si | 15 P | 16 S | 17 Cl | 18 Ar | | | | | | | | | | |
| 4 | 19 K | 20 Ca | | | | | | | | | | | | | | | | | 21 Sc | 22 Ti | 23 V | 24 Cr | 25 Mn | 26 Fe | 27 Co | 28 Ni | 29 Cu | 30 Zn | 31 Ga | 32 Ge | 33 As | 34 Se | 35 Br | 36 Kr |
| 5 | 37 Rb | 38 Sr | | | | | | | | | | | | | | | | | 39 Y | 40 Zr | 41 Nb | 42 Mo | 43 Tc | 44 Ru | 45 Rh | 46 Pd | 47 Ag | 48 Cd | 49 In | 50 Sn | 51 Sb | 52 Te | 53 I | 54 Xe |
| 6 | 55 Cs | 56 Ba | 57 La | 58 Ce | 59 Pr | 60 Nd | 61 Pm | 62 Sm | 63 Eu | 64 Gd | 65 Tb | 66 Dy | 67 Ho | 68 Er | 69 Tm | 70 Yb | 71 Lu | 72 Hf | 73 Ta | 74 W | 75 Re | 76 Os | 77 Ir | 78 Pt | 79 Au | 80 Hg | 81 Tl | 82 Pb | 83 Bi | 84 Po | 85 At | 86 Rn | | |
| 7 | 87 Fr | 88 Ra | 89 Ac | 90 Th | 91 Pa | 92 U | 93 Np | 94 Pu | 95 Am | 96 Cm | 97 Bk | 98 Cf | 99 Es | 100 Fm | 101 Md | 102 No | 103 Lr | 104 Rf | 105 Db | 106 Sg | 107 Bh | 108 Hs | 109 Mt | 110 Ds | 111 Rg | 112 Cn | 113 Uut | 114 Fl | 115 Uup | 116 Lv | 117 Uus | 118 Uuo | | |

Units in Radiation and Tissue

Inform yourself on doses related to Chernobyl and Fukushima.

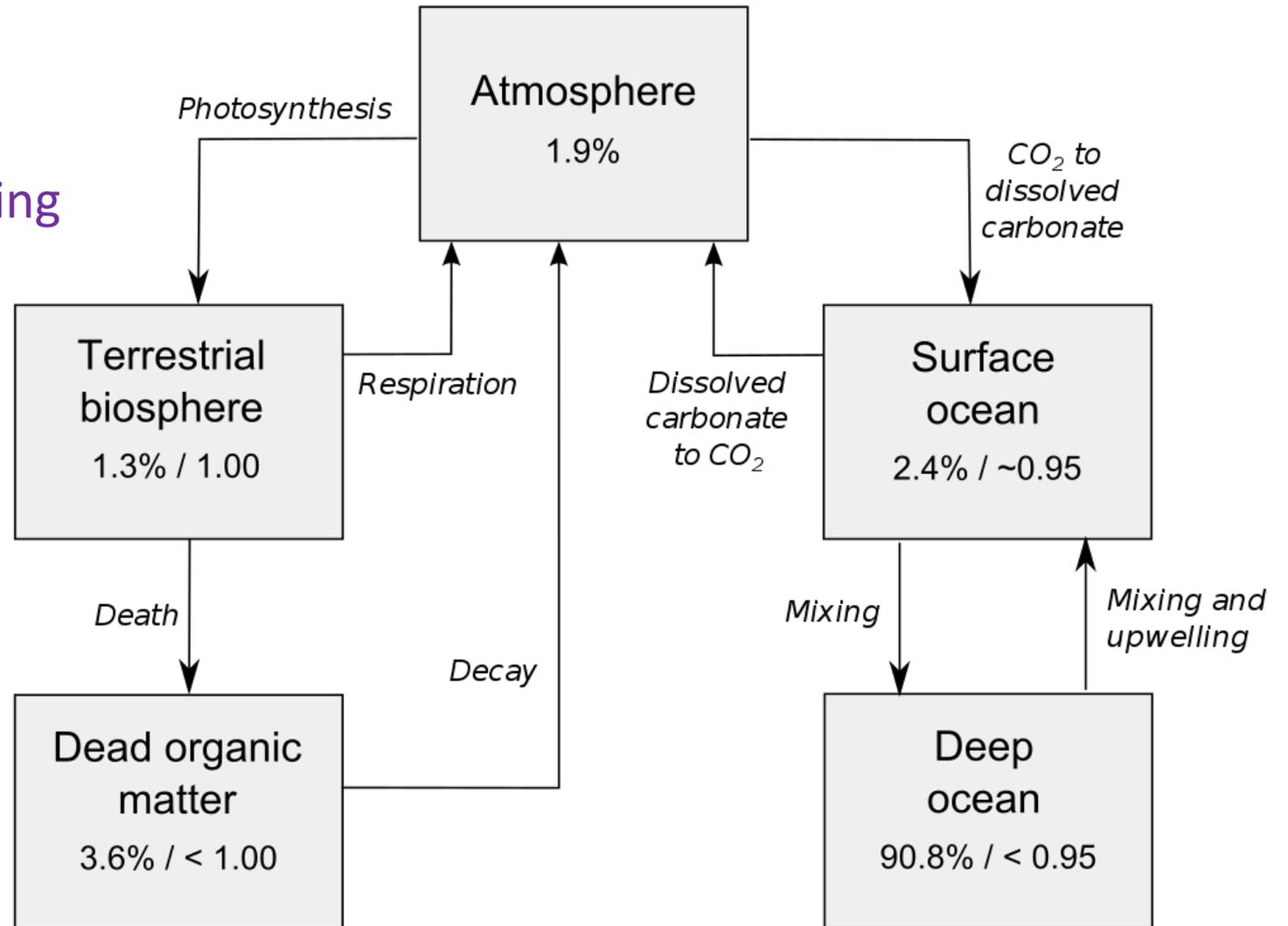
- Activity:
 - Number of disintegrations in a radioactive source is used to measure the intensity of the source
 - Main unit is Bequerel (Bq). 1 Bq is one event per second (typical kBq, MBq, GBq)
- Absorbed dose (exposure for X-rays):
 - The amount of energy coming from a source that is absorbed in a tissue. Used to assess the potential for biochemical changes in specific tissues.
 - Main unit is Gray (Gy). 1 Gy means that one kg of matter absorbed one joule of energy (typical mGy)
- Equivalent or biological dose:
 - Used to assess how much biological damage is expected from the absorbed dose. Different types of radiation have different damaging properties
 - Main unit is Sievert (Sv). 1 Sv equal 1 Gy multiplied by a weighting factor
- Effective dose:
 - Used to assess the potential for long-term effects that might occur in future. Takes into account all the organs in the body, the timespan of irradiation etc.

Units in Radiation and Tissue

| Ionizing radiation related quantities view · talk · edit | | | | | |
|--|--|--------|--|------|--------------------------------|
| Quantity | Unit | Symbol | Derivation | Year | SI equivalence |
| Absorbed dose (<i>D</i>) | gray | Gy | $\text{J} \cdot \text{kg}^{-1}$ | 1974 | SI unit |
| Absorbed dose (<i>D</i>) | erg per gram | erg/g | $\text{erg} \cdot \text{g}^{-1}$ | 1950 | 1.0×10^{-4} Gy |
| Absorbed dose (<i>D</i>) | rad | rad | $100 \text{ erg} \cdot \text{g}^{-1}$ | 1953 | 0.010 Gy |
| Activity (<i>A</i>) | becquerel | Bq | s^{-1} | 1974 | SI unit |
| Activity (<i>A</i>) | curie | Ci | $3.7 \times 10^{10} \text{ s}^{-1}$ | 1953 | 3.7×10^{10} Bq |
| Activity (<i>A</i>) | rutherford | Rd | 10^6 s^{-1} | 1946 | 1,000,000 Bq |
| Equivalent dose (<i>H</i>) | sievert | Sv | $\text{J} \cdot \text{kg}^{-1} \times \underline{W_R}$ | 1977 | SI unit |
| Equivalent dose (<i>H</i>) | röntgen equivalent man | rem | $100 \text{ erg} \cdot \text{g}^{-1} \times \underline{W_R}$ | 1971 | 0.010 Sv |
| Exposure (<i>X</i>) | coulomb per kilogram | C/kg | $\text{C} \cdot \text{kg}^{-1}$ of air | 1974 | SI unit |
| Exposure (<i>X</i>) | röntgen | R | $\underline{\text{esu}}$ / 0.001293 g of air | 1928 | 2.58×10^{-4} C/kg |

Exercise-3: How does Radiocarbon dating work?

- Exercise:
 - Explain how the Carbon dating method works



Percentages show the fraction of the total carbon reservoir of each type.
Numbers after slash show ratio of ¹⁴C to ¹²C as fraction of atmospheric ratio.

A model of the nucleus: Liquid drop model (~1935)

- Nucleus ~ uniform density, like an incompressible drop of water
- Strong nuclear force – pairs of nucleons: expect $\sim A^2$, but:
 - Very short ranges: sees only nearest neighbours
 - 'Volume' energy term $\propto A$
 - At surface less neighbours: a negative correction
 - 'Surface tension' term: $\propto A^{2/3}$, (since radius $\propto A^{1/3}$)
- Coulomb repulsion: Long range, all protons see all others. $R \propto A^{1/3}$
 - 'Coulomb term': $\propto Z^2 A^{-1/3}$ (think of sphere of charge density $\propto Q^2/R$)
- Pauli exclusion:
 - Asymmetry term, prefer to fill up low energy states first:
 - 'Pauli term': $\propto (N - Z)^2/A$ or $(A - 2Z)^2/A$
- Spin-spin coupling (pairing term), lowers energy if even #p or even #n:
 - $\propto \delta A^{-3/4}$ (empirical) where $\delta = \{-1, 0, 1\}$ if = $\{Z \text{ and } N = \text{even}, A = \text{odd}, Z \text{ and } N = \text{odd}\}$

See Wikipedia:
Semi-empirical_mass_formula

- Binding energy (semi-empirical):

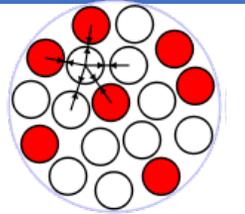
$$E_B = a_1 A - a_2 A^{2/3} - a_3 \frac{Z^2}{A^{1/3}} - a_4 \frac{(N-Z)^2}{A} + \delta a_5 A^{-3/4}$$

- Bethe-Weizsacker empirical mass formula:

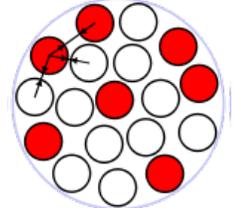
$$M(A, Z) = (A - Z)m_n + Z(m_p) - \frac{E_B}{c^2}$$

Values:

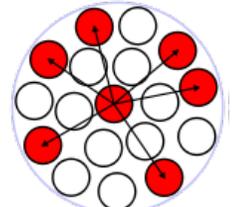
$$\begin{aligned} a_1 &\approx 15.6 \text{ MeV}, & a_2 &\approx 16.8 \text{ MeV}, \\ a_3 &\approx 0.72 \text{ MeV}, & a_4 &\approx 23.3 \text{ MeV} \\ a_5 &\approx 34 \text{ MeV} \end{aligned}$$



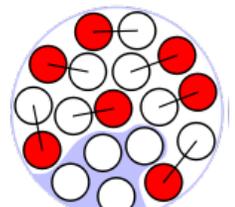
Volume



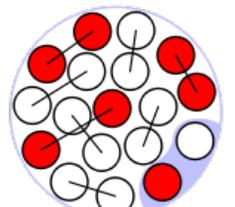
Surface



Coulomb



Asymmetry

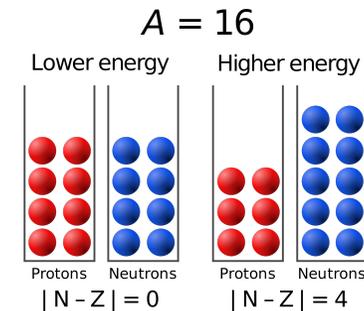


Pairing

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See Wikipedia:
Semi-empirical_mass_formula



- Binding energy (semi-empirical):
- Bethe-Weizsacker empirical mass formula:

$$E_B = a_1 A - a_2 A^{2/3} - a_3 \frac{Z^2}{A^{1/3}} - a_4 \frac{(N-Z)^2}{A} + \delta a_5 A^{-3/4}$$

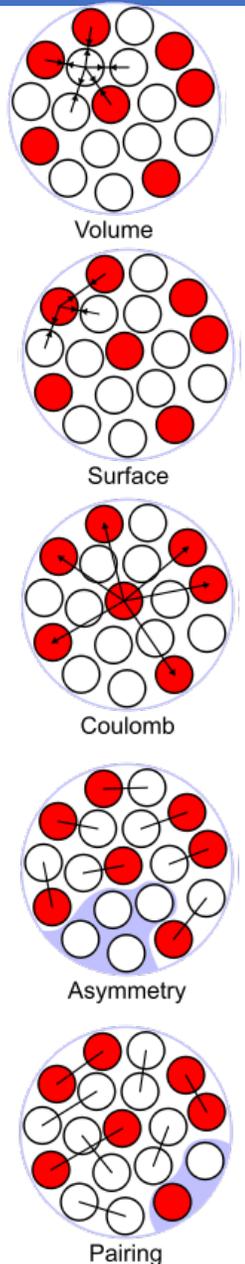
$$M(A, Z) = (A - Z)m_n + Z(m_p) - \frac{E_B}{c^2}$$

Values:

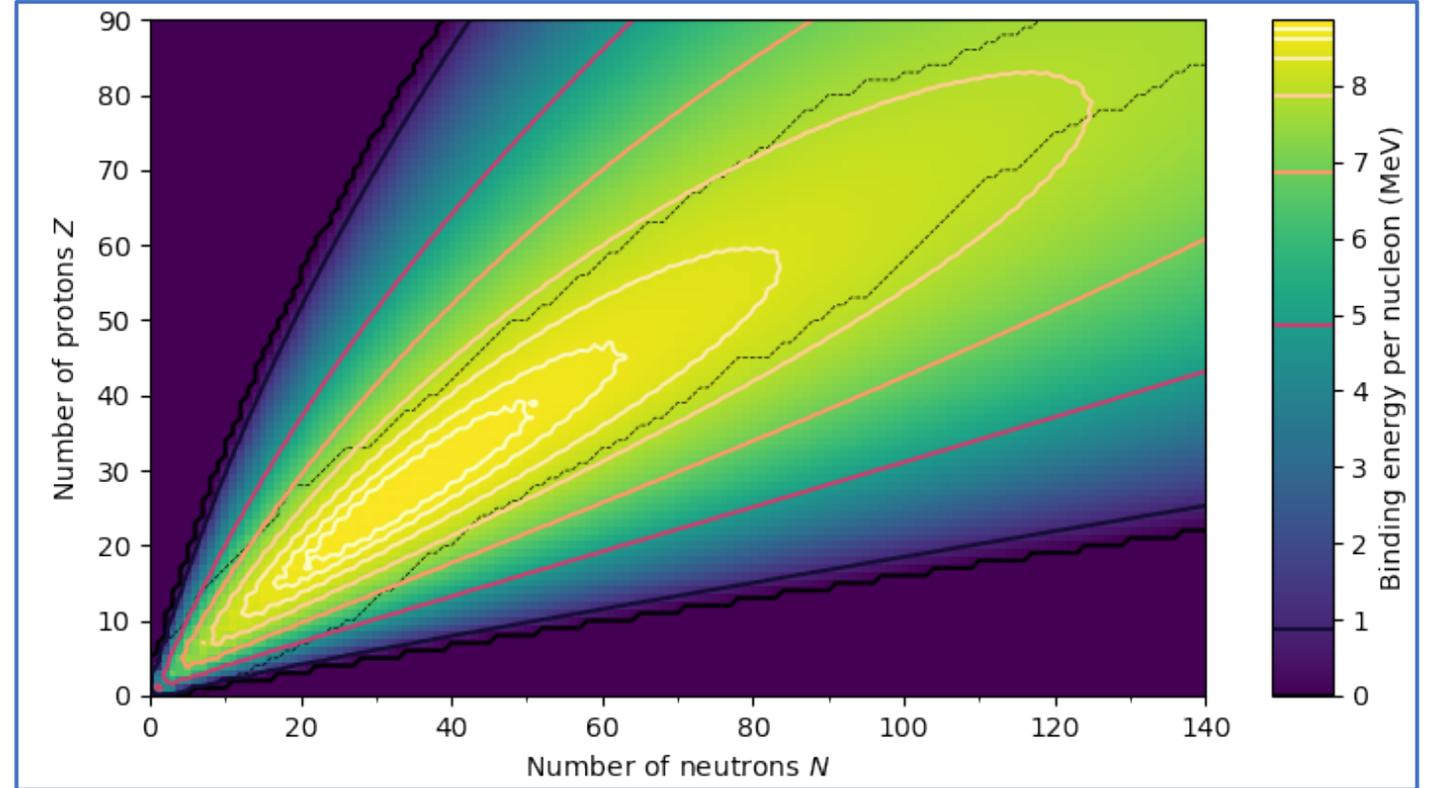
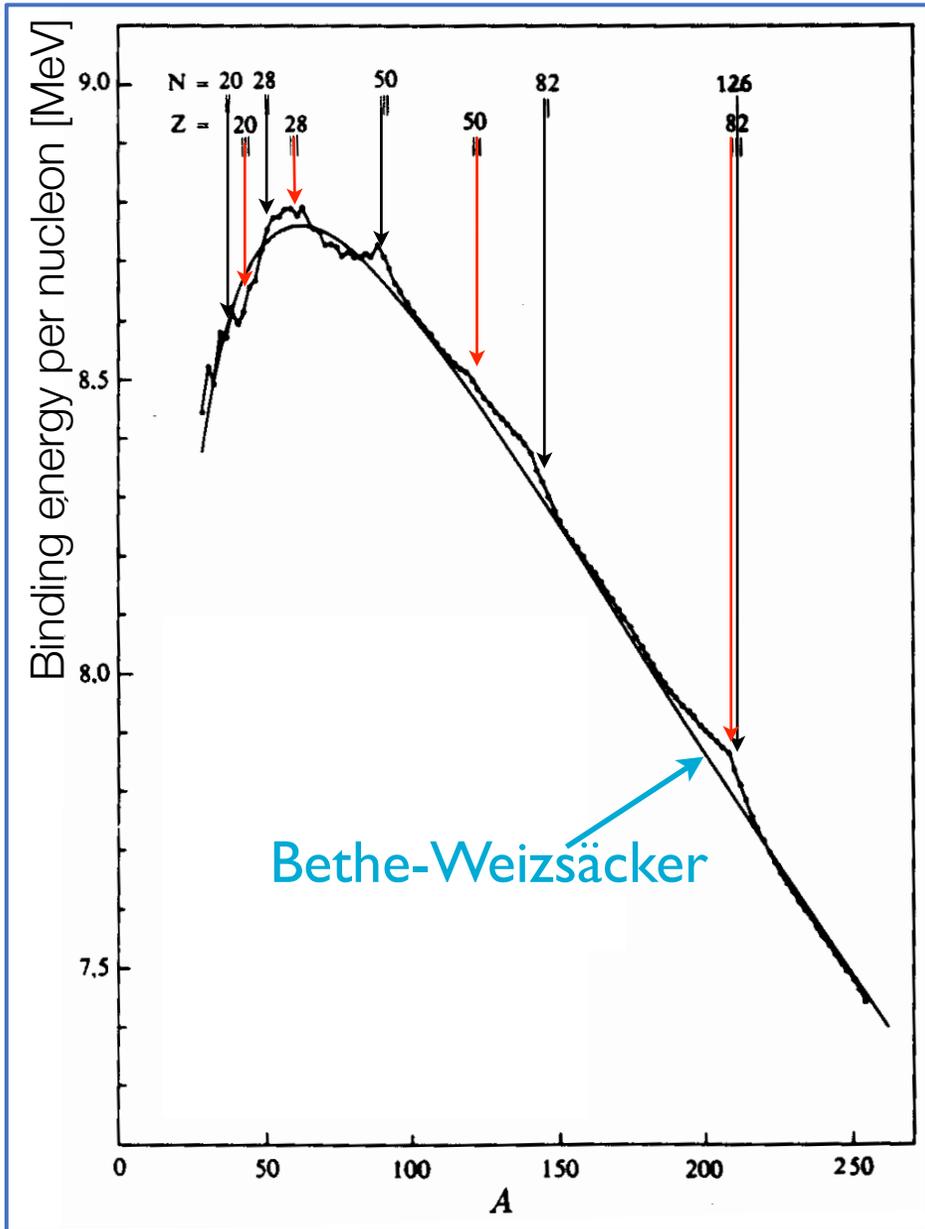
$$a_1 \approx 15.6 \text{ MeV}, a_2 \approx 16.8 \text{ MeV},$$

$$a_3 \approx 0.72 \text{ MeV}, a_4 \approx 23.3 \text{ MeV}$$

$$a_5 \approx 34 \text{ MeV}$$



Binding Energy: 'magic numbers'



- Fits quite well
- Cannot explain 'peaks' that occur at 'magic numbers' where the nucleus is strongly bound.
 - N or $Z = 2, 8, 20, 28, 50, 82, 126$
- Double magic nuclei (both N and Z are magic):
 - ${}^4\text{He}$, ${}^{16}\text{O}$, ${}^{40}\text{Ca}$, ${}^{48}\text{Ca}$, ${}^{48}\text{Ni}$, ${}^{208}\text{Pb}$

Nuclear Shell model (1949)

- Similar to the atomic shell model (remember hydrogen atom) for electrons):

- Atomic shells: Energy levels; n, l, s quantum numbers
- Solution of Schrodinger equation (QED)

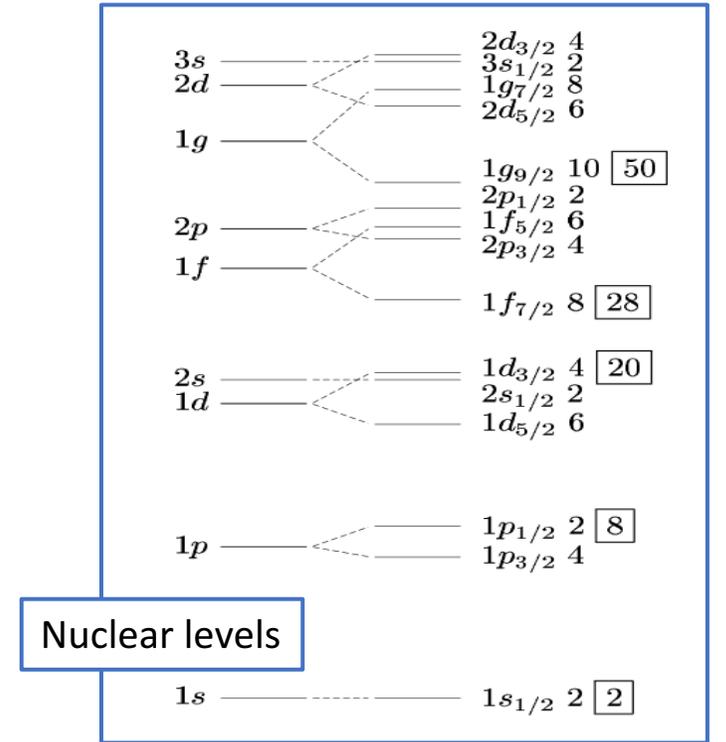
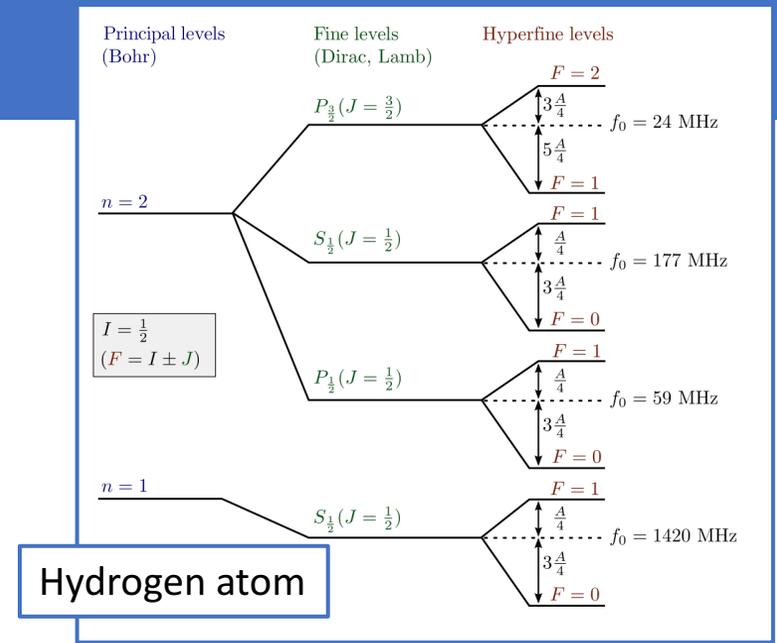
- $$i\hbar \frac{\partial}{\partial t} \psi = -\frac{\hbar^2}{2m} \nabla^2 \psi + V\psi \quad \text{with } V = -\frac{e^2}{4\pi\epsilon_0} \frac{1}{r}$$

- Now strong force: which potential V ?

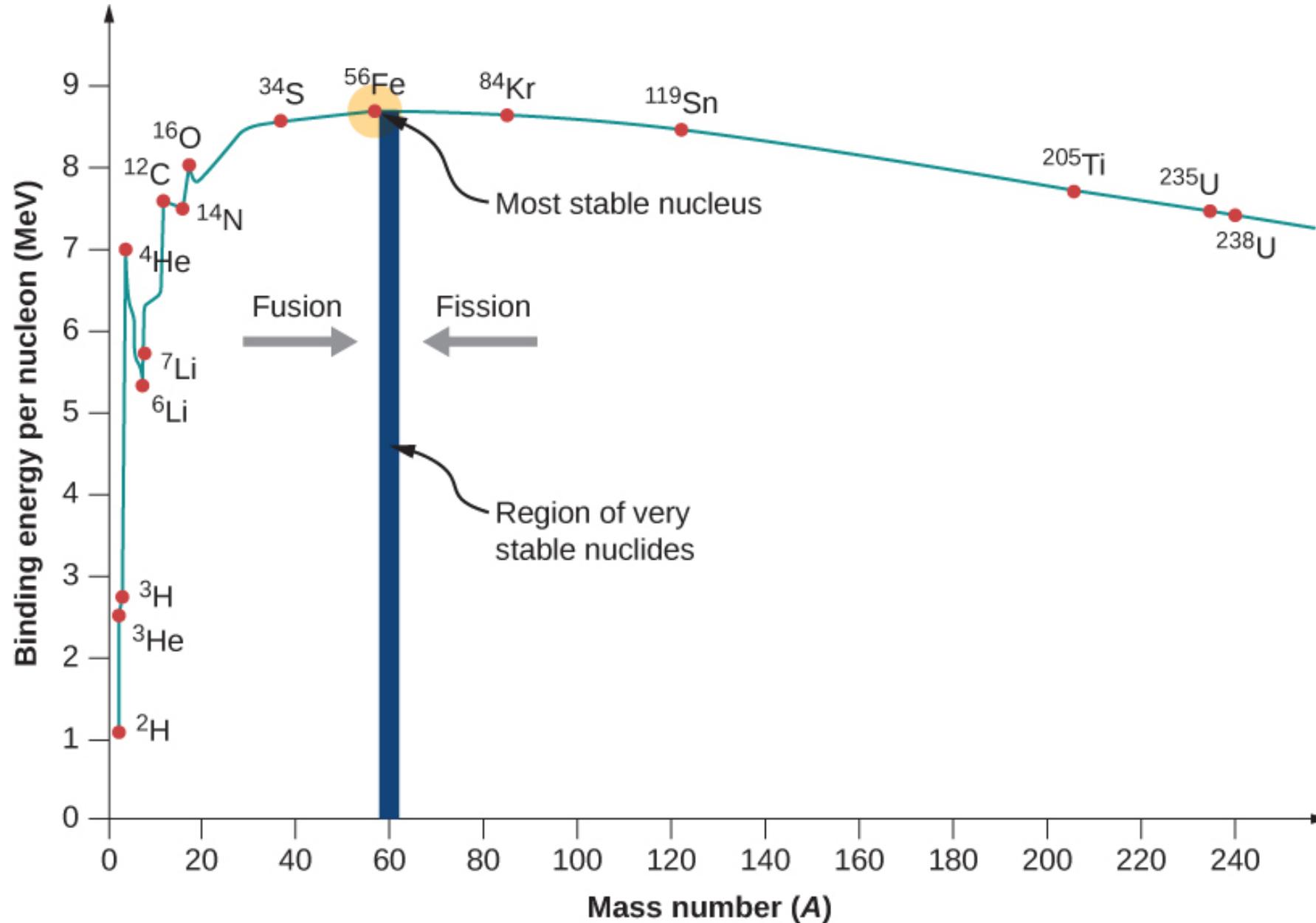
- Use the nuclear potential
- Try square well, try Harmonic oscillator, $V = \mu\omega^2 r^2 / 2$
Need something inbetween.
- Woods Saxon works well: $V(r) = -\frac{V_0}{1 + \exp\left(\frac{r-R}{a}\right)}$
- Spin orbit interaction is stronger than in atom

- Nuclear shells “magic numbers”:

- Count energy levels of shells including spin:
 - $2 \times 1 = 2, 2 \times (1+3) = 8, 2 \times (1+3+6) = 20, \dots$
- Filled shell \rightarrow more tightly bound \rightarrow larger E_B

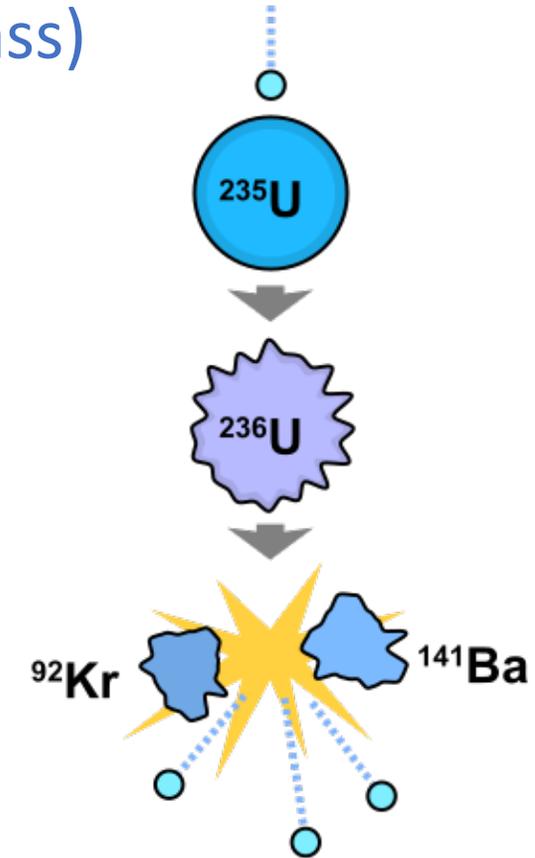


Nuclear Fission and Fusion



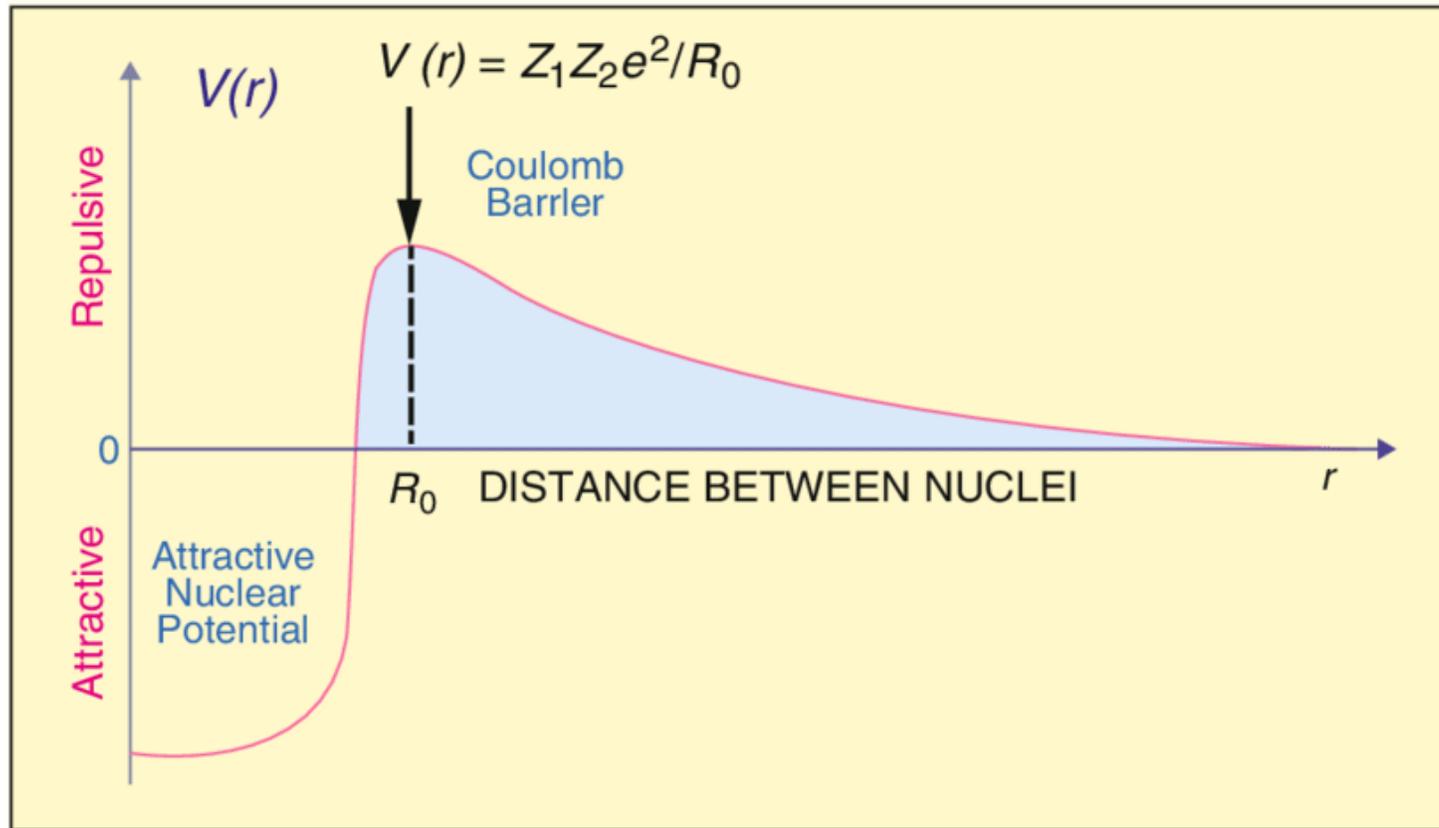
Nuclear Fission

- Heavy elements: less binding energy per nucleon (=more mass)
 - Transition heavy \rightarrow light: free some mass \rightarrow energy ($E = mc^2$)
 - Form high mass unstable isotope: eg. $^{235}_{92}\text{U} + 1$ neutron. Reaction:
$$^{236}_{92}\text{U} \rightarrow ^{141}_{56}\text{Ba} + ^{92}_{36}\text{Kr} + 3^1_0\text{n}$$
$$236.045568u \rightarrow 140.914411u + 91.926156u + 3 \times 1.008644u$$
$$\Delta m = 0.18u \Rightarrow E = \Delta m c^2 = 2.68 \times 10^{-11} \text{J} = 168 \text{MeV}$$
 - Note: $^{235}_{92}\text{U}$ occurs as 0.72% natural Uranium
 - To use it as an energy source it must be enriched (centrifuge)
- E_B turned into kinetic energy \rightarrow high temperature \rightarrow steam
 - Nuclear reactors: controlled reaction, moderators for neutron absorption
 - Nuclear bombs: uncontrolled reaction



Nuclear Fusion

- Light elements fuse to free energy (Δm)
- Need to overcome Coulomb barrier in order to fuse together
 - Fuse H or D

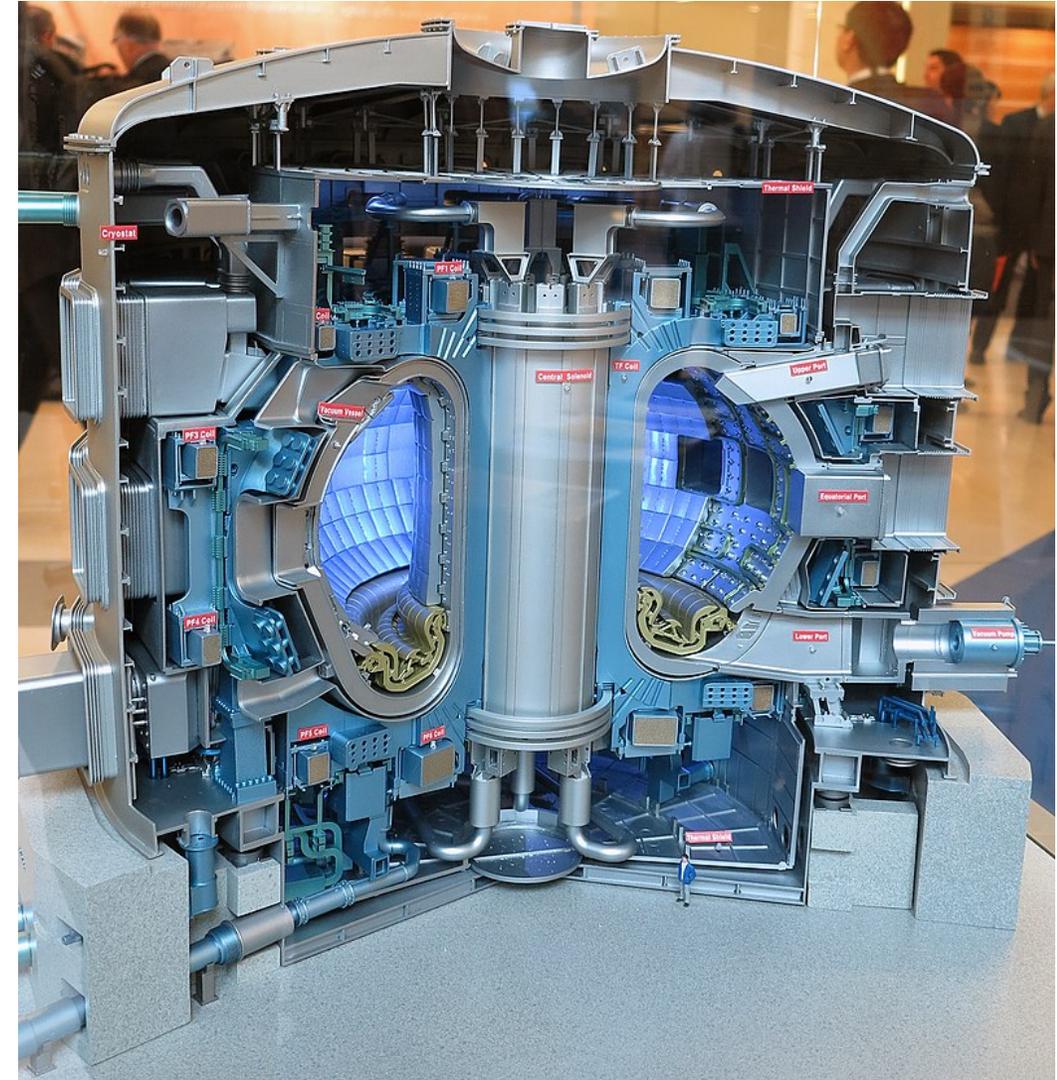
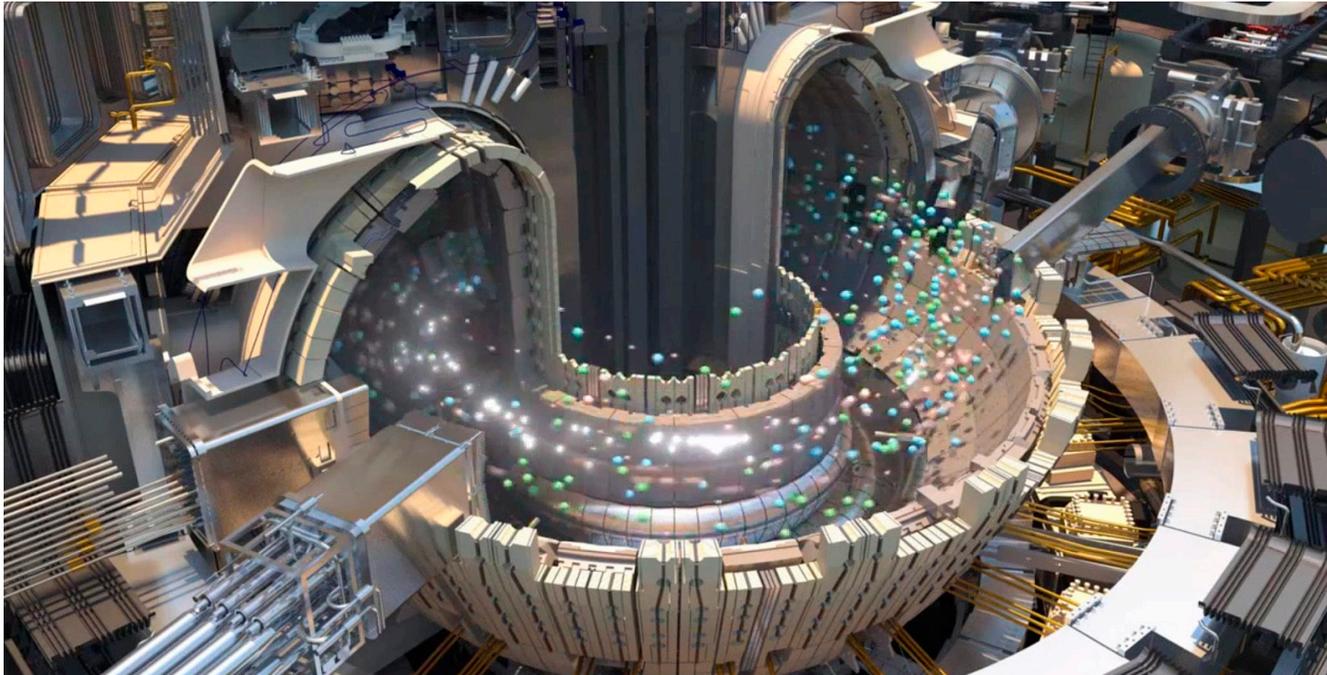


Coulomb barrier for charged-particle reactions

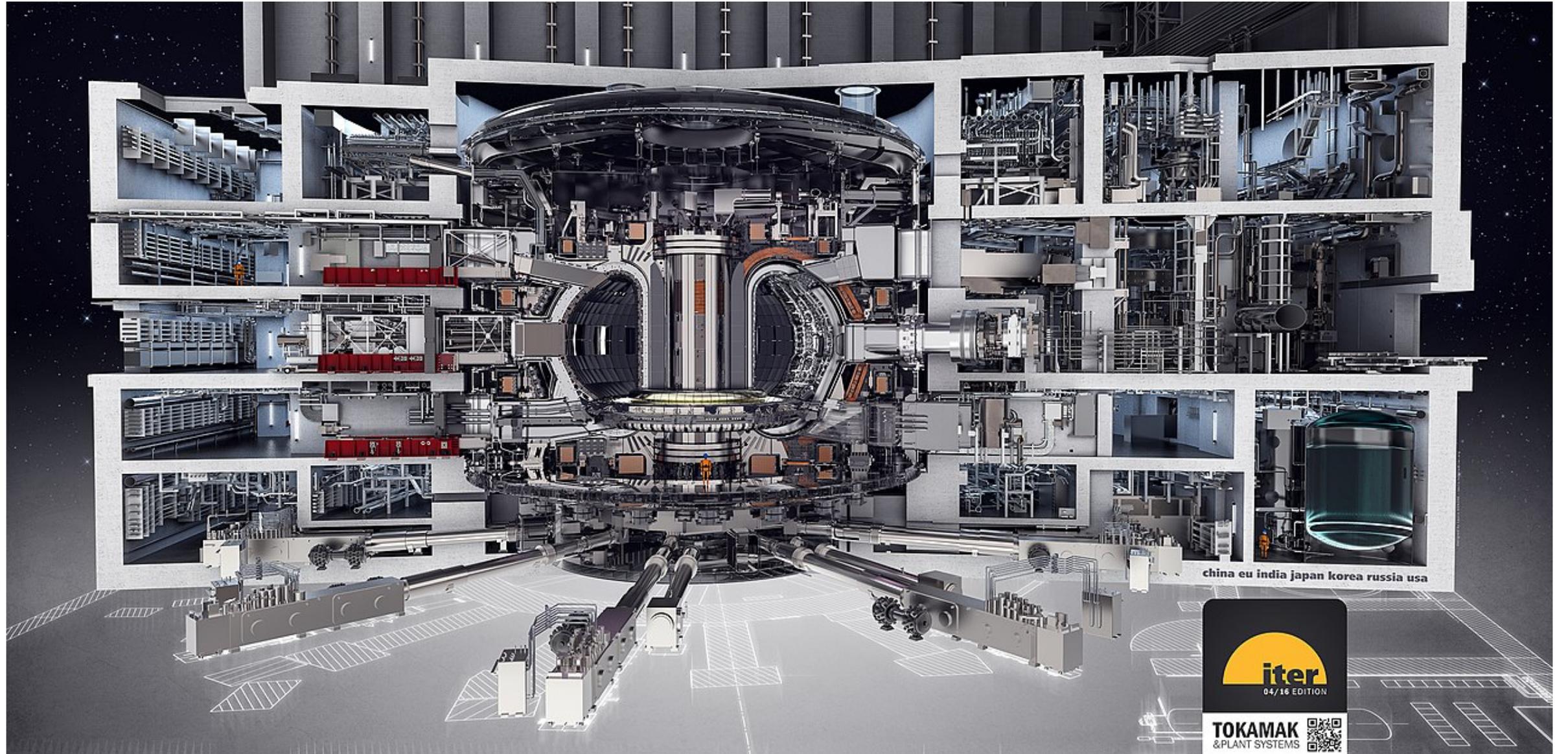
- Classically possible to fuse?
 - Would require extremely high kinetic energy \rightarrow unrealistic temperature
 - Sun would not burn!
- Quantum mechanical tunneling helps:
 - Go through the barrier instead of over it
 - Gamow factor

Nuclear Fusion: lab

- Fusion for power: need high energies and densities
 - ITER in France
- $150 \times 10^6 \text{ } ^\circ\text{C}$
- Challenges:
 - keep confined
 - Keep sustained



ITER



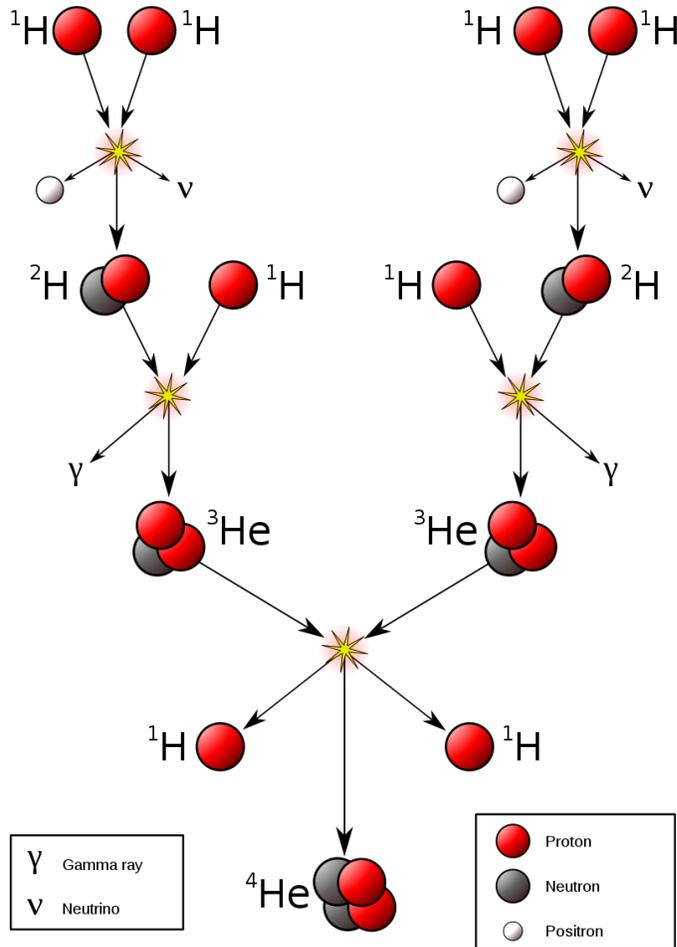
ITER in 2020



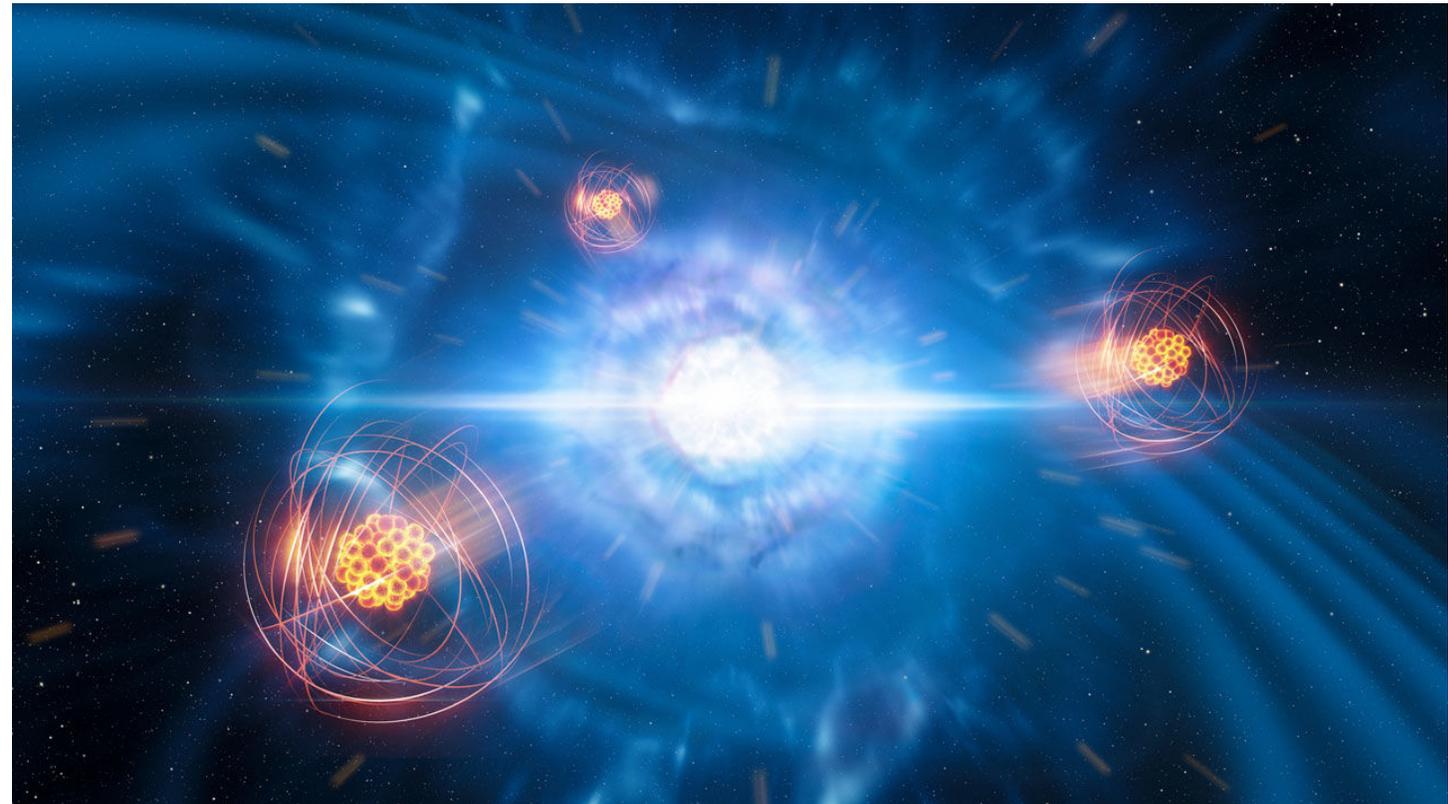
Nuclear Fusion: Universe

See Wikipedia: Nucleosynthesis

- Fusion in stars:
 - Proton-proton chain reaction (sun)
 - CNO catalytic cycle ($m_{star} > 1.3 m_{sun}$)



- How are heavy elements formed in the universe?
 - Colliding neutron stars



Exercise-4: Fission vs Fusion

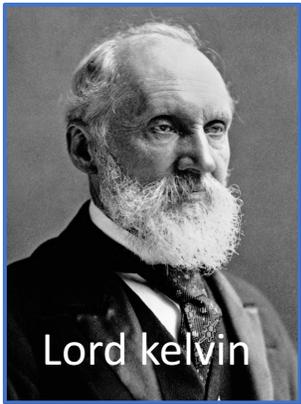
- a) Calculate the energy released if 1 gram of U-235 splits into La-148 + Br-87.
- b) Calculate the energy released in the fusion process of 0.5 grams of heavy water (D₂O) with 0.5 grams of superheavy water (T₂O), creating He-4 and a neutron. You may neglect the binding energies of the molecules.
- c) Compare the energies released per gram of fuel calculated above. Which would you prefer?

Lecture 1 : Particles

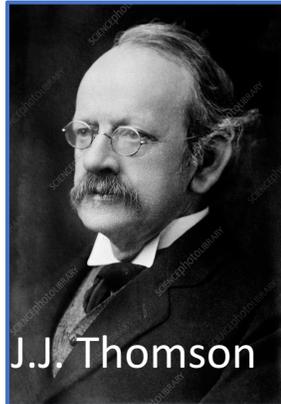
Part 2

Subatomic Particles

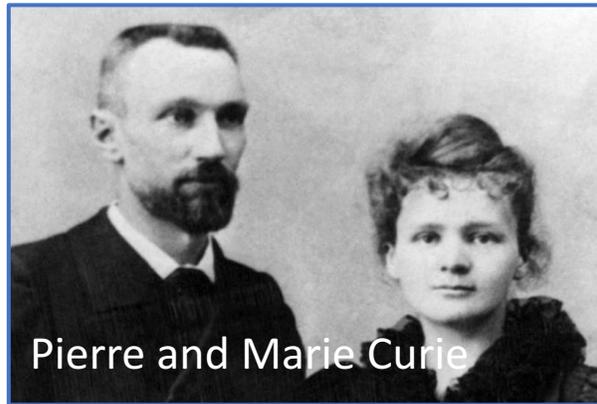
Particle Physics: Historical introduction – Griffiths chapter 1



Lord kelvin



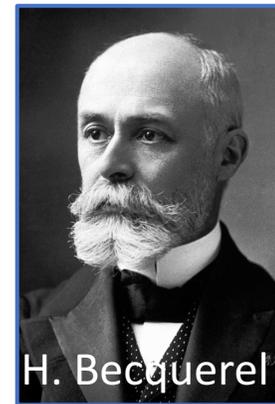
J.J. Thomson



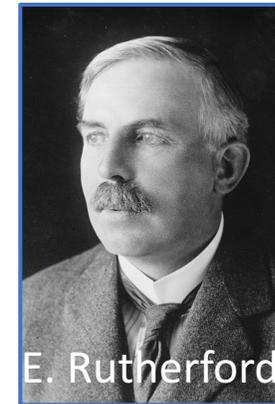
Pierre and Marie Curie



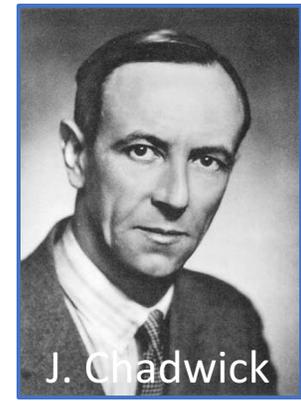
W. Röntgen



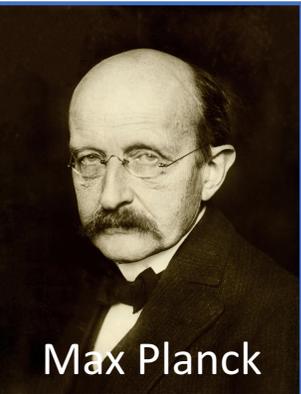
H. Becquerel



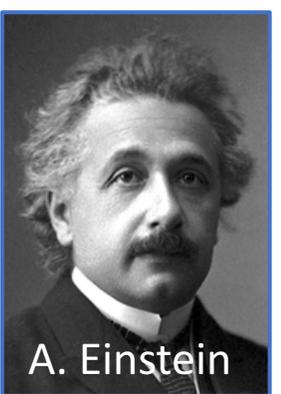
E. Rutherford



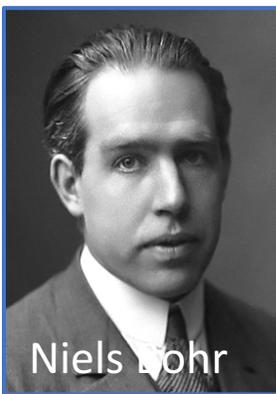
J. Chadwick



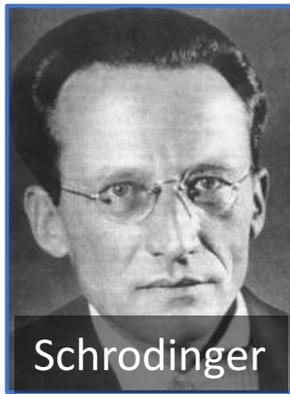
Max Planck



A. Einstein



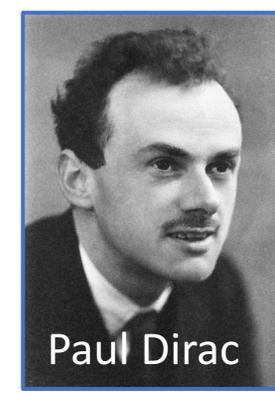
Niels Bohr



Schrodinger



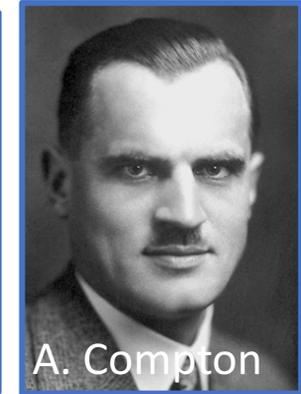
Heisenberg



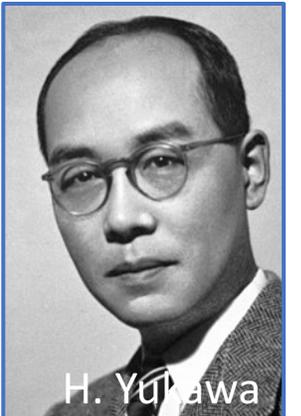
Paul Dirac



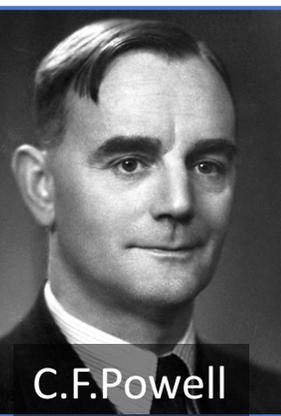
L. De Broglie



A. Compton



H. Yukawa



C.F. Powell



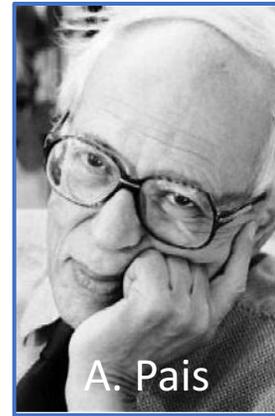
W. Pauli



Anderson



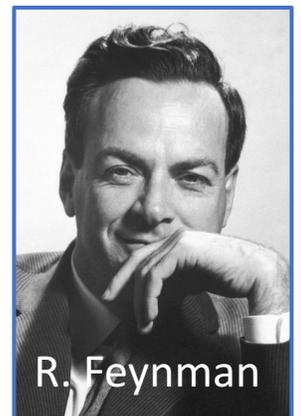
J de Vries



A. Pais



M. Gell Mann



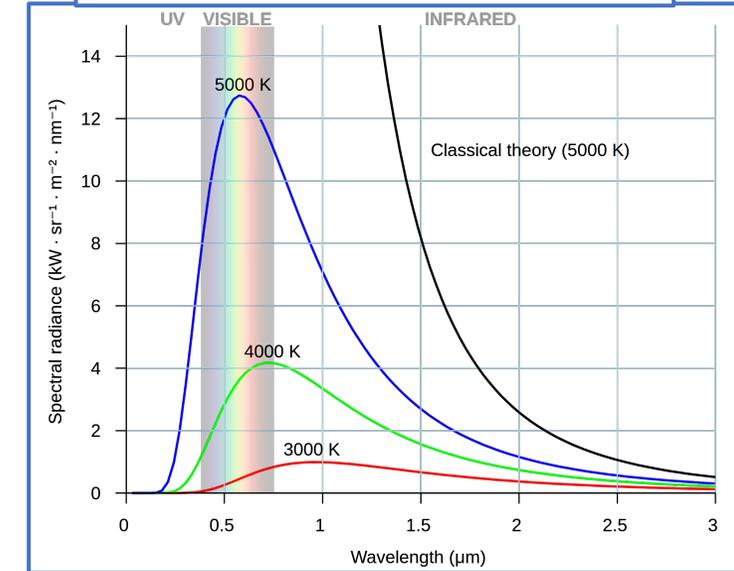
R. Feynman

The classic era

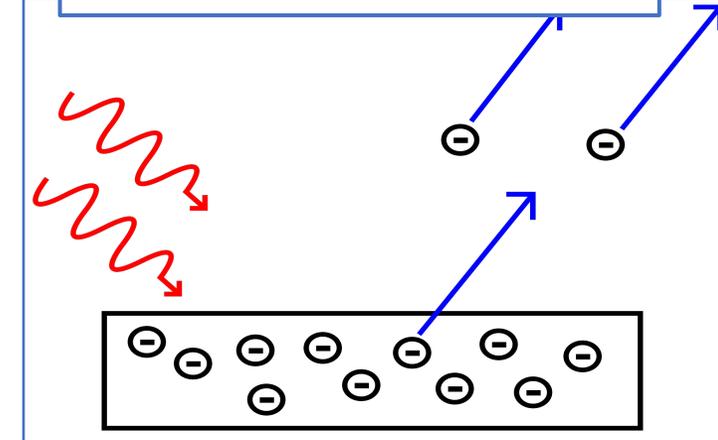
- ~1900: Lord Kelvin on physics:
 - “There is nothing new to be discovered in physics now. All that remain is more and more precise measurements.”
 - Enter Relativity Theory and Quantum Mechanics
- 1896-1897 Becquerel, Röntgen, Marie & Pierre Curie discover radiation
- 1897: J.J Thomson noted cathode rays are quantized particles, charge to mass ratio: discovery of electrons
- 1900: Planck: The blackbody spectrum can be explained by introducing emission of light in *quanta* \hbar
- 1905: Einstein: photo electric effect: light is quantized: photon
 - Scattering behaviour verified in 1923 by Arthur Holly Compton
- 1911: Rutherford: nucleus hydrogen is a proton
- 1932: Chadwick: discovery of the neutron
 - Neutral particle with the mass of a proton

Griffiths §1.1 and §1.2

Black body spectrum: Planck



Photoelectric Effect: Einstein

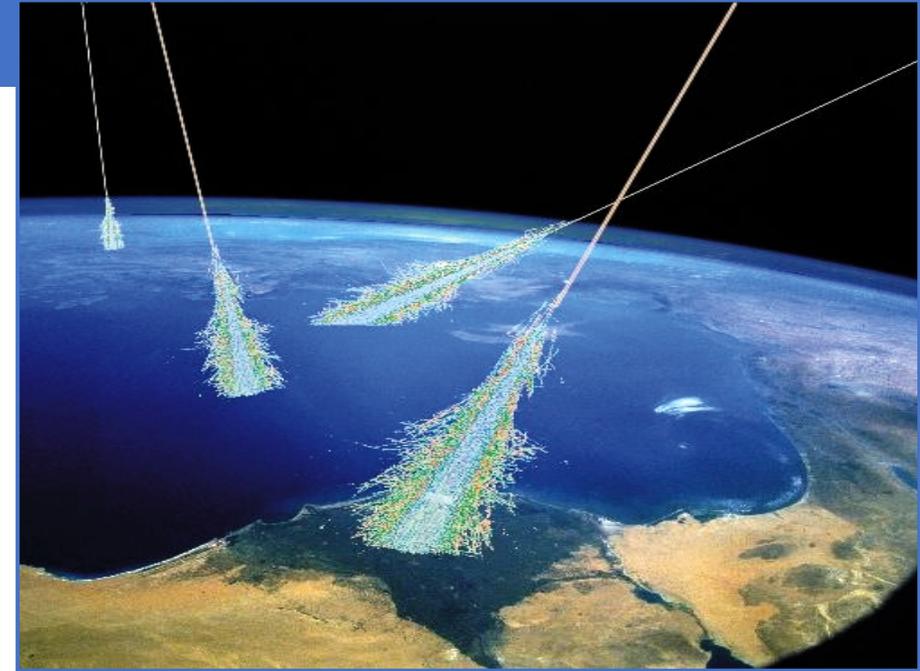


Mesons 1934 - 1947

Griffiths §1.3

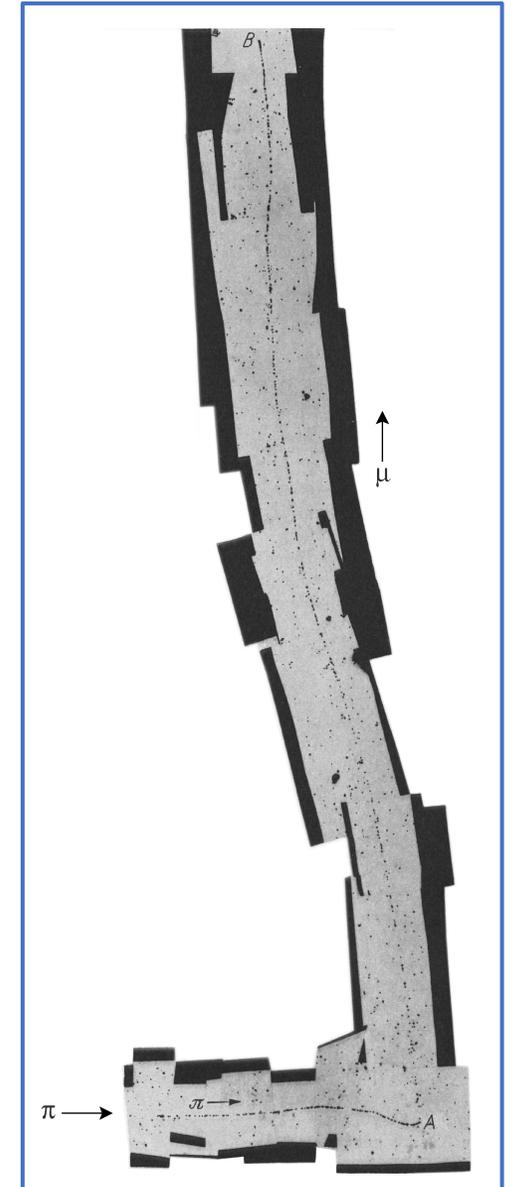
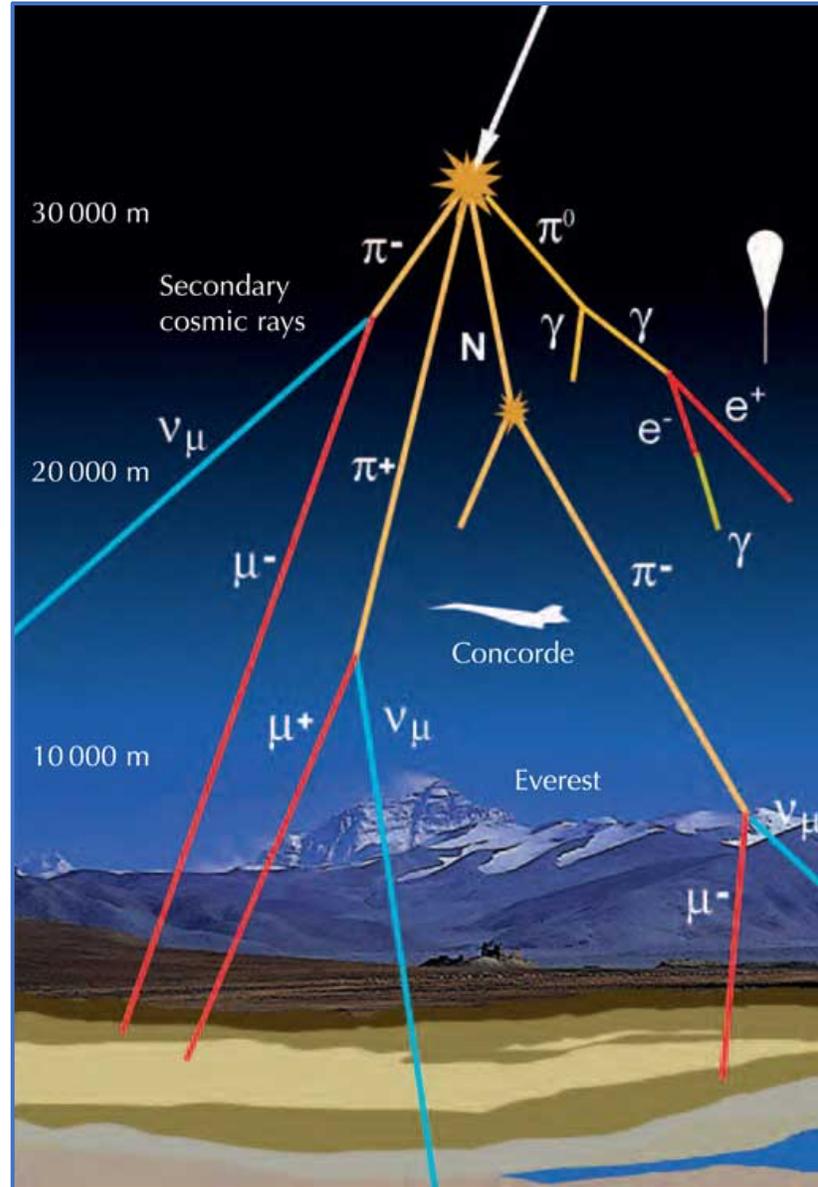
- The nucleus is held together by strong force, mediated by pions or pi-mesons.
- Can we see these pion quanta of mass $\sim 150 \text{ MeV}$?
- In 1937 particles were detected in cosmic rays:
 - Their mass was a bit too light: $m = 105 \text{ MeV}$
 - *They did not interact strongly with nuclei ?!*
- It turned out to be a muon, heavy version of the electron
 - “Who ordered that?”: Isaac Rabi
- Particles:
 - Hadrons (p, n), Mesons (π), Leptons (e, μ)

Lepton: Greek “small” or “thin”: small mass, feels no nuclear force
Hadron: Greek “thick” : large mass, feels nuclear interaction
Meson: Greek “middle”: medium mass, feels nuclear interaction

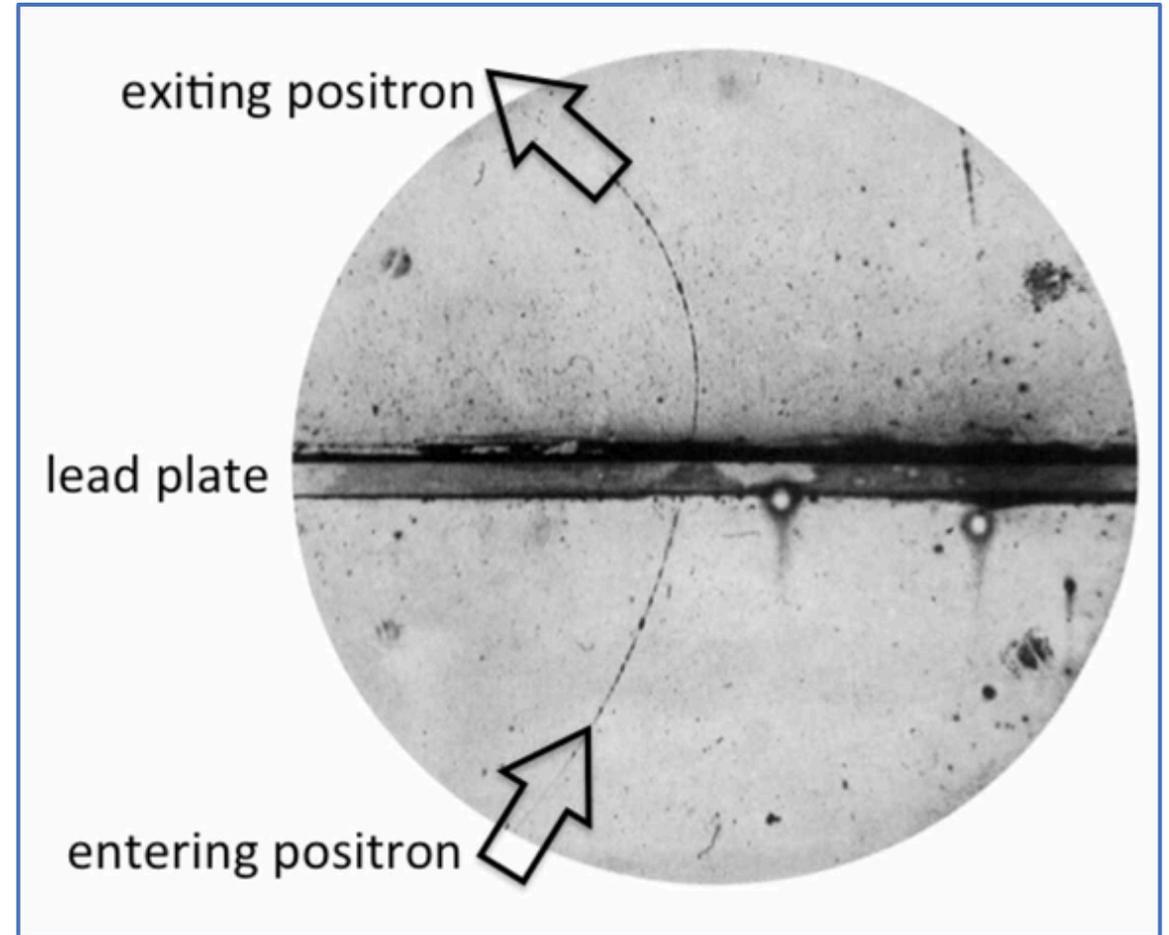


Discovery of the pion - 1947

- Powell, 1947
 - Go to mountain top
 - Photographic emulsion
- Observes that cosmic rays include muons and pions
 - $m_{\pi} = 140 \text{ MeV}/c^2$
 - $m_{\mu} = 105 \text{ MeV}/c^2$
- A pion can decay into a muon, which can again decay into an electron
- The pion was Yukawa's meson



- In 1928 Dirac predicted the existence of antimatter particles, combining relativity theory and quantum mechanics
 - We will learn about Dirac's equation later
- Exercise: convince yourself that Klein-Gordon equation: $E^2 = p^2c^2 + m^2c^4$ is in agreement with the relativistic formulae: $E = m\gamma c$ and $p = m\gamma v$
- Dirac: E can have positive and negative solutions:
 - Positive: matter particles (electron)
 - Negative antimatter particles (positron)
- In 1932 the positron was discovered by Anderson



Question: How did he know which direction the particle went?

Antimatter particles 1928 - 1956

- Feynman Stückelberg interpretation of particles (more in lecture 3):
 - The *negative energy* solution of a *particle* corresponds with the *positive energy* solution of an *antiparticle* going backwards in time.

$$\psi_{\pm}(\vec{x}, t) = a_{\pm} e^{\frac{i}{\hbar}(\vec{x}\vec{p} - Et)}$$

- CPT theorem: an antiparticle *is* an anti-particle going backwards in time
- For each particle p there exists a mirror anti-particle \bar{p} in nature.
 - Berkeley Bevatron: discovery anti-proton (1954, Chamberlain, Segré) and discovery anti-neutron (1956, Cork).
 - The antiparticle has the *same mass, lifetime and spin, but opposite internal quantum numbers like charge*.
 - Matter and antimatter have identical interactions. Definition what is what?
- Wheeler: is there only one electron in the entire universe?
- Question: is there also an anti-photon?

Antiparticle and Crossing Symmetry

- Crossing symmetry:

If: $A + B \rightarrow C + D$, then also possible:

$$A \rightarrow \bar{B} + C + D$$

$$A + \bar{C} \rightarrow \bar{B} + D$$

$$\bar{C} + \bar{D} \rightarrow \bar{A} + \bar{B}$$

Limited by energy conservation.

- Example:

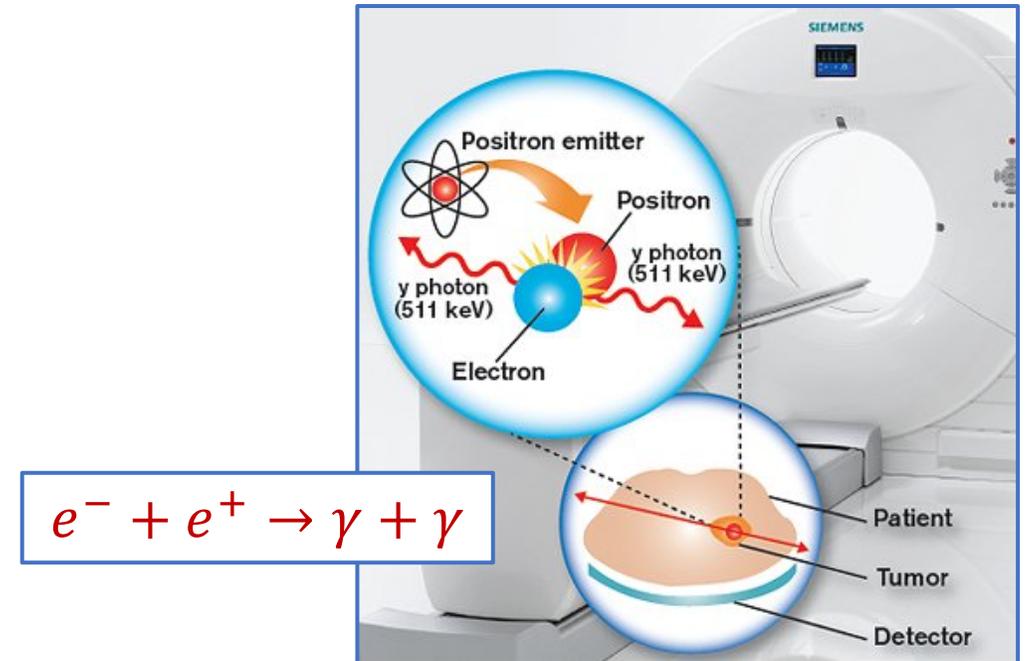
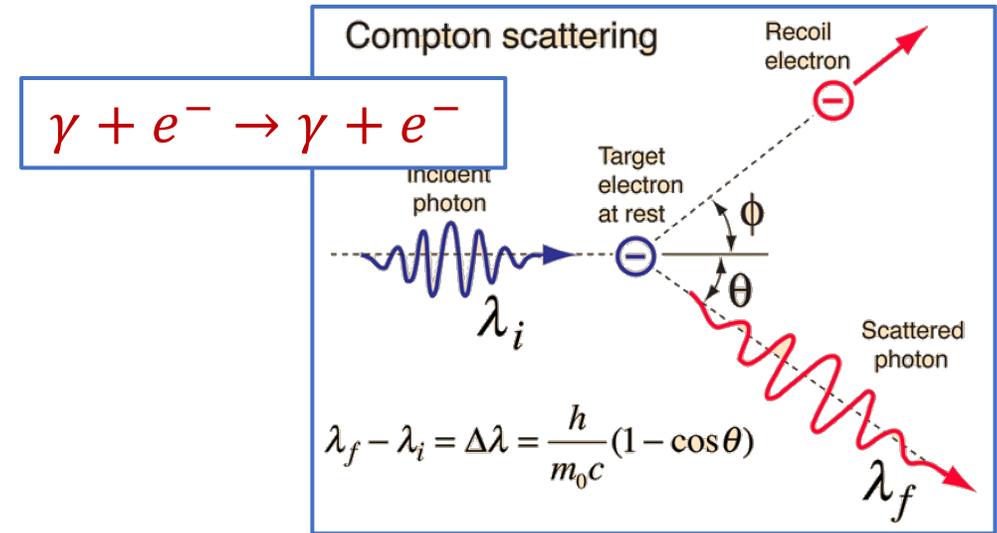
Compton scattering = pair annihilation

$$\gamma + e^- \rightarrow \gamma + e^- = e^- + e^+ \rightarrow \gamma + \gamma$$

- General symmetry between matter and antimatter (CPT theorem)

→ Why is the universe matter dominated?

→ Subtle features in the weak interaction!



Antiparticle and Crossing Symmetry

- Crossing symmetry:

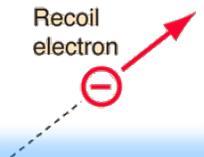
If: $A + B \rightarrow C + D$, then also possible:

$$\gamma + e^- \rightarrow \gamma + e^-$$

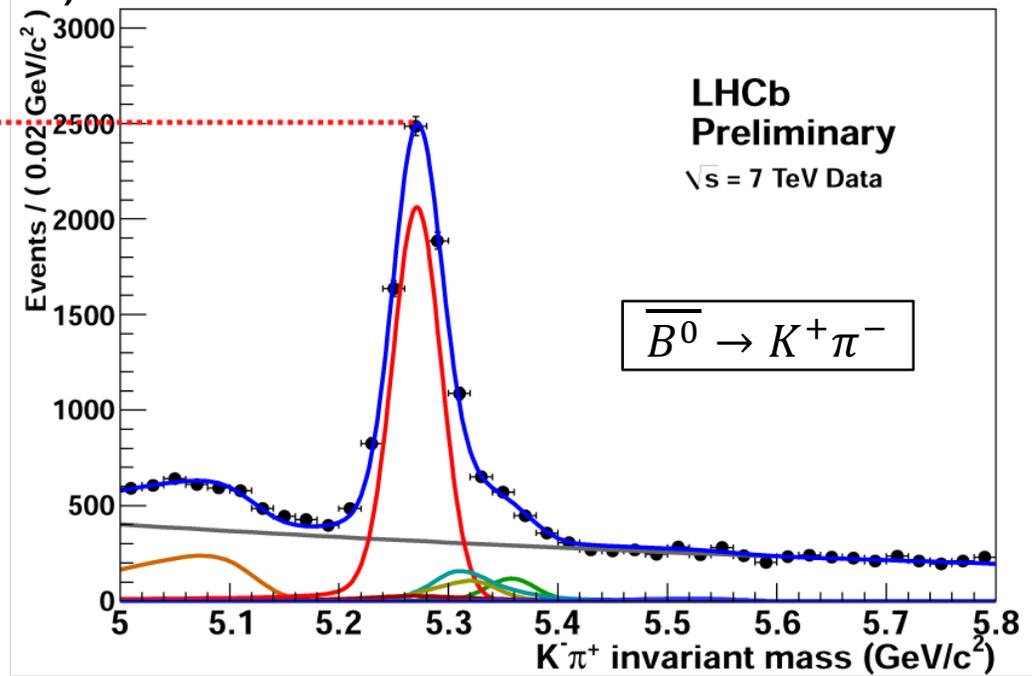
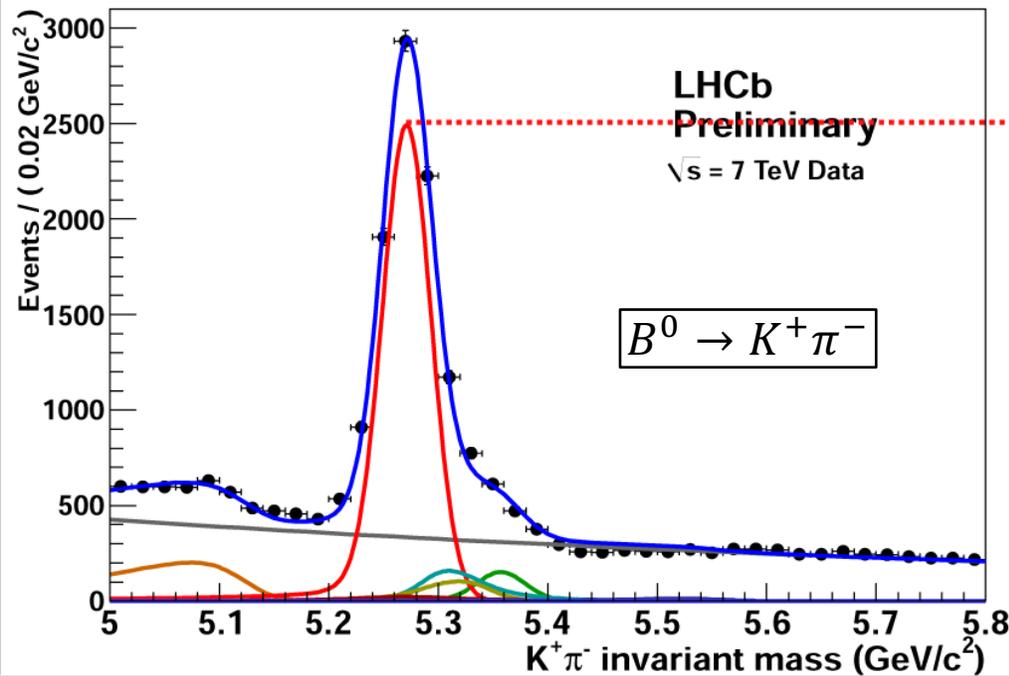
Compton scattering

Recoil electron

Target



(2012)



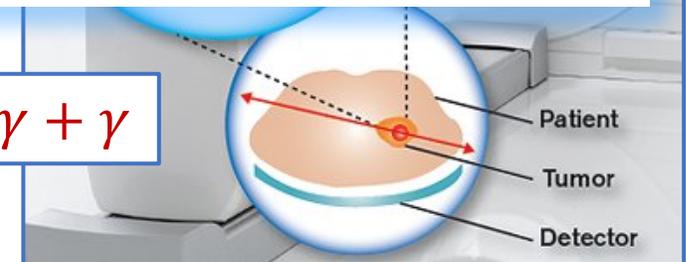
- Example

- Generation of antimatter (CPT theorem)

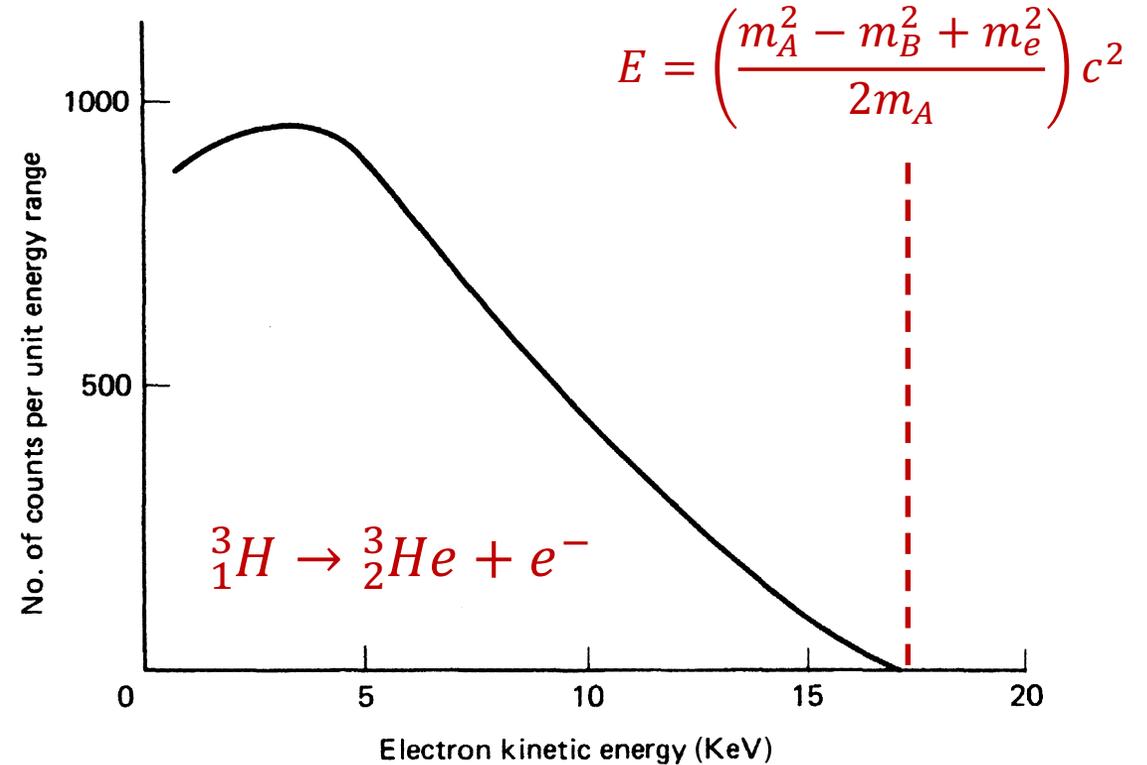
→ Why is the universe matter dominated?

→ Subtle features in the weak interaction!

$$e^- + e^+ \rightarrow \gamma + \gamma$$

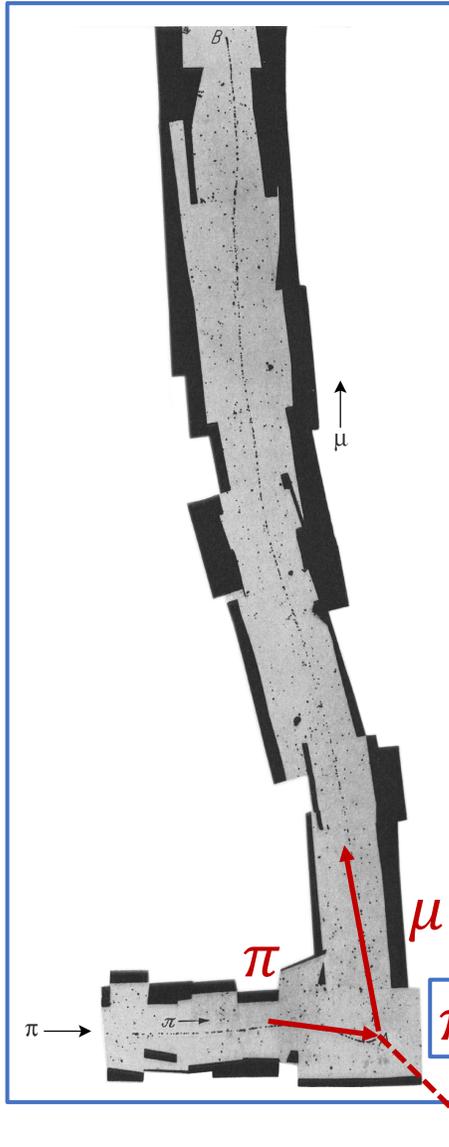


- Nuclear beta decay: $A \rightarrow B + e^-$
 - Exercise: calculate the kinetic energy of the electron.
 - Observed kinetic energy in tritium decay is a *spectrum*
- Niels Bohr was thinking to abandon the law of conservation of energy(!)



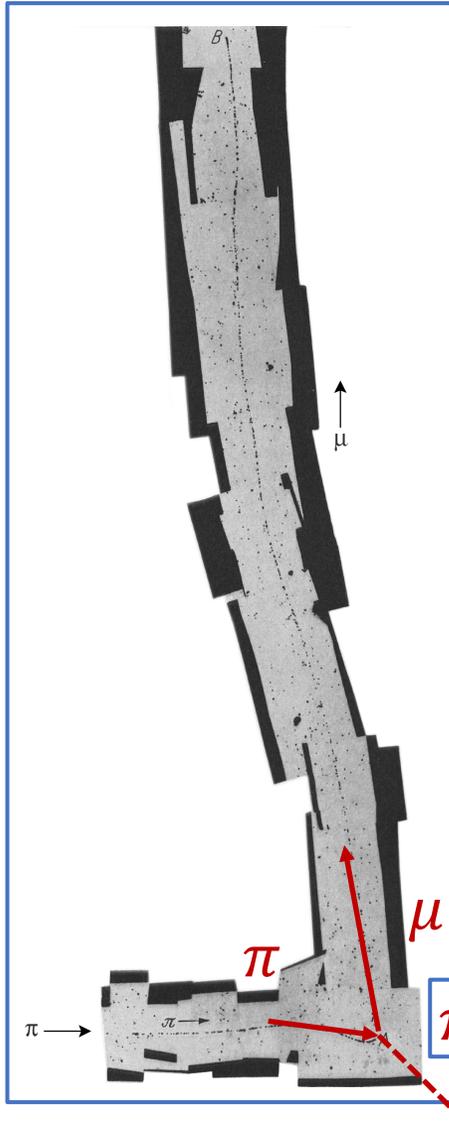
- Pauli proposed that an undetected neutral particle was produced
 - Proposed the name neutron
 - Fermi presented beta decay theory, neutrino: $n \rightarrow p + e^- + \bar{\nu}$

Neutrinos 1930 - 1962

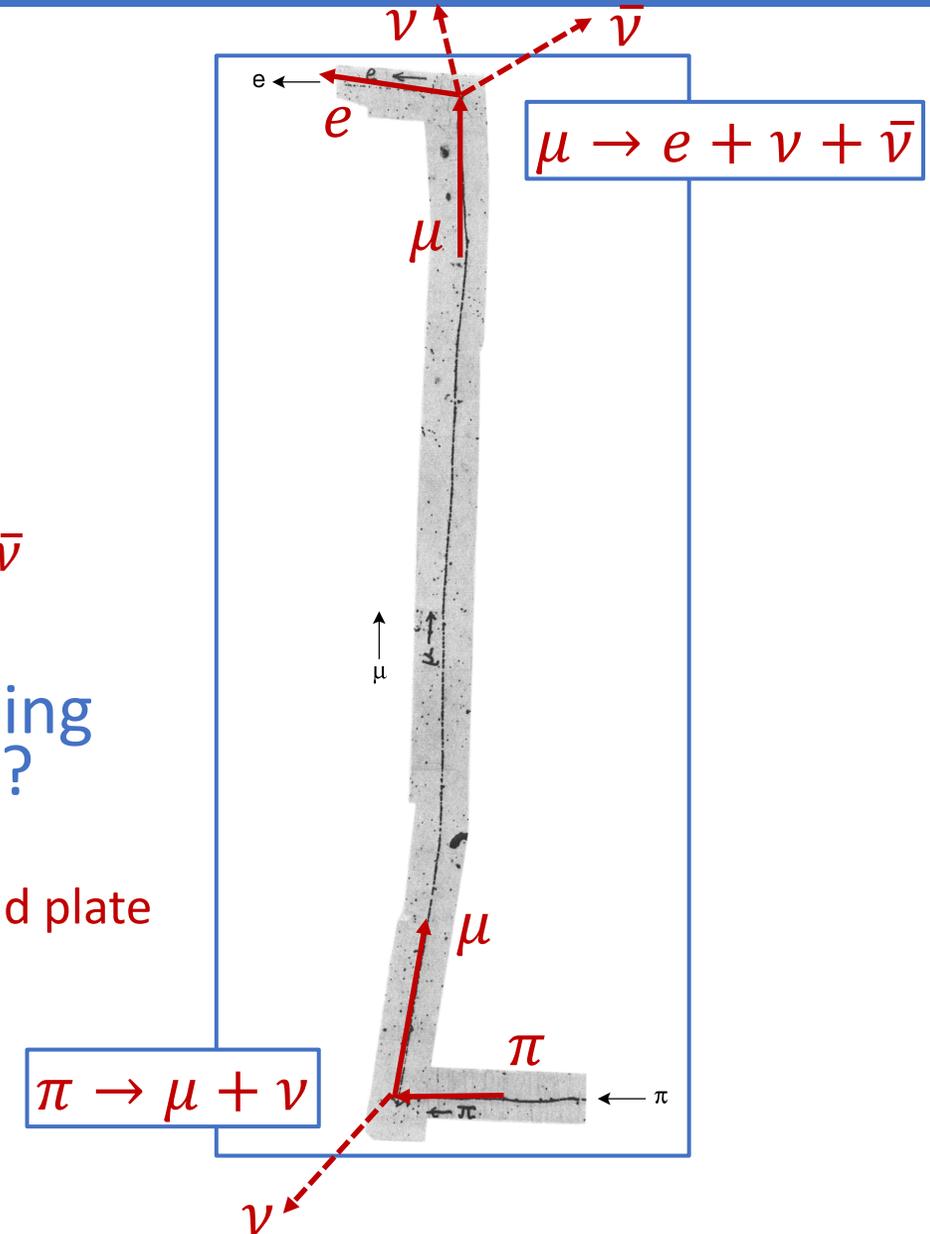


- Powell's discovery of muon and pion
 - Pion decay: $\pi \rightarrow \mu + \nu$

Neutrinos 1930 - 1962



- Powell's discovery of muon and pion
 - Pion decay: $\pi \rightarrow \mu + \nu$
- Later discovery of Powell
 - Pion *and* muon decays: $\pi \rightarrow \mu + \nu$
followed by: $\mu \rightarrow e + \nu + \bar{\nu}$
- Neutrinos: are they a bookkeeping device or are they real particles?
 - *Very weak* interaction
 - Can penetrate 1000 lightyears thick lead plate
 - What is their mass? $m_\nu \neq 0$?



Observation of neutrinos

- 1955 Cowan and Reines observe “inverse beta decay”
 - Water tank next to Nuclear Reactor
 - Antineutrinos colliding with protons: $\bar{\nu} + p^+ \rightarrow n + e^+$
 - Inverse beta decay
- Are neutrinos their own antiparticles, like photons?
 - From Cowan and Reines and crossing we know that: $\nu + n \rightarrow p^+ + e^-$ must exist
 - Davis and Hamer looked for: $\bar{\nu} + n \rightarrow p^+ + e^-$ It does **not** exist
 - Neutrino is not its own antiparticle. Or is there more going on?
- What distinguishes a neutrino from an anti-neutrino?
 - A nice research topic: “Dirac” neutrinos vs “Majorana” neutrinos

Lepton Number and Lepton Flavor

- 1953, Introduction Lepton number

- Leptons (e^- , μ^- , ν) have quantum number $L = 1$
- Antileptons ($\bar{e} = e^+$, $\bar{\mu} = \mu^+$, $\bar{\nu}$) have quantum number $L = -1$
- Lepton number is conserved in reactions, eg:

$$\begin{array}{cccccc} \pi^- & \rightarrow & \mu^- & + & \bar{\nu} & \quad \text{or} \quad \pi^+ & \rightarrow & \mu^+ & + & \nu \\ L: & 0 & 1 & -1 & & 0 & -1 & & & \end{array}$$

- Lepton Flavor: how about: $\mu^- \rightarrow e^- + \gamma$? It is not observed!

- Each lepton ‘family’ has its own lepton number conservation, eg:

$$\begin{array}{cccc} \mu^- & \rightarrow & e^- & + & \bar{\nu}_e & + & \nu_\mu \\ L_\mu: & 1 & 0 & 0 & 1 & & \\ L_e: & 0 & 1 & -1 & 0 & & \end{array}$$

Lepton number is conserved for each type (‘generation’) separately

- Proven in 1962: $\bar{\nu}_\mu + p \rightarrow \mu^+ + n$ was observed,

while: $\bar{\nu}_\mu + p \rightarrow e^+ + n$ was not!

- How did they know? Because these neutrino’s were produced by pion decays into a muon at Brookhaven lab.

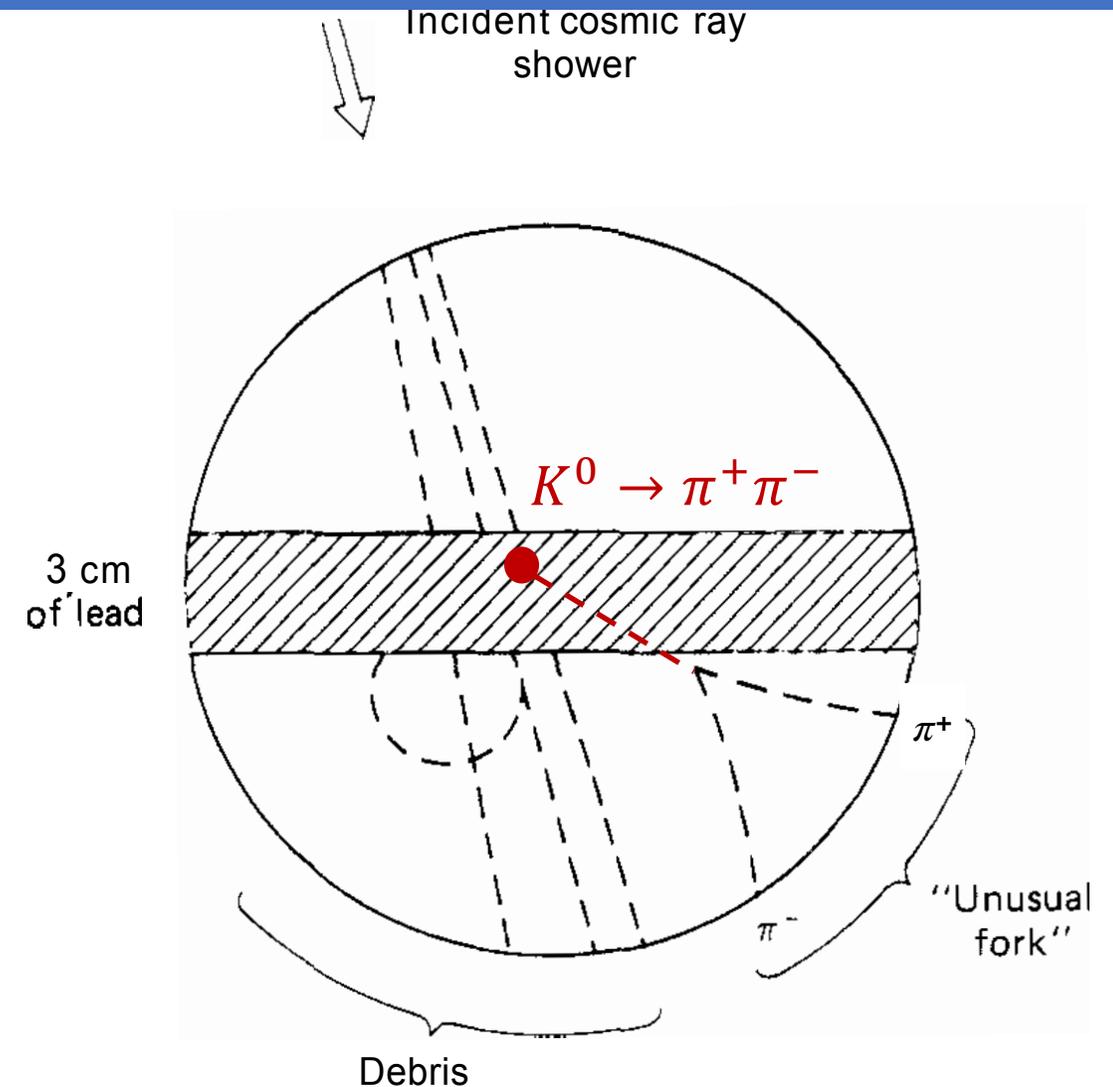
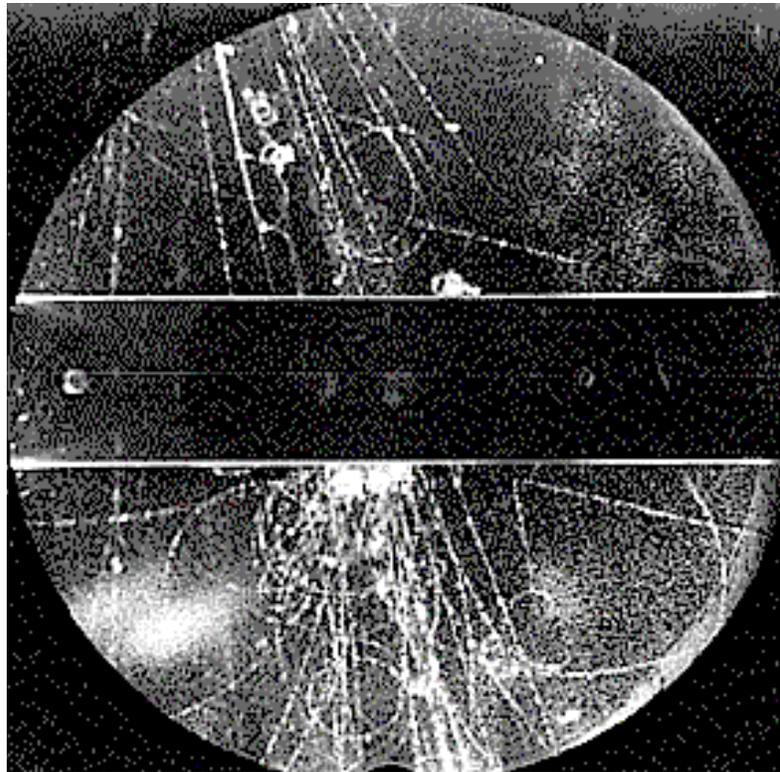
Lepton summary 1962 - 1976

| | Lepton number | Electron number | Muon number |
|-----------------|------------------|--------------------|----------------|
| Leptons | | | |
| e^- | 1 | 1 | 0 |
| ν_e | 1 | 1 | 0 |
| μ^- | 1 | 0 | 1 |
| ν_μ | 1 | 0 | 1 |
| Antileptons | | | |
| e^+ | -1 | -1 | 0 |
| $\bar{\nu}_e$ | -1 | -1 | 0 |
| μ^+ | -1 | 0 | -1 |
| $\bar{\nu}_\mu$ | -1 | 0 | -1 |

- Are neutrinos massless? Not exactly → Neutrino oscillations
 - Neutrino's can oscillate to different neutrino type and back! (good research topic)

Strangeness (1947 – 1960)

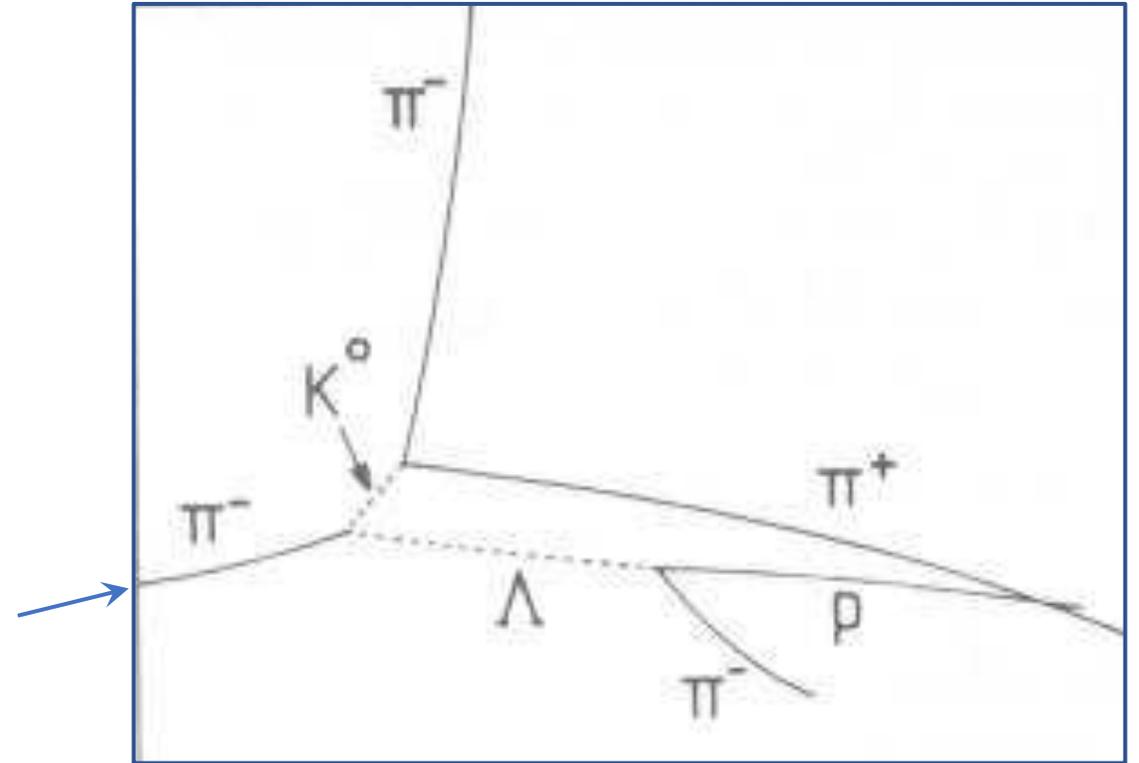
- Rochester and Butler observed strange “V-prongs” in cosmic rays:



- Strange: produced copiously, but decay slowly!
 - Abraham Pais: They are produced with the strong force, but they decay with the weak force.

Similarly observed: $\Lambda \rightarrow p^+ \pi^-$

Example of associated strangeness production



Bubble chamber picture of the associated reaction $\pi^- + p \rightarrow K^0 + \Lambda$. Incoming pion is indicated by the arrow. The unseen neutral particles K^0 and Λ are detected by their “ V^0 ” decays: $K^0 \rightarrow \pi^0 + \pi^-$ and $\Lambda \rightarrow \pi^- + p$.

It turns out these strange particles are always produced in pairs.

Strangeness

- Also observed: $K^+ \rightarrow \pi^+ + \pi^+ + \pi^- \rightarrow M_K \sim 500 \text{ MeV}$; it's a meson
- 1952, Brookhaven cosmotron: new strange *baryons*: Σ ($\sim 1.2 \text{ GeV}$), Ξ ($\sim 1.3 \text{ GeV}$)
- In production (strong interaction) conserve *baryon number* as well as *strangeness*

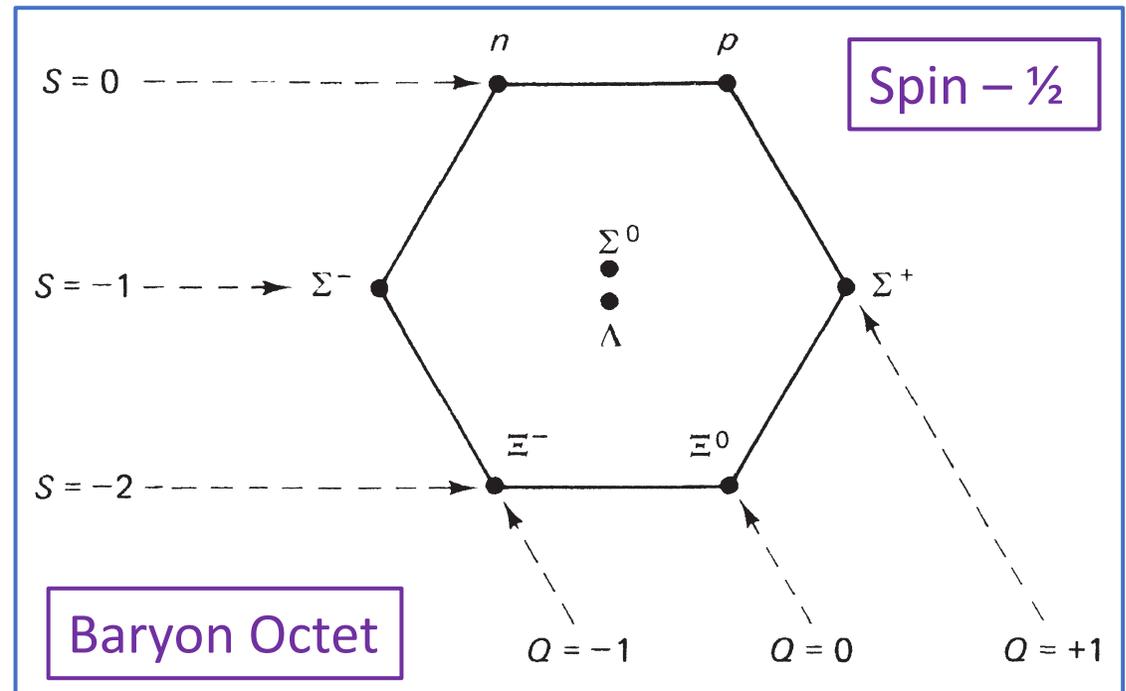
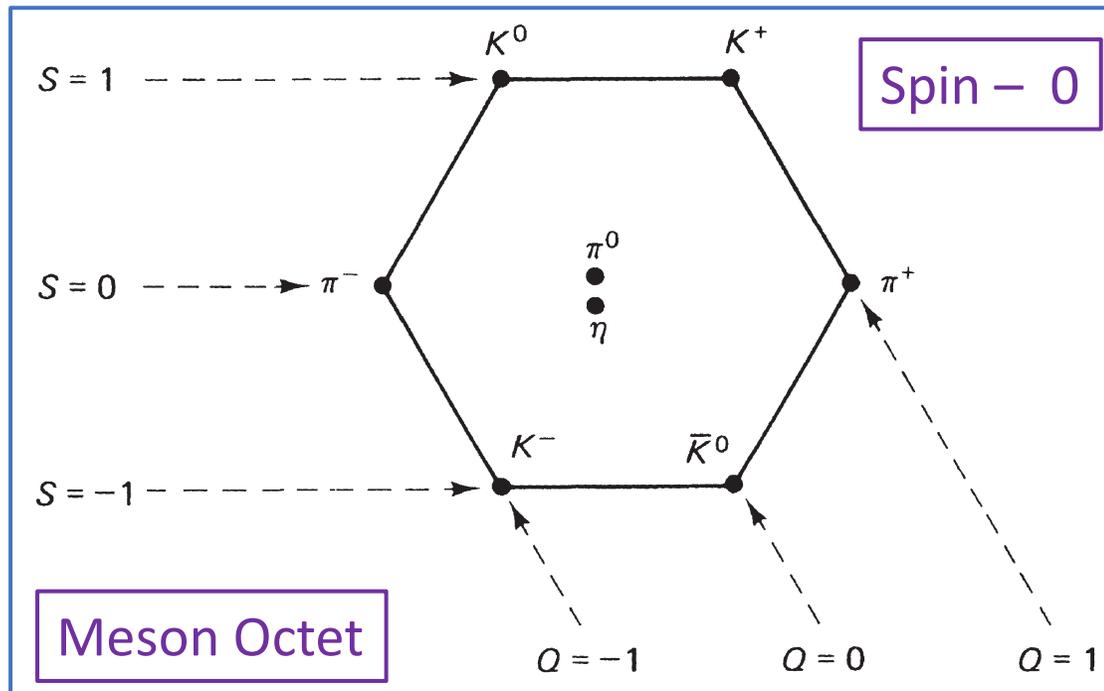
| | B: | S: | OK? |
|--|---------------------------|----------------------------|-----|
| $\pi^- + p \rightarrow K^+ + \Sigma^-$ | $0 + 1 \rightarrow 0 + 1$ | $0 + 0 \rightarrow 1 + -1$ | Yes |
| $\rightarrow K^0 + \Lambda$ | $0 + 1 \rightarrow 0 + 1$ | $0 + 0 \rightarrow 1 + -1$ | Yes |
| $\rightarrow \pi^+ + \Sigma^-$ | $0 + 1 \rightarrow 0 + 1$ | $0 + 0 \rightarrow 0 + -1$ | No |
| $\rightarrow K^+ + K^-$ | $0 + 1 \rightarrow 0 + 0$ | $0 + 0 \rightarrow 1 + -1$ | No |

- In decay (weak force) *strangeness is not conserved*: long lifetimes
eg. decays: $\Lambda \rightarrow p^+ + \pi^-$; $\Sigma^+ \rightarrow n + \pi^+$
- Electric charge is always conserved!

The Particle Zoo and the Eightfold Way

Griffiths §1.7

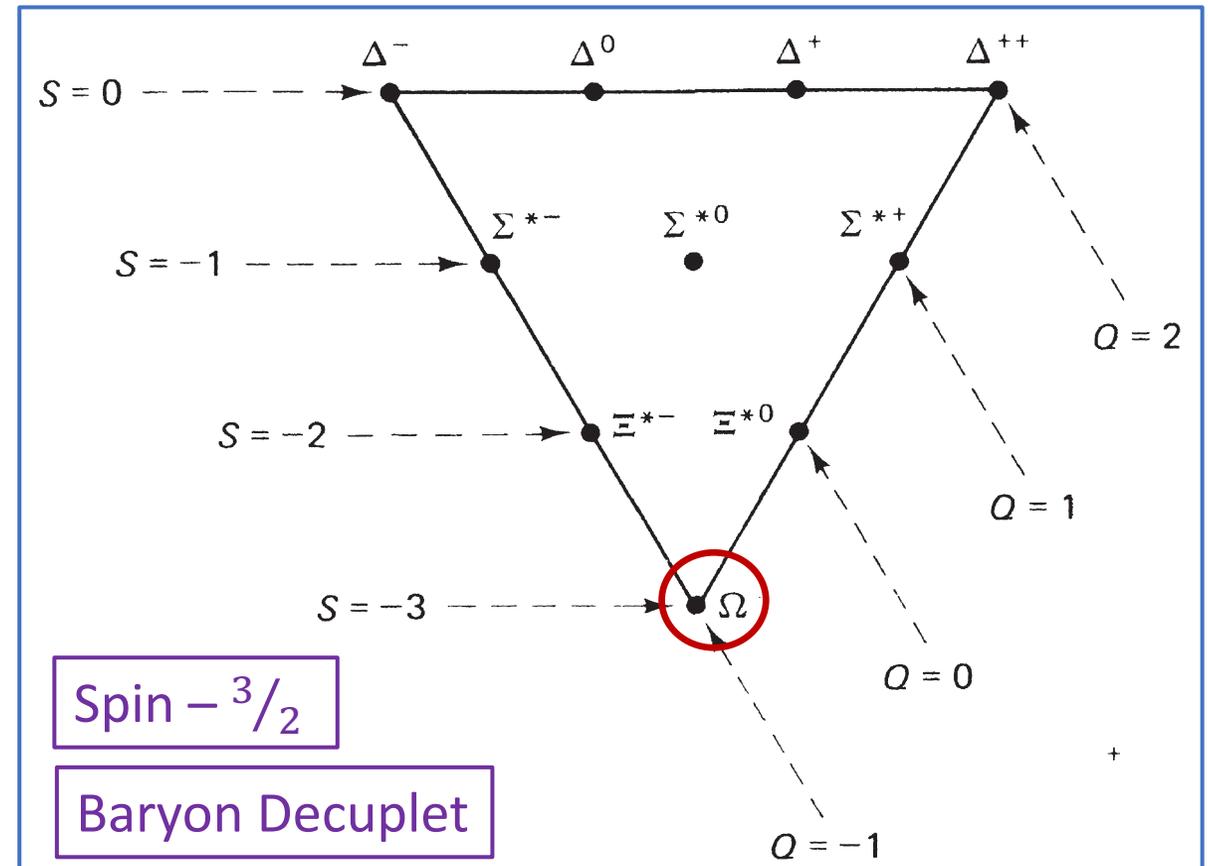
- So many particles! *“The finder of a new elementary particle should be punished by a 10,000 \$ fine!”* - Willis Lamb, 1955.
- Gell-Mann (1961): Make a classification a la Periodic Table



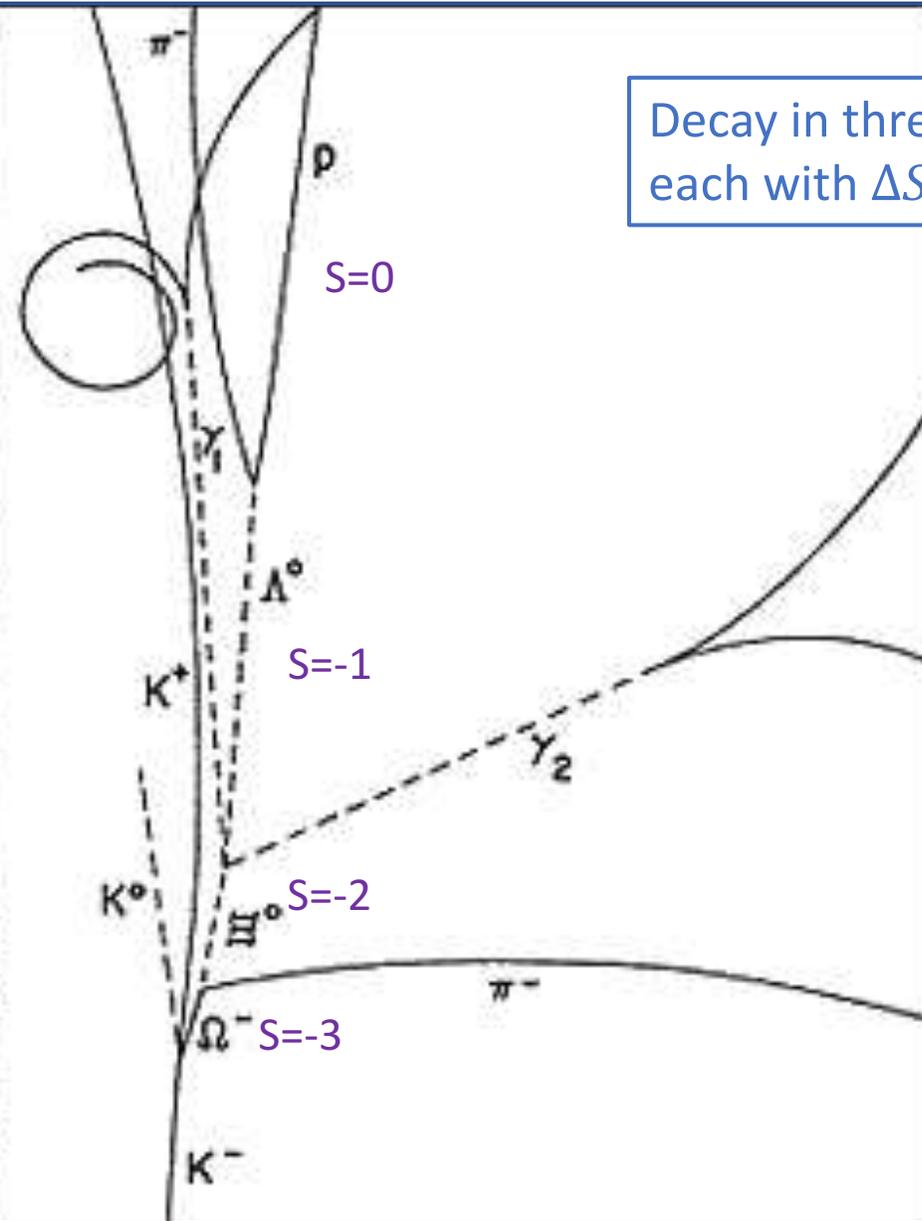
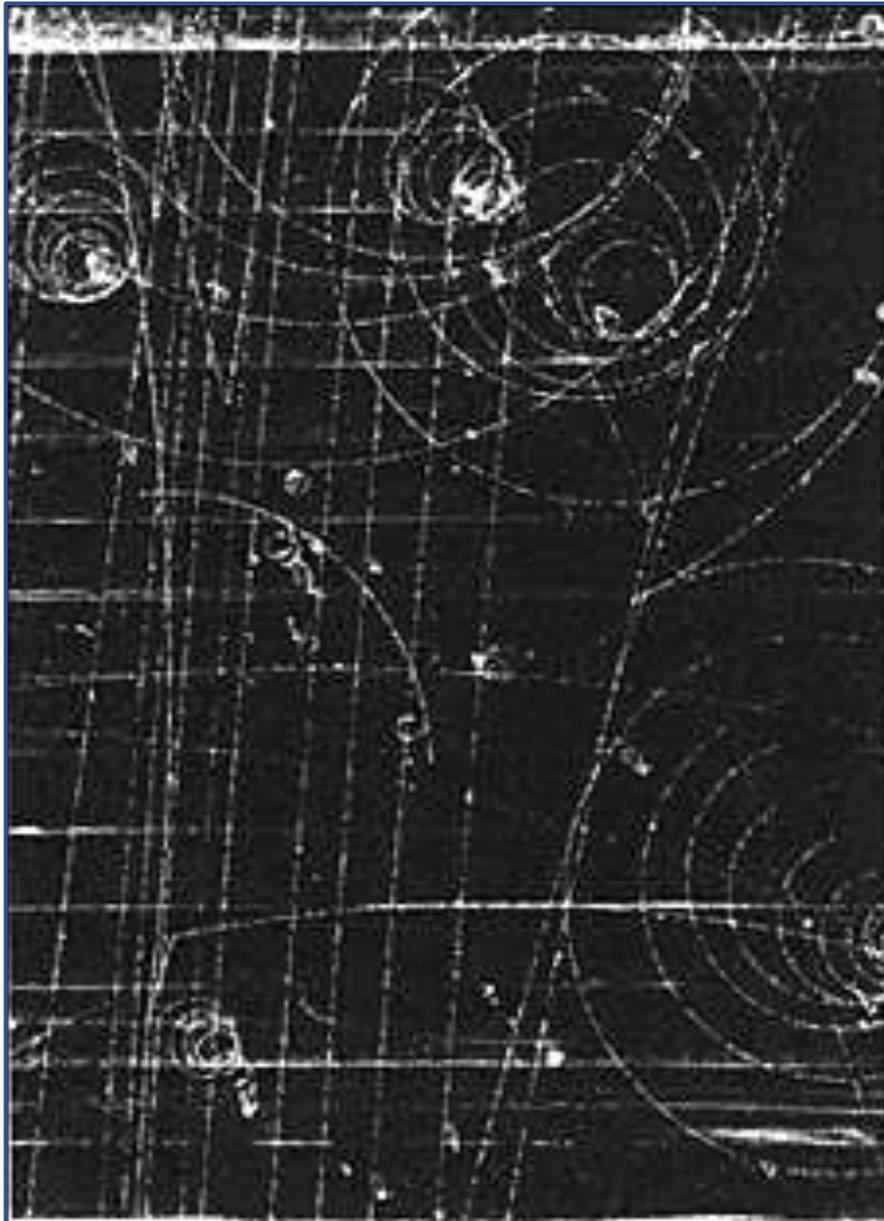
The Particle Zoo and the Eightfold Way

- So many particles! *“The finder of a new elementary particle should be punished by a 10,000 \$ fine!”* - Willis Lamb, 1955.
- Gell-Mann (1961): Make a classification a la Periodic Table

- For heavier baryon particles (spin- $3/2$) there is a decuplet
 - The reason that spin- $1/2$ baryons form an octet and spin- $3/2$ a decuplet is far from trivial.
- The Ω particle was not known yet:
 - Mass and lifetime was predicted
 - Observed in 1964
- Octets and decuplets suggest an underlying structure! – quarks!



Discovery of the Omega particle

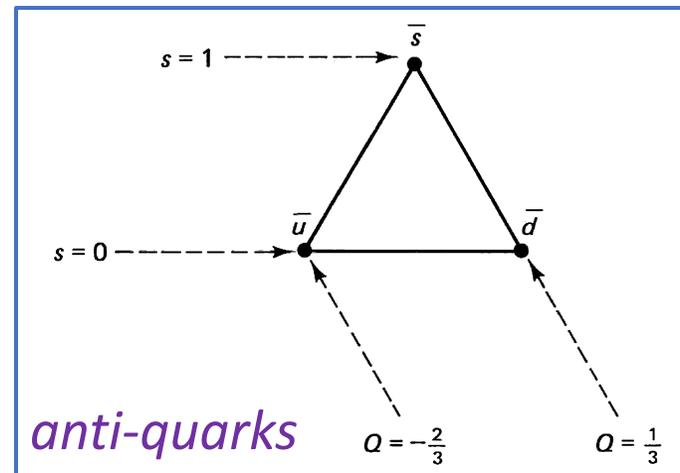
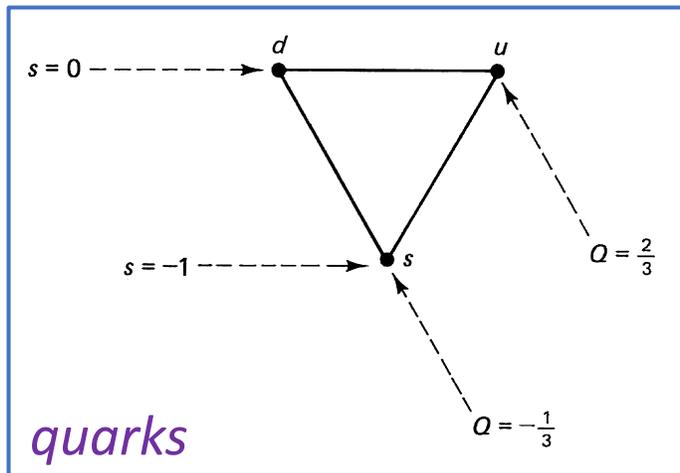


Decay in three steps,
each with $\Delta S = -1$

The Quark Model (1964)

Griffiths §1.8

- Gell-Mann and Zweig independently proposed that elementary particles are composed of spine- $\frac{1}{2}$ *quarks: up, down, strange:*

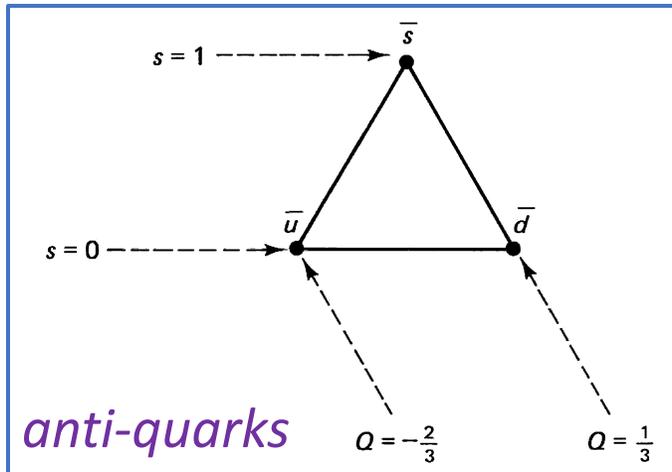
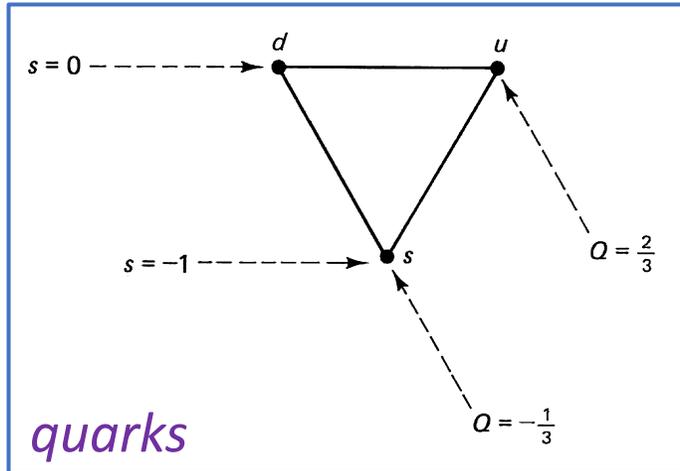


- Baryons: particle consisting of 3 quarks or antiquarks ($q q q$) or ($\bar{q} \bar{q} \bar{q}$)
 - Proton= uud , neutron= udd , etc
- Mesons: particles consisting of 1 quark and 1 anti-quarks: ($q \bar{q}$)
 - Pions: $\pi^+ = u\bar{d}$, $\pi^0 = u\bar{u}+d\bar{d}$, $\pi^- = d\bar{u}$
 - Kaons: $K^+ = u\bar{s}$, etc

Explains “elementary particles” as quark combinations, spin, strangeness etc.

The Quark Model (1964)

- Gell-Mann and Zweig independently proposed that elementary particles are composed of spine- $\frac{1}{2}$ *quarks: up, down, strange:*



The meson **nonet**

| $q\bar{q}$ | Q | S | Meson |
|------------|-----|-----|-------------|
| $u\bar{u}$ | 0 | 0 | π^0 |
| $u\bar{d}$ | 1 | 0 | π^+ |
| $d\bar{u}$ | -1 | 0 | π^- |
| $d\bar{d}$ | 0 | 0 | η |
| $u\bar{s}$ | 1 | 1 | K^+ |
| $d\bar{s}$ | 0 | 1 | K^0 |
| $s\bar{u}$ | -1 | -1 | K^- |
| $s\bar{d}$ | 0 | -1 | \bar{K}^0 |
| $s\bar{s}$ | 0 | 0 | ?? |

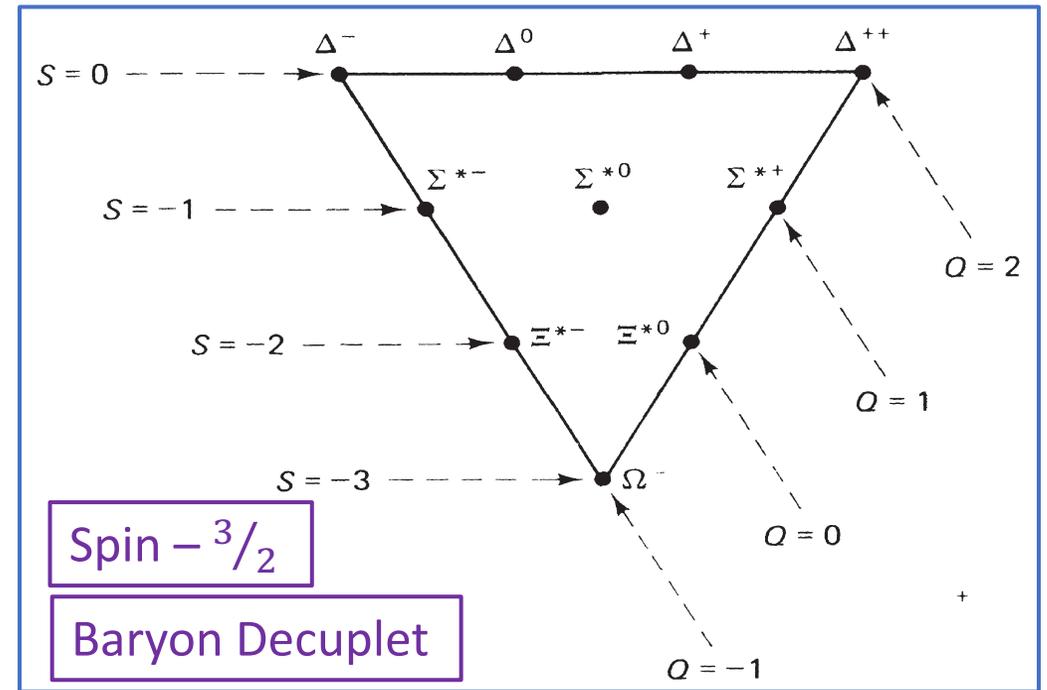
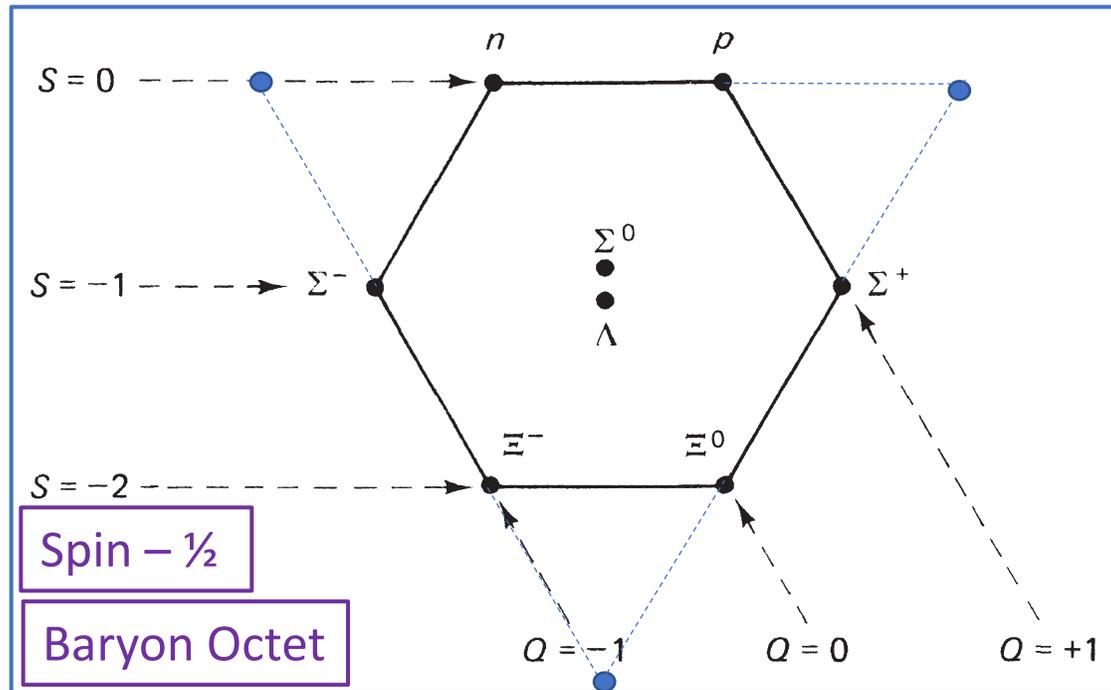
The baryon decuplet

| qqq | Q | S | Baryon |
|-------|-----|-----|---------------|
| uuu | 2 | 0 | Δ^{++} |
| uud | 1 | 0 | Δ^+ |
| udd | 0 | 0 | Δ^0 |
| ddd | -1 | 0 | Δ^- |
| uus | 1 | -1 | Σ^{*+} |
| uds | 0 | -1 | Σ^{*0} |
| dds | -1 | -1 | Σ^{*-} |
| uss | 0 | -2 | Ξ^{*0} |
| dss | -1 | -2 | Ξ^{*-} |
| sss | -1 | -3 | Ω^- |

- Complications: η' singlet, baryon octet:
 - Spin and (anti-)symmetrization of wave functions!*

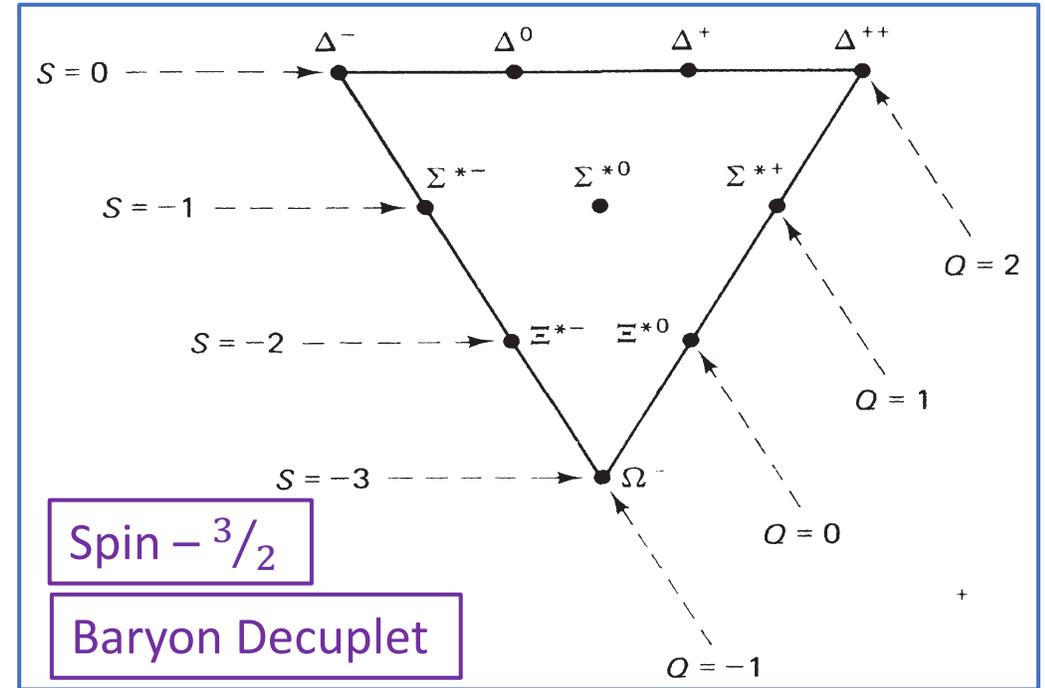
Complications

- The spin- $\frac{1}{2}$ octet is like the spin- $\frac{3}{2}$ decuplet with the corners missing.
 - Wave function has:
 - 3 identical quarks ($u u u$), ($d d d$), or ($s s s$)
 - 3 identical spin directions of quarks: $\uparrow\uparrow\uparrow$ or $\downarrow\downarrow\downarrow$



Desperate Measures

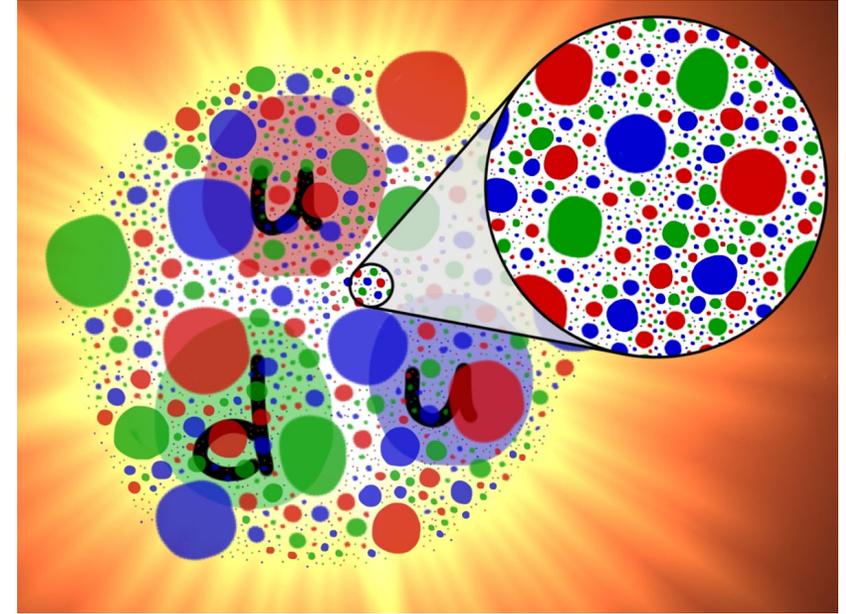
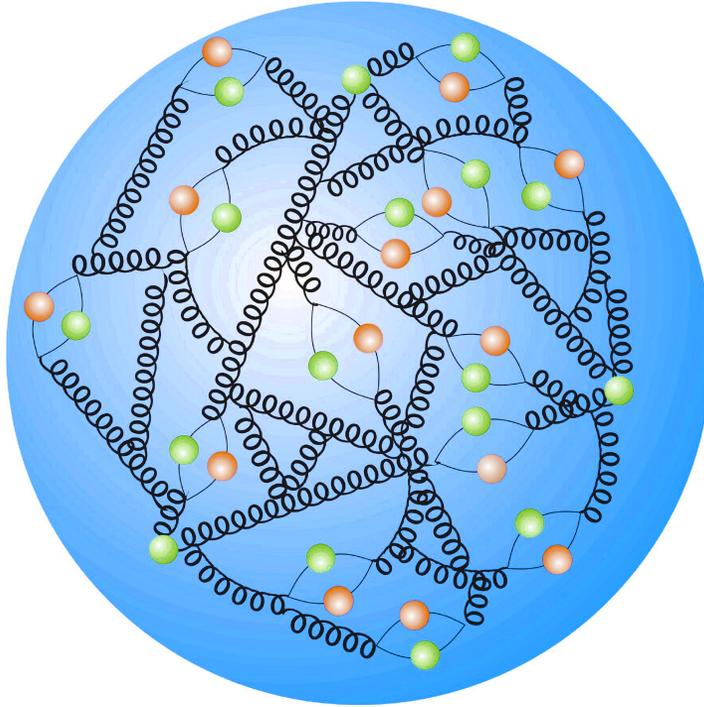
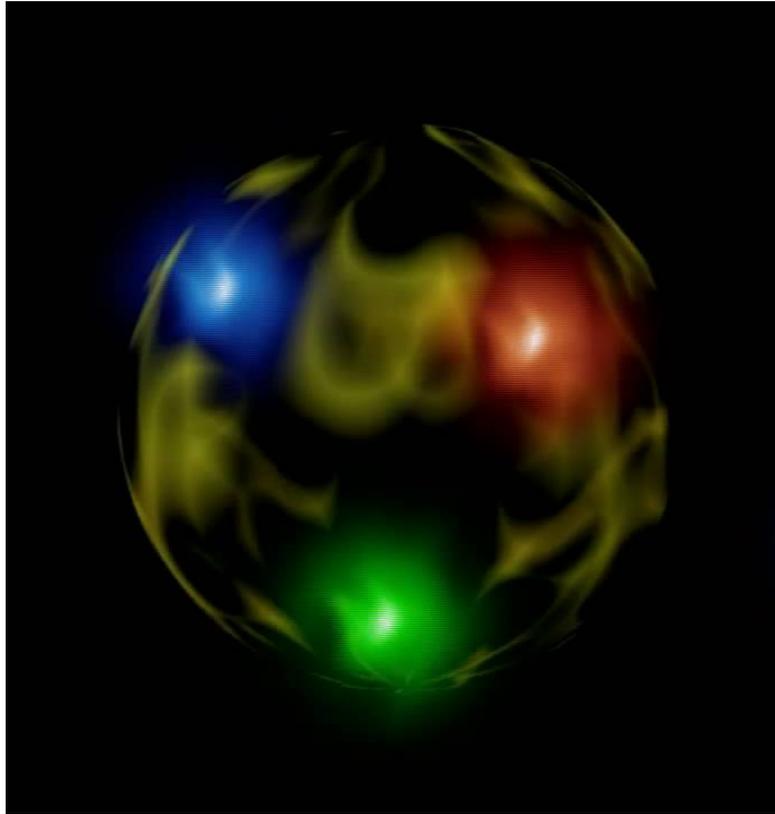
- A quantum mechanical problem: check Δ^{++} :
 - Wave function has:
 - 3 identical quarks ($u u u$), ($d d d$), or ($s s s$)
 - 3 identical spin directions of quarks: $\uparrow\uparrow\uparrow$ or $\downarrow\downarrow\downarrow$
 - Not allowed by Pauli-exclusion principle:
 - This wave function is symmetric under particle exchange
 - *Identical* spin- $\frac{1}{2}$ particles must have an asymmetric wave function under exchange of the particles



- Quarks differ by having an additional quantum number: **color**
 - A quark can have quantum number: “red”, “green”, “blue”
 - An anti-quark can carry quantum number: “anti-red”, “anti-green”, “anti-blue”
- All physical particles must be colorless (“confinement”):
 - baryons $\rightarrow r g b$, mesons $\rightarrow r r$, $g g$, or $b b$

No free quarks in nature!

How to make a mental picture of a proton?



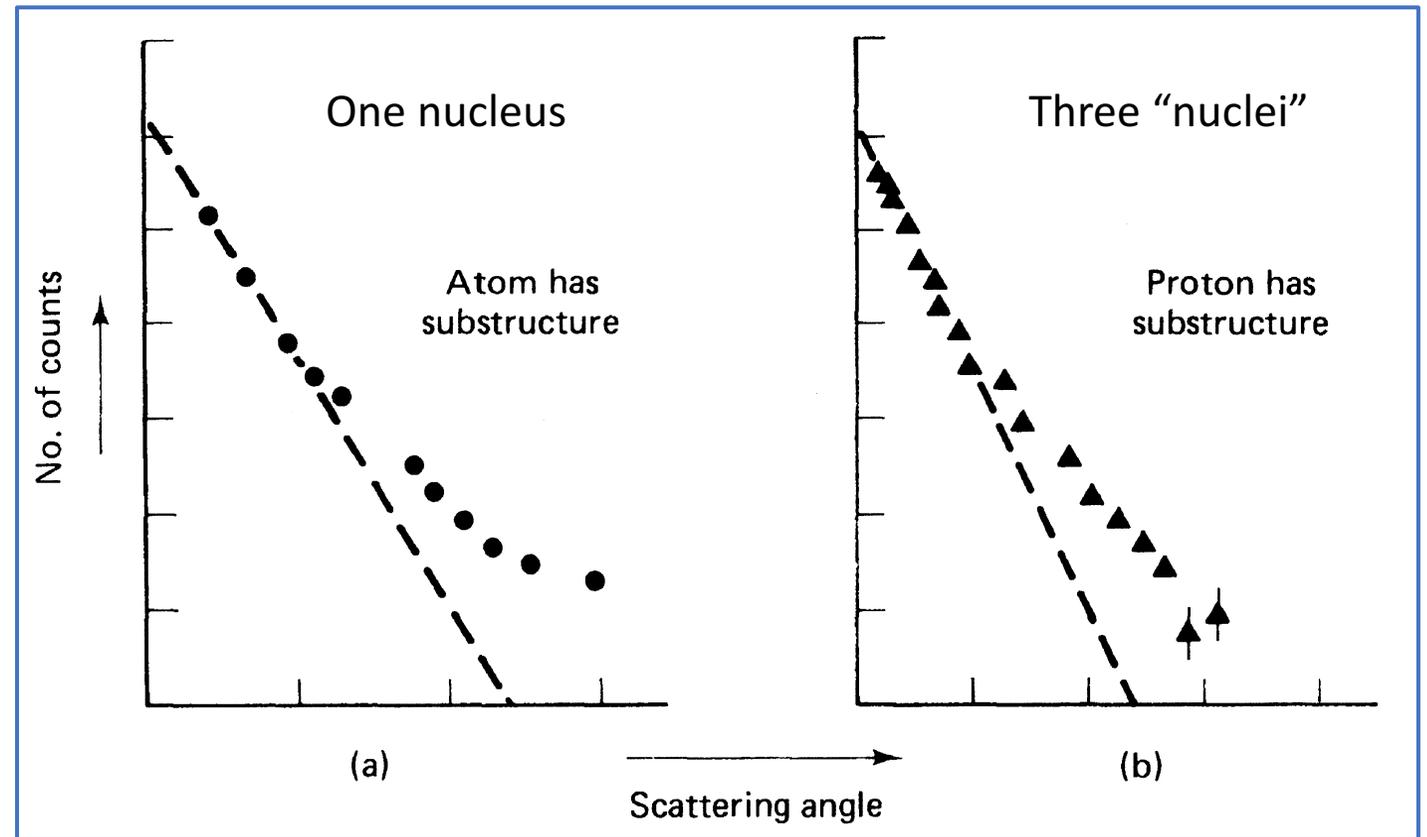
- Looking from "afar" there are three colored quarks: red, green, blue
- Zooming in it becomes a quantum foam of particles + antiparticles + force particles (gluons)

Deep Inelastic Scattering (“DIS”)

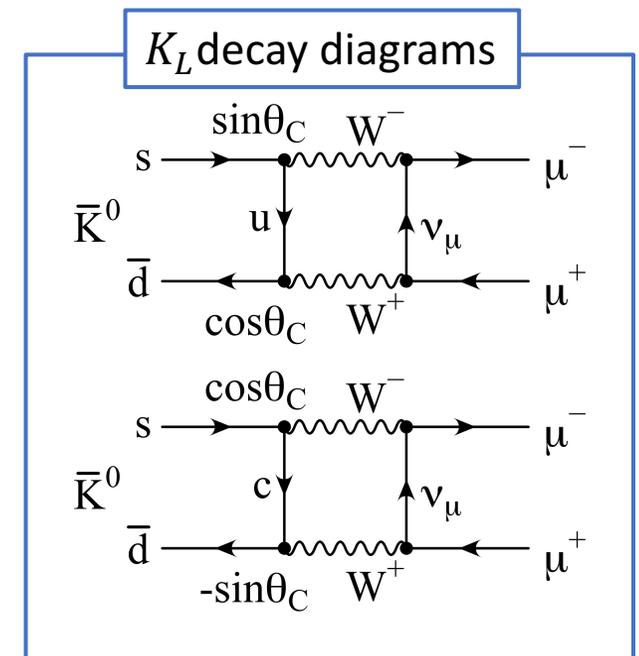
- Indeed individual quarks have never been observed.
 - Do they actually exist or are they just a mathematical bookkeeping tool?
- ~1970 SLAC: “DIS”
 - Proton substructure is seen similar to Rutherford scattering
- Quarks are real and they carry an additional quantum number which can have three values
 - “Color” is just a name

Research:

what is the principle behind confinement, ie. being colorless?



- Fundamental particles:
 - Why 4 Leptons: (e, ν_e) (μ, ν_μ) and 3 Quarks : (u, d, s) ?
 - 1974 Two groups discover a new particle: Ting at BNL (“ J ”) and Richter at SLAC (“ ψ ”)
 - J/ψ particle is special: very heavy $M \sim 3000 \text{ MeV}$, long lifetime $\tau \sim 1000 \times$ longer than heavy hadrons
 - new meson consisting of heavy charm quarks: $c\bar{c}$ → Enter: **charm** quantum number
- Existence of charm also solved the Glashow, Iliopoulos, Maiani (GIM) puzzle.
 - It explained why the K_L particle had a very long lifetime
- Other new particles were discovered soon afterwards
 - Mesons: $D^0 (c\bar{u})$, $D^+ (c\bar{d})$, $D_s^+ (c\bar{s})$, ...
 - Baryons: $\Sigma_c (uuc)$, $\Lambda_c (udc)$, $\Xi_c (usc)$, $\Omega_c (ssc)$, ...
- Similar to “strangeness”, “charm” is conserved in production (strong force), and violated in (weak force) decay

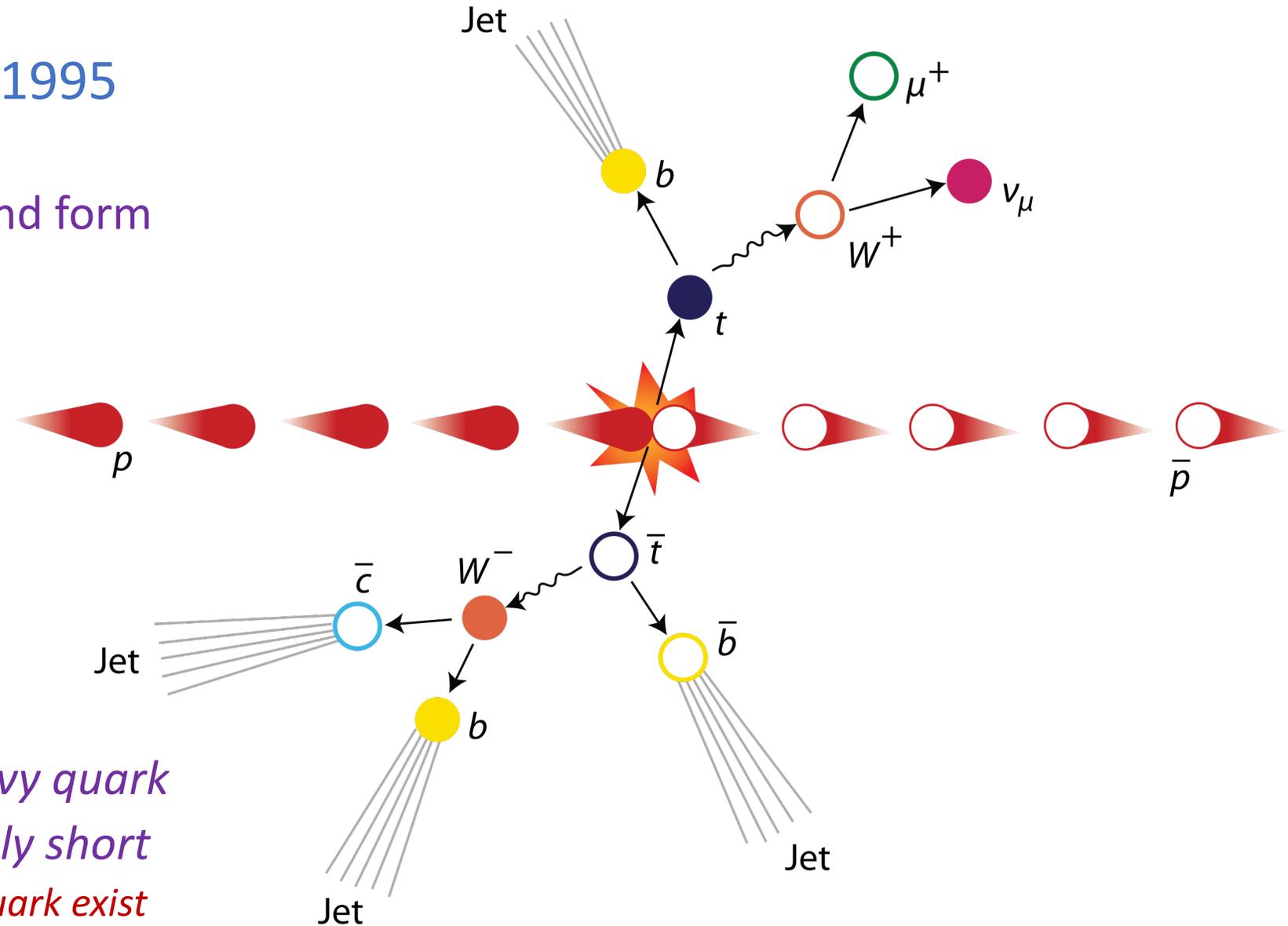


The November Revolution: 1974 - 1983

- 1974 Discovery of charm brings Lepton-Quark symmetry:
 - (ν_e, e) (ν_μ, μ) and (u, d) (c, s)
- 1975 Discovery of the τ - lepton breaks symmetry again
 - Also a corresponding ν_τ neutrino
- 1977 Discovery Υ ($b\bar{b}$) particle, consisting of *bottom* or *beauty* quarks
 - Baryons: 1980: Λ_b^0 (udb), 2006: Σ_b^+ (uub), 2007: Ξ_b^- (dsb),
 - Mesons: 1983: B^0 ($\bar{b}d$), B^- ($b\bar{u}$), later also: B_s^0 ($\bar{b}s$), B_c^+ ($\bar{b}c$)
 - First $B_c^+ \rightarrow B_s^0$ weak decay observed by J.A. de Vries *et al.*
- Terminology: upness, downness, strangeness, charm, beauty = “*Flavour*”
 - Quarks have *charge*, *flavor* and *color* quantum numbers
- Now 6 leptons and 5 quarks?
 - (ν_e, e) (ν_μ, μ) (ν_τ, τ) and (u, d) (c, s) (b, \dots)

Top quark

- Discovered at Fermilab 1995
 - $p + \bar{p} \rightarrow t + \bar{t}$
 - Top decay immediately and form so-called *jets*



- Top quark:
 - $m_t = 176 \text{ GeV}$, very heavy quark
 - $\tau_t = 5 \times 10^{-25} \text{ s}$, extremely short
 - *No bound states with top quark exist*

Standard Model of Elementary Particles

| | | three generations of matter (elementary fermions) | | | three generations of antimatter (elementary antifermions) | | | interactions / force carriers (elementary bosons) | |
|---------|--------|--|--|--|--|--|--|--|---|
| | | I | II | III | I | II | III | | |
| QUARKS | mass | $\approx 2.2 \text{ MeV}/c^2$ | $\approx 1.28 \text{ GeV}/c^2$ | $\approx 173.1 \text{ GeV}/c^2$ | $\approx 2.2 \text{ MeV}/c^2$ | $\approx 1.28 \text{ GeV}/c^2$ | $\approx 173.1 \text{ GeV}/c^2$ | 0 | $\approx 124.97 \text{ GeV}/c^2$ |
| | charge | $\frac{2}{3}$ | $\frac{2}{3}$ | $\frac{2}{3}$ | $-\frac{2}{3}$ | $-\frac{2}{3}$ | $-\frac{2}{3}$ | 0 | 0 |
| | spin | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | 1 | 0 |
| | | u up | c charm | t top | \bar{u} antiup | \bar{c} anticharm | \bar{t} antitop | g gluon | H higgs |
| | | $\approx 4.7 \text{ MeV}/c^2$ | $\approx 96 \text{ MeV}/c^2$ | $\approx 4.18 \text{ GeV}/c^2$ | $\approx 4.7 \text{ MeV}/c^2$ | $\approx 96 \text{ MeV}/c^2$ | $\approx 4.18 \text{ GeV}/c^2$ | 0 | |
| | | $-\frac{1}{3}$ | $-\frac{1}{3}$ | $-\frac{1}{3}$ | $\frac{1}{3}$ | $\frac{1}{3}$ | $\frac{1}{3}$ | 0 | |
| | | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | 1 | |
| | | d down | s strange | b bottom | \bar{d} antidown | \bar{s} antistrange | \bar{b} antibottom | γ photon | |
| LEPTONS | mass | $\approx 0.511 \text{ MeV}/c^2$ | $\approx 105.66 \text{ MeV}/c^2$ | $\approx 1.7768 \text{ GeV}/c^2$ | $\approx 0.511 \text{ MeV}/c^2$ | $\approx 105.66 \text{ MeV}/c^2$ | $\approx 1.7768 \text{ GeV}/c^2$ | $\approx 91.19 \text{ GeV}/c^2$ | |
| | charge | -1 | -1 | -1 | 1 | 1 | 1 | 0 | |
| | spin | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | 1 | |
| | | e electron | μ muon | τ tau | e^+ positron | $\bar{\mu}$ antimuon | $\bar{\tau}$ antitau | Z Z ⁰ boson | |
| | | $< 2.2 \text{ eV}/c^2$ | $< 0.17 \text{ MeV}/c^2$ | $< 18.2 \text{ MeV}/c^2$ | $< 2.2 \text{ eV}/c^2$ | $< 0.17 \text{ MeV}/c^2$ | $< 18.2 \text{ MeV}/c^2$ | $\approx 80.39 \text{ GeV}/c^2$ | $\approx 80.39 \text{ GeV}/c^2$ |
| | | 0 | 0 | 0 | 0 | 0 | 0 | 1 | -1 |
| | | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | $\frac{1}{2}$ | 1 | 1 |
| | | ν_e electron neutrino | ν_μ muon neutrino | ν_τ tau neutrino | $\bar{\nu}_e$ electron antineutrino | $\bar{\nu}_\mu$ muon antineutrino | $\bar{\nu}_\tau$ tau antineutrino | W^+ W ⁺ boson | W^- W ⁻ boson |

GAUGE BOSONS
VECTOR BOSONS

SCALAR BOSONS

Current Fundamental Questions in Particle physics

- Why are there three generations of particles?
- Why are the masses of the particles what they are?
- Why is there no antimatter in our universe?
- Why is the charge of the electron exactly opposite to that of the proton?
Or: why is the sum of the charge of leptons + quarks exactly equal to zero?
- Is a neutrino its own anti-particle?
- Can all forces be described in a single theory? Unification
- Are quarks and leptons truly fundamental
- What is the source of dark matter?
- What is the source of dark energy?

- In particle physics we make often use of natural units
 - Very confusing at first but very convenient when you are used to it (“sloppy”)
Set $c = 2.998 \times 10^8 \text{ m/s} \equiv 1$ and $\hbar = 1.055 \times 10^{-34} \text{ Js} \equiv 1$
(Just leave them out and put them back at very end of any calculation)
 - Consequence: there is only one basic unit for length, time, mass and energy: GeV
- Exercise: derive the numbers on the conversion table on the next page

Natural Units: conversion table

| quantity | symbol in natural units | equivalent symbol in ordinary units |
|-----------------|-------------------------|-------------------------------------|
| space | x | $x/\hbar c$ |
| time | t | t/\hbar |
| mass | m | mc^2 |
| momentum | p | pc |
| energy | E | E |
| positron charge | e | $e\sqrt{\hbar c/\epsilon_0}$ |

Conversion of basic quantities between natural and ordinary units.

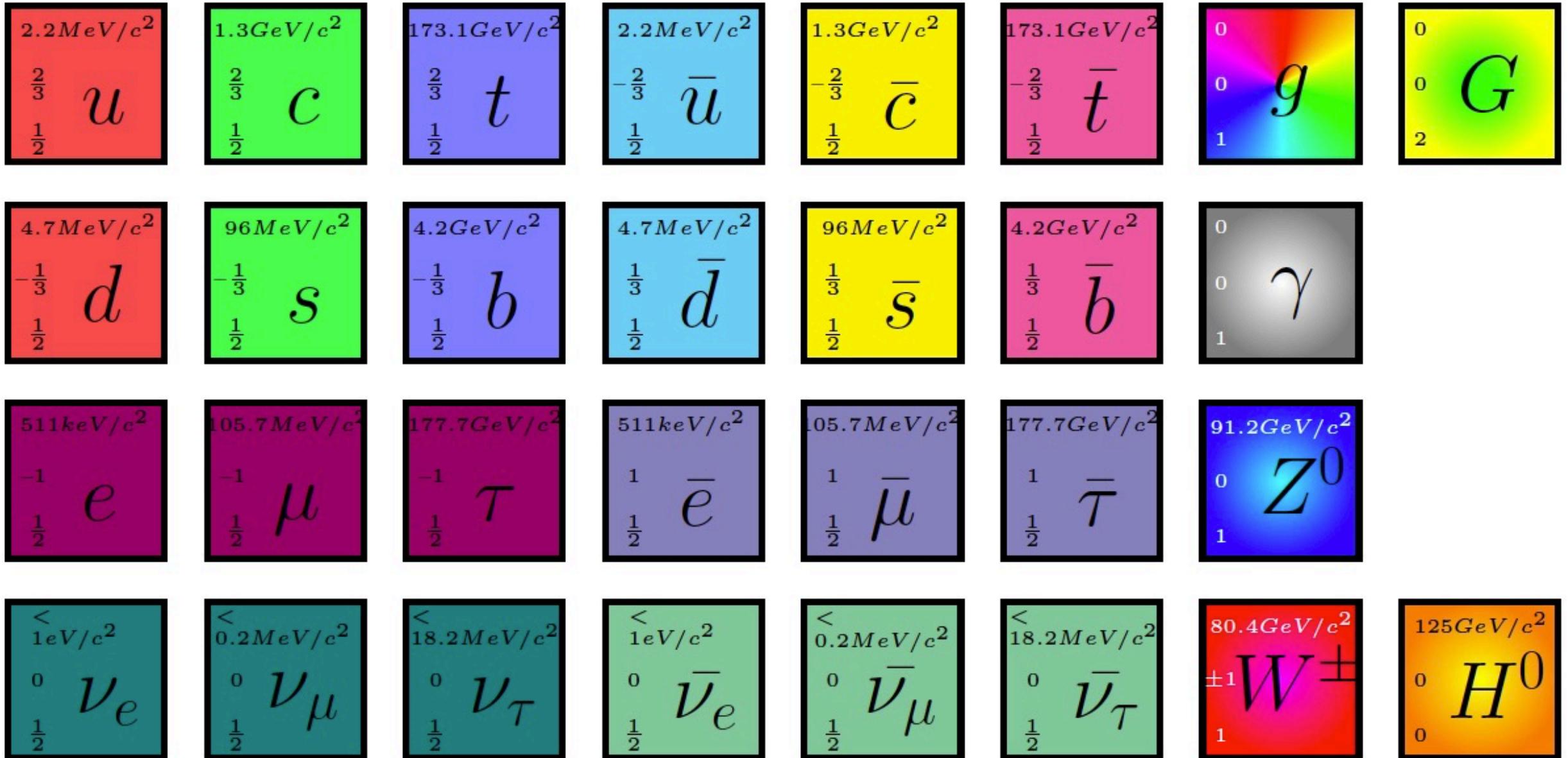
| quantity | conversion factor | natural unit | normal unit |
|----------|--|-------------------|------------------------|
| mass | $1 \text{ kg} = 5.61 \times 10^{26} \text{ GeV}$ | GeV | GeV/c^2 |
| length | $1 \text{ m} = 5.07 \times 10^{15} \text{ GeV}^{-1}$ | GeV^{-1} | $\hbar c / \text{GeV}$ |
| time | $1 \text{ s} = 1.52 \times 10^{24} \text{ GeV}^{-1}$ | GeV^{-1} | \hbar / GeV |

Conversion factors from natural units to ordinary units.

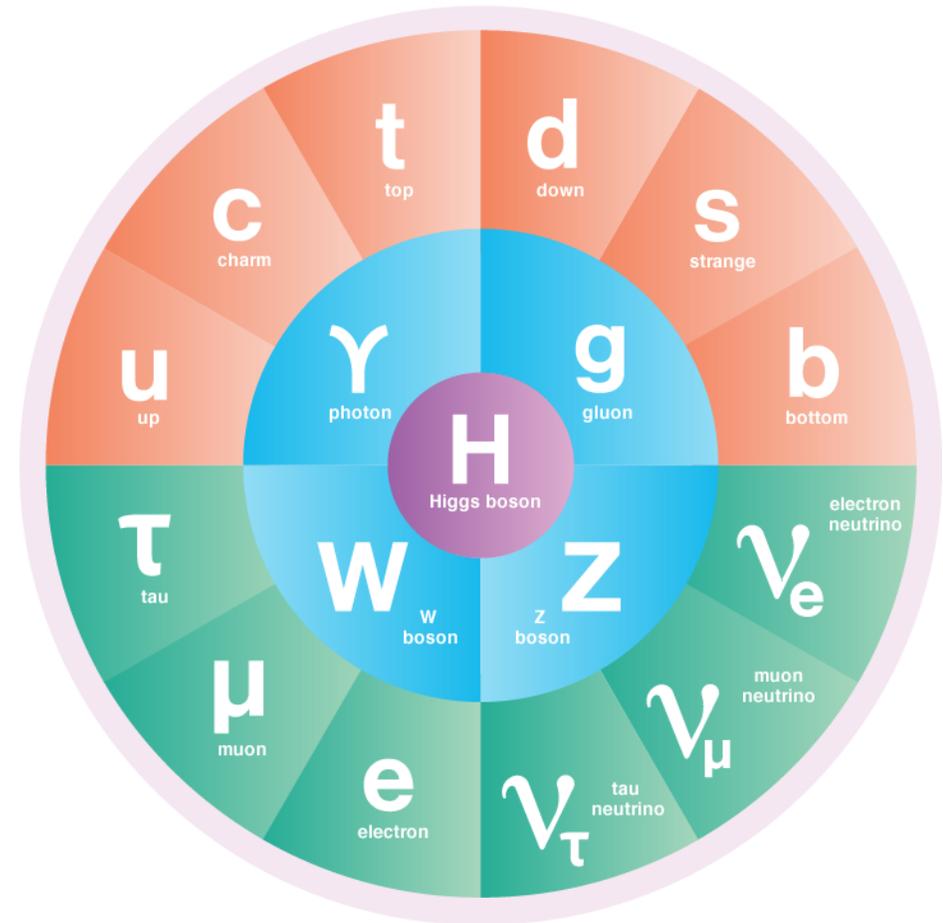
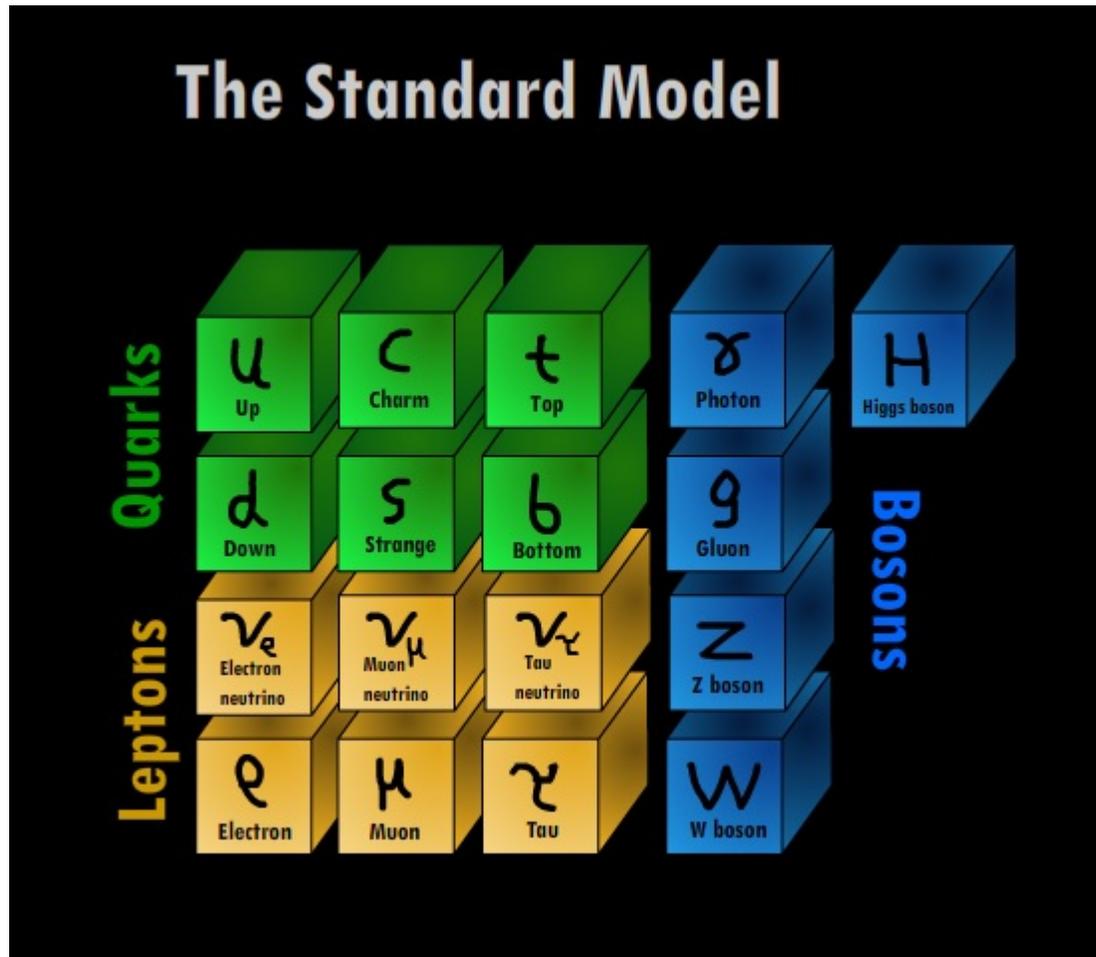
Exercise-6 : the quark model; wave function of hadrons

- a) Quarks are fermions with spin $1/2$. Show that the spin of a meson (2 quarks) can be either a triplet of spin 1 or a singlet of spin 0.
- Hint: use the “Clebsch-Gordon” coefficients in adding quantum numbers. In group theory this is often represented as the product of two doublets leads to the sum of a triplet and a singlet: $2 \otimes 2 = 3 \oplus 1$ or, in terms of quantum numbers: $1/2 \otimes 1/2 = 1 \oplus 0$.
- b) Show that for baryon spin states we can write: $1/2 \otimes 1/2 \otimes 1/2 = 3/2 \oplus 1/2 \oplus 1/2$ or equivalently $2 \otimes 2 \otimes 2 = 4 \oplus 2 \oplus 2$
- c) Let us restrict ourselves to two quark flavours: u and d . We introduce a new quantum number, called *isospin* in complete analogy with spin, and we refer to the u -quark as the isospin $+1/2$ component and the d -quark to the isospin $-1/2$ component (or u =isospin “up” and d =isospin “down”).
- What are the possible isospin values for the resulting baryon?
- d) Optional for die-hards! The Δ^{++} particle is in the lowest angular momentum state ($L = 0$) and has spin $J_3 = 3/2$ and isospin $I_3 = 3/2$. The overall wavefunction ($L \Rightarrow$ space-part, $S \Rightarrow$ spin-part, $I \Rightarrow$ isospin-part) must be anti-symmetric under exchange of any of the quarks. The symmetry of the space, spin and isospin part has a consequence for the required symmetry of the Color part of the wave function.
- Write down the color part of the wave-function taking into account that the particle is color neutral.

Graphical views of the Standard Model of particles



Graphical views of the Standard Model of particles



Graphical views of the SM

STANDARD MODEL OF ELEMENTARY PARTICLES

| QUARKS | UP | | | GLUON | | | HIGGS BOSON | | |
|--------------------------|-----------------------------|--------------------------|---------------------------|----------|----------|-------------------------|-------------|---|---|
| | mass 2,3 MeV/c ² | 1,275 GeV/c ² | 173,07 GeV/c ² | 0 | 0 | 126 GeV/c ² | 0 | 0 | 0 |
| | charge 2/3 | 2/3 | 2/3 | 0 | 0 | 0 | 0 | 0 | 0 |
| spin 1/2 | 1/2 | 1/2 | 1 | 1 | 1 | 0 | 0 | 0 | |
| | u | c | t | g | H | | | | |
| LEPTONS | DOWN | | | PHOTON | | | Z BOSON | | |
| | 4,8 MeV/c ² | 95 MeV/c ² | 4,18 GeV/c ² | 0 | 0 | 91,2 GeV/c ² | 0 | 0 | 1 |
| | -1/3 | -1/3 | -1/3 | 0 | 0 | 0 | 0 | 0 | 1 |
| spin 1/2 | 1/2 | 1/2 | 1 | 1 | 1 | 1 | 1 | 1 | |
| | d | s | b | γ | Z | | | | |
| | ELECTRON | | | W BOSON | | | | | |
| 0,511 MeV/c ² | 105,7 MeV/c ² | 1,777 GeV/c ² | 80,4 GeV/c ² | ±1 | 1 | | | | |
| -1 | -1 | -1 | ±1 | 1 | | | | | |
| spin 1/2 | 1/2 | 1/2 | 1 | 1 | | | | | |
| | e | μ | τ | W | | | | | |
| | ELECTRON NEUTRINO | | | W BOSON | | | | | |
| <2,2 eV/c ² | <0,17 MeV/c ² | <15,5 MeV/c ² | 80,4 GeV/c ² | ±1 | 1 | | | | |
| 0 | 0 | 0 | ±1 | 1 | | | | | |
| spin 1/2 | 1/2 | 1/2 | 1 | 1 | | | | | |
| | ν_e | ν_μ | ν_τ | W | | | | | |

