

# **QCD** corrections to single top quark production in electron photon interactions

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In collaboration with J. H. Kühn, P. Uwer [hep-ph/0303233]

# Motivation

Single top quark production is important:

- Provides a possibility to measure the CKM-matrix element  $|V_{tb}|^2$  directly
- At lepton colliders single top-quark production

$$e^+ \gamma \rightarrow t \bar{b} \bar{\nu}_e$$

- No  $t\bar{t}$ -background  
⇒ Clean environment to study single top quark production
- Process allows the measurement of  $|V_{tb}|^2$  with high accuracy and with an uncertainty of 1% at  $2\sigma$  level (E. Boos et al. '01)  
⇒ Knowledge of the QCD corrections mandatory
- Large  $m_t$  ⇒ high energy scale ⇒ pert. QCD reliable  
⇒ Test of the SM at high energies ⇒ New physics ?

# Preliminaries

- Describe process  $e^+ \gamma \rightarrow t\bar{b}\bar{\nu}_e$  through effective W-approximation  
Kane et al. '84; Dawson '85; Lindfors '85; Kunszt, Soper '88; Kauffman '89
- Consider momentum distribution of the W-bosons through structure function  $f_{e/W}$

Structure function distinguishes between longitudinal and transversal polarized W-bosons

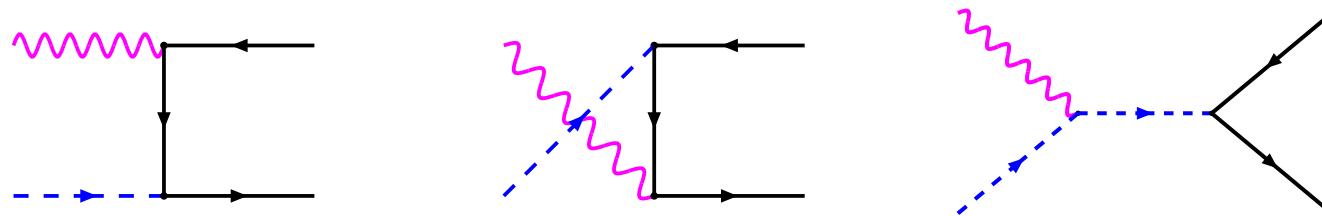
⇒ relevant process:

$$W_{l,t}^+ \gamma \longrightarrow t\bar{b}$$

- Cross section through convolution:

$$\sigma_{e^+ \gamma \rightarrow t\bar{b}\bar{\nu}_e} \sim f_{e/W_i} \otimes \sigma_{W_i \gamma \rightarrow t\bar{b}}$$

# Born process



- ⇒ Trivial calculation!
- ⇒ In principle it is possible to do it automatically

But:

Structure of logarithmic contributions



Analytical calculation important

# Born results

$$\sigma_{\text{tot}}^{T,L} = \frac{1}{9\sqrt{2}} \frac{\alpha G_f |V_{tb}|^2 N}{(1-z_w)^3} \frac{1}{\mathcal{N}_{T,L}} \left( l_1^{T,L} \ln \left( \frac{1+\beta_b}{1-\beta_b} \right) + l_2^{T,L} \ln \left( \frac{1+\beta_t}{1-\beta_t} \right) + K^{T,L} \right)$$

$$\begin{aligned} K^L &= 2 \lambda(1, z_b, z_t) \left( 28 z_b^2 - 9 z_t + 28 z_t^2 - z_b (9 + 56 z_t) + 2 z_w (18 z_b^2 + 41 z_t + 18 z_t^2 \right. \\ &\quad \left. + z_b (5 - 36 z_t)) - z_w^2 (-8 + 12 z_b^2 - 3 z_b (1 + 8 z_t) - 27 z_t + 12 z_t^2) \right) \\ K^T &= 4 z_w \lambda(1, z_b, z_t) \left( -24 z_b^2 + 6 z_b (3 + 8 z_t) - 11 - 12 z_t - 24 z_t^2 - 2 z_w (-9 z_b^2 + 3 z_b (1 + 6 z_t) \right. \\ &\quad \left. + 5 + 15 z_t - 9 z_t^2) - z_w^2 (6 z_b^2 - 12 z_b z_t + 11 - 6 z_t + 6 z_t^2) \right) \\ l_1^L &= 2 (-10 z_b^3 - 2 z_b^2 (1 - 11 z_t) + z_b (1 + 4 z_t - 14 z_t^2) + z_t - 2 z_t^2 + 2 z_t^3 \\ &\quad - 2 z_w (19 z_b^2 + z_t^2 + 4 z_b (1 - 3 z_t)) + z_w^2 (z_t - 7 z_b)) \\ l_2^L &= 8 (z_b - 2 z_b^2 + 2 z_b^3 + (1 + 4 z_b - 8 z_b^2) z_t - 2 (1 - 5 z_b) z_t^2 - 4 z_t^3 \\ &\quad + z_w (-2 z_b^2 - 2 (4 - 9 z_b) z_t - 20 z_t^2) + z_w^2 (z_b - 7 z_t)) \\ l_1^T &= 4 z_w \left( 1 + 14 z_b^2 + 2 z_b (1 - 8 z_t) - 2 z_t + 2 z_t^2 + 2 z_w (7 z_b - z_t) + z_w^2 \right) \\ l_2^T &= 16 z_w \left( 1 + 2 z_b^2 - z_b (2 + 10 z_t) + 2 z_t + 8 z_t^2 - 2 z_w (z_b - 4 z_t) + z_w^2 \right) \\ z_i &= m_i^2/s, \quad \beta_t = \lambda(1, z_b, z_t) / (1 + z_t - z_b), \quad \text{and} \quad , \beta_b = \lambda(1, z_b, z_t) / (1 + z_b - z_t) \end{aligned}$$

Do we need to keep  $m_b$  ?

# Resummation of $\log(m_b^2)$

- Initial state collinear singularity for  $m_b = 0$
- In the case of massless b-quarks the singularity is absorbed in structure functions:

$$\begin{aligned}\sigma &= \int dx \Gamma_{\gamma/\gamma}(\mu_F, x) \times \hat{\sigma}(W^+(p_w)\gamma(xp_\gamma) \rightarrow t(p_t)\bar{b}(p_b)) \\ &+ \int dx \Gamma_{b/\gamma}(\mu_F, x) \times \hat{\sigma}(W^+(p_w)b(xp_\gamma) \rightarrow t(p_t))\end{aligned}$$

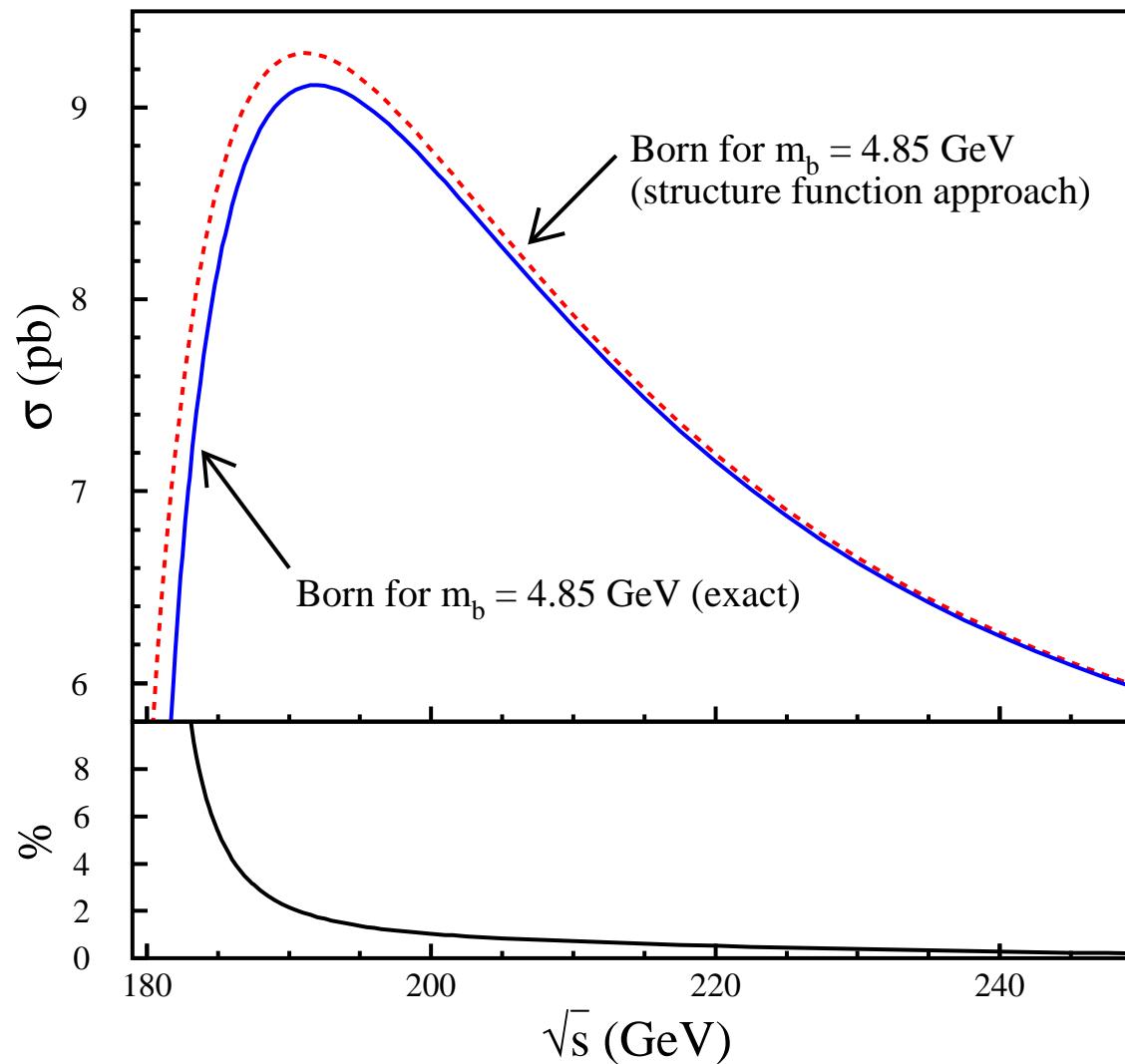
- $\hat{\sigma}$  :  $\mu_F$  dependent,  $\overline{\text{MS}}$  subtracted cross section
- Matching calculation gives:

$$\Gamma_{\gamma/\gamma}(\mu_F, x) = \delta(1-x) + O(\alpha),$$

$$\Gamma_{b/\gamma}(\mu_F, x) = \frac{\alpha}{2\pi} Q_b^2 (x^2 + (1-x)^2) \ln \left( \frac{\mu_F^2}{m_b^2} \right) + O(\alpha^2).$$

- Resummation of the leading logarithms to all orders through evolution equations à la DGLAP

# Fixed order versus structure functions



⇒ Finite b-quark mass is important, affects the location of the threshold

## **QCD corrections**

Calculation of the QCD-corrections consists of 2 parts:

- 1.) Calculation of the virtual corrections to the process:

$$W^+ \gamma \rightarrow t \bar{b}$$

- 2.) Calculation of the real corrections:

$$W^+ \gamma \rightarrow t \bar{b} g$$

Combination of 1.) + 2.) yields finite result

# Virtual corrections

Technicalities:

- Dimensional regularisation of the **UV**-singularities as well as of the **IR**-singularities (t'Hooft, Veltman; Marciano)
- Passarino-Veltman reduction of the tensor integrals to scalar one loop integrals
- Solution of the scalar integrals through Feynman-parametrisation
- Replacement of the scalar box integrals in  $d = 4 - 2\varepsilon$  dimensions through:

$$D_0^{d=4-2\varepsilon} = \underbrace{a D_0^{d+2}}_{\text{IR finite}} + \underbrace{\sum_{i=1}^4 b_i C_0^{i,d}}_{\text{IR divergent}}$$

$\Rightarrow$  algebraic complexity is reduced.

- **IR**- singularities in three-point integrals ( $C_0$ )
- **UV**- singularities in one-,two-point integrals ( $A_0, B_0$ )

# Analytic result

As usual:

$$\text{Result} = \sum_i \text{Coefficient}_i \times \text{Scalar-integral}_i$$

Divergent parts:

$$\begin{aligned} \delta |\mathcal{M}_{1,d}|^2|_{\text{UV-div.}} &= \frac{\alpha_s}{2\pi} \Gamma(1+\epsilon) C_F \left( \frac{4\pi\mu^2}{m_t m_b} \right)^\epsilon \frac{1}{\epsilon} |\mathcal{M}_0|^2 \\ &\quad - 3 \frac{\alpha_s}{\pi} \Gamma(1+\epsilon) C_F \left( \frac{4\pi\mu^2}{m_t m_b} \right)^\epsilon \frac{1}{\epsilon} F(z_w, z_b, z_t) \\ \delta |\mathcal{M}_{1,d}|^2|_{\text{IR-div.}} &= \frac{\alpha_s}{\pi} C_F (z_b + z_t - 1) (2\pi\mu)^{2\epsilon} \text{Re} C_0(1, 2, 3) s \sum_{\text{Pol.}} |\mathcal{M}_{0,\text{d}}|^2 \end{aligned}$$

the finite parts are a little bit lengthier. . .

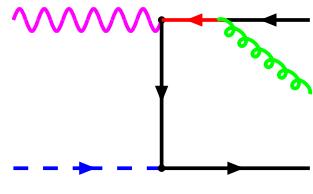
## Finite part:

$$\begin{aligned}
& \sum_{\text{Spins}} M_{fi}^{1-\text{loop}} M_{fi}^{\text{*Born,d}} \Big|_{\text{finite}} = \frac{e^4 g_s^2}{2 \sin^2 \theta_w} |V_{tb}|^2 \left[ -8/9 D_0^6 (2 t_{bg} - t_{tg}) (-3 m_b^4 m_t^2 t_{bg}^2 + 3 t_{bg}^2 m_b^6 - 2 m_b^4 t_{bg}^3 + 12 t_{bg}^3 m_w^4 + 3 m_t^6 t_{bg}^2 - 4 t_l m_b^6 t_{tg}^2 - 2 m_t^4 t_{bg}^3 + m_b^2 t_{tg}^3 t_{bg} + m_t^2 t_{tg}^3 t_{bg} - 2 m_b^8 t_{bg} + 4 m_w^8 t_{bg} + 12 m_w^6 t_{bg}^2 + 4 t_{bg}^4 m_w^2 + m_t^2 t_{bg}^4 + m_b^2 t_{bg}^4 - 7 m_t^2 t_{bg}^3 m_w^2 + 4 m_b^4 m_t^4 t_{tg} + 3 m_w^2 - 5 m_t^4 t_{tg} t_{bg}^2 + 2 m_b^6 t_{bg} m_w^2 + 12 m_b^4 t_{tg} m_w^4 - 10 m_b^2 m_w^6 t_{bg} + 4 m_b^4 t_{tg}^2 m_w^2 + 16 t_{tg} t_{bg}^2 m_w^4 - 10 m_t^2 t_{bg} m_w^6 - 4 m_b^2 m_t^6 t_{tg} + 2 m_t^6 t_{bg} m_w^2 + m_t^4 t_{bg} + 4 m_b^2 t_{tg}^2 m_t^4 - 3 m_t^4 t_{tg}^2 t_{bg} + 6 t_{tg}^2 t_{bg} m_w^4 + 4 m_b^6 t_{tg} m_t^2 - 18 m_t^2 t_{bg}^2 m_w^4 + 8 t_{tg} t_{bg} m_b^6 + 6 m_t^4 t_{bg} m_w^4 - 8 m_b^2 t_{tg}^2 m_w^4 + 3 m_t^4 t_{bg}^2 m_w^2 - t_{tg}^2 t_{bg} + 8 t_{tg} t_{bg} m_w^6 - 7 m_b^2 t_{bg}^3 m_w^2 + 3 m_b^2 t_{tg}^2 t_{bg}^2 + 4 t_{tg} t_{bg} m_t^6 - 5 m_b^4 t_{bg}^2 t_{tg} + 6 m_b^4 t_{bg} m_w^4 + 3 m_b^4 t_{bg}^2 m_w^2 - 8 m_b^2 t_{tg} m_w^6 + 6 t_{tg} t_{bg} m_w^2 - 1 m_b^2 t_{tg} + 3 m_t^2 t_{bg}^3 t_{tg} - 3 m_t^4 t_{bg}^2 m_b^2 - 10 m_b^2 t_{bg} m_w^2 m_t^4 - 16 m_b^4 t_{tg} m_w^2 m_t^2 + 10 m_t^2 t_{bg}^2 m_w^2 m_b^2 - 8 m_b^2 t_{bg}^2 m_w^2 t_{tg} - 3 m_b^2 t_{tg}^2 m_w^2 t_{bg} + 12 m_t^2 t_{tg} m_w^4 + 4 m_b^2 t_{tg}^2 m_w^2 m_t^2 - 12 t_{tg} t_{bg} m_w^4 m_t^2 + 20 t_{bg} m_b^2 m_t^2 t_{tg} m_w^2 - 20 t_{tg} t_{bg} m_w^4 m_b^2 - 8 m_t^2 t_{bg}^2 t_{tg} m_w^2 - 3 m_t^2 t_{tg}^2 t_{bg} m_w^2 + 2 m_b^2 m_t^2 t_{tg} t_{bg}^2 + m_b^4 t_{tg} t_{bg} m_t^2 + 4 m_b^4 t_{tg} t_{bg} m_w^2 - 10 m_b^4 m_t^2 t_{bg} m_w^2) (-m_b^2 t_{tg}^2 - m_t^2 t_{bg}^2 + t_{bg} m_w^2 t_{tg} - m_b^2 t_{tg} t_{bg} - m_t^2 t_{bg} t_{tg} + t_{tg}^2 t_{bg} + t_{bg}^2 t_{tg}) / (2 m_m^2 + t_{tg} + t_{bg}) / (-2 m_b m_t + m_w^2 - m_b^2 - m_t^2 + t_{tg} + t_{bg}) / (t_{tg} + t_{bg}) - 2/9 B_0(1,2) (16 t_{tg}^6 m_w^{16} m_b^2 - 56 t_{bg}^2 t_{tg}^7 m_w^{12} + 135 t_{tg}^5 t_{bg}^7 m_t^6 - m_t^{12} m_w^2 - 152 t_{tg}^6 m_b^6 m_w^{10} m_t^2 + m_t^4 t_{tg}^7 m_w^8 t_{bg}^2 - 3 m_t^{10} t_{bg}^2 t_{tg}^8 - 129 t_{bg}^9 m_t^2 t_{tg}^3 m_w^4 + 12 m_t^8 t_{tg}^7 m_b^4 m_w^4 - 84 m_b^{16} t_{tg}^4 m_w^2 t_{bg}^2 + 15 m_t^{12} t_{bg}^2 t_{tg}^7 - 24 t_{bg}^9 t_{tg}^2 m_w^8 + 32 m_w^{20} t_{tg}^3 t_{bg}^2 - 1360 t_{tg}^2 t_{bg}^7 m_w^{12} - 136 m_t^{14} t_{bg}^7 m_w^2 + 80 t_{tg}^6 m_b^{10} m_w^8 - 16 m_t^{10} t_{tg}^7 m_b^2 m_w^4 + 453 t_{bg}^7 m_b^6 m_t^2 t_{tg}^4 - 496 m_b^6 t_{bg}^8 t_{tg}^2 m_w^4 m_b^2 + 2652 t_{bg}^7 m_t^4 t_{tg}^2 m_w^6 m_b^2 - 846 t_{bg}^7 m_t^2 m_b^4 t_{tg}^4 m_w^2 + 652 t_{tg}^5 t_{bg}^5 m_t^2 m_w^6 m_b^2 - 532 t_{tg} t_{bg}^4 m_t^{12} m_w^2 m_b^6 + 32 t_{tg}^2 t_{bg}^5 m_t^8 m_w^6 m_b^2 + 978 t_{tg}^5 t_{bg}^4 m_t^4 m_b^8 t_{bg}^4 m_w^4 - 349 t_{bg}^3 t_{tg}^5 m_t^6 m_w^8 - 552 m_t^{12} t_{bg}^6 m_w^4 t_{tg} - 16 m_b^{16} t_{tg}^3 m_w^4 t_{bg}^2 - 578 m_t^6 t_{bg}^3 t_{tg}^4 m_w^10 + 202 m_t^4 t_{bg}^3 t_{tg}^5 m_w^{10} - 111 m_t^{12} t_{tg}^2 t_{bg}^5 m_w^4 m_b^2 + 440 t_{tg}^4 t_{bg}^4 m_t^8 m_w^4 m_b^2 + 2236 t_{tg}^4 t_{bg}^4 m_t^6 m_w^6 m_b^2 + 9640 m_t^4 t_{bg}^6 m_w^6 m_b^6 t_{tg} - 1488 m_t^8 t_{bg}^5 m_w^6 m_b^6 - 1440 m_t^8 t_{bg}^4 m_w^4 m_b^{10} + 224 m_t^4 t_{bg}^4 m_w^6 m_b^{10} + 288 m_t^8 t_{bg}^4 m_w^6 m_8 + 4359 t_{tg}^4 t_{bg}^3 m_b^8 t_{bg}^3 m_t^4 m_w^4 + 560 m_t^{10} t_{bg}^7 m_w^4 t_{tg} - 3808 m_t^{10} t_{bg}^4 m_w^8 t_{tg} m_b^2 - 2688 m_t^{10} t_{bg}^5 m_w^8 t_{tg} - 142 t_{tg}^6 m_b^8 t_{bg}^3 t_{bg}^3 m_t^4 m_w^2 - 4344 m_t^4 t_{bg}^5 m_w^{14} t_{tg} + 200 m_t^{14} t_{bg}^5 m_w^4 t_{tg} + 36 t_{tg}^8 m_b^2 t_{bg}^3 m_w^6 + 7508 m_t^4 t_{bg}^4 m_w^{14} t_{tg} m_b^2 + 8 t_{tg}^6 t_{bg}^4 m_w^4 m_b^6 - 880 t_{tg}^6 t_{bg}^5 m_w^2 m_b^4 m_t^2 t_{bg} - 5560 m_t^4 t_{bg}^6 m_w^{12} t_{tg} + 846 t_{bg}^3 t_{tg}^3 m_t^6 m_w^{12} + 40 t_{tg}^4 m_w^{18} t_{bg}^2 + 8 t_{tg}^7 t_{bg}^6 m_w^4 - 9 m_t^{16} t_{tg}^2 t_{bg}^5 + 1080 t_{bg}^7 m_t^6 m_w^{10} + 144 t_{tg}^5 t_{bg}^6 m_w^8 + 16 t_{bg}^{11} n t_{bg}^8 - 800 m_t^{10} t_{bg}^6 m_w^8 + 9500 m_t^4 t_{bg}^4 m_w^{10} m_b^6 t_{tg} + 602 t_{tg}^6 t_{bg}^4 m_w^2 m_b^6 m_t^2 - 3307 t_{tg}^3 t_{bg}^4 m_t^{10} m_w^6 - 1888 m_t^6 t_{bg}^4 m_w^8 m_b^6 t_{tg} - 936 t_{bg}^3 t_{tg}^3 m_t^8 m_w^{10} + t_{tg} + 1984 m_t^8 t_{bg}^6 m_w^8 t_{tg} - 90 t_{tg}^6 m_b^4 m_t^8 t_{bg}^3 - 12888 m_t^6 t_{bg}^5 m_w^{10} t_{tg} m_b^2 + 3420 m_t^6 t_{bg}^6 m_w^{10} t_{tg} + 3440 m_t^8 t_{bg}^5 m_w^8 t_{tg} m_b^2 - 7528 m_t^6 t_{bg}^4 m_w^4 m_b^8 m_w^4 - 728 m_t^{10} t_{bg}^6 m_w^6 t_{tg} + 64 t_{tg}^5 m_b^{14} m_w^2 t_{bg}^2 + 573 t_{tg}^2 t_{bg}^5 m_t^{10} m_w^4 m_b^2 - 112 m_t^6 t_{tg}^7 m_w^6 t_{bg}^2 - 8 t_{tg}^8 m_b^6 m_w^4 t_{bg}^2 - 36 t_{tg}^8 t_{bg}^3 m_t^4 m_b^4 + 719 m_t^{12} t_{tg}^5 m_t^3 t_{bg}^2 + 35 m_t^8 t_{tg}^5 m_w^8 t_{bg}^2 - 103 m_t^6 t_{tg}^6 m_w^8 t_{bg}^2 - 176 m_t^{14} t_{tg}^3 m_w^6 t_{bg}^2 + 156 m_t^{16} t_{tg}^4 m_w^2 t_{bg}^2 + 4760 m_t^{10} t_{bg}^5 m_w^2 m_b^8 - 252 m_t^{14} t_{tg}^3 m_b^4 t_{bg}^2 m_w^2 - 800 m_t^6 t_{bg}^4 m_w^4 m_b^{12} + 1184 t_{tg}^3 m_b^4 t_{bg}^3 m_w^{14} - 72 m_t^6 t_{bg}^5 t_{tg}^5 m_b^4 + 98 m_t^6 t_{tg}^2 m_b^2 t_{bg}^3 m_w^4 - 2 m_t^6 t_{tg}^7 m_b^2 t_{bg}^3 m_w^2 + 188 t_{tg}^3 t_{bg}^5 m_t^{12} m_w^2 + 1580 m_t^4 t_{tg}^3 t_{tg}^4 m_b^6 t_{bg}^2 + 168 m_t^{12} t_{bg}^7 m_w^2 t_{tg} - 448 m_t^6 t_{bg}^7 m_w^8 t_{tg} + 2564 m_t^8 t_{tg}^3 t_{bg}^4 m_w^2 m_b^6 - 3880 m_t^8 t_{tg}^3 t_{bg}^5 m_w^2 m_b^4 + 3156 m_t^8 t_{tg}^3 t_{bg}^5 m_w^6 - 213 t_{tg}^4 t_{tg}^4 m_b^8 t_{bg}^2 + 432 m_t^6 t_{bg}^4 t_{tg}^5 m_b^6 - 308 m_t^8 t_{tg}^6 m_b^2 t_{bg}^3 m_w^2 - 42 m_t^6 t_{tg}^7 m_b^6 t_{bg}^2 - 1017 t_{tg}^5 m_b^2 m_t^{10} m_w^4 t_{bg}^2 + 119 t_{tg}^7 m_b^8 m_w^2 m_t^2 t_{bg}^2 + 560 m_w^{16} t_{tg}^3 m_b^4 t_{tg}^4 m_w^2 m_b^2 + 888 m_t^4 t_{tg}^4 t_{bg}^5 m_w^2 m_b^2 + 3856 m_t^4 t_{tg}^4 m_b^4 t_{bg}^2 m_w^{10} - 2394 m_t^4 t_{tg}^4 m_b^2 t_{bg}^3 m_w^{10} - 980 m_t^{14} t_{tg}^4 t_{bg}^4 m_w^6 - 346 m_t^6 t_{tg}^5 t_{bg}^5 m_w^4 + 3296 m_t^8 t_{tg}^4 t_{tg}^3 m_b^2 m_w^2 + 224 m_t^6 t_{tg}^6 t_{bg}^5 m_w^2 + 261 m_t^{10} t_{tg}^4 t_{bg}^4 m_b^4 - 34 m_t^8 t_{tg} + \dots
\end{aligned}$$

$$t_{ij} = 2(p_i \cdot p_j)$$

# Real corrections

- IR-singularities from phase space integration through soft gluon



Denominator of the propagator:  
 $-2E_g E_b(1 - \beta \cos \theta_{bg})$   
 $\Rightarrow$  Vanishes for  $E_g = 0$

- Factorisation in the limit  $p_g \rightarrow 0$ :

$$\mathcal{M}_0(p_\gamma, p_w, p_t, p_b, p_g) \xrightarrow{p_g \text{soft}} \mathcal{S}(p_t, p_g, p_b) \times \mathcal{M}_0(p_\gamma, p_w, p_t, p_b)$$

with the eikonal factor

$$\mathcal{S}(p_i, p_s, p_j) = \frac{2(p_i \cdot p_j)}{(p_i \cdot p_s)(p_j \cdot p_s)} - \frac{(p_i \cdot p_i)}{(p_i \cdot p_s)^2} - \frac{(p_j \cdot p_j)}{(p_j \cdot p_s)^2}.$$

$\Rightarrow$  Consistency check of the amplitudes

- Extraction of the singularities:
  - 1.) Decomposition of the phase space
  - 2.) Dipol subtraction method for massive quarks

Phaf, Weinzierl '01,  
 Catani et al. '02

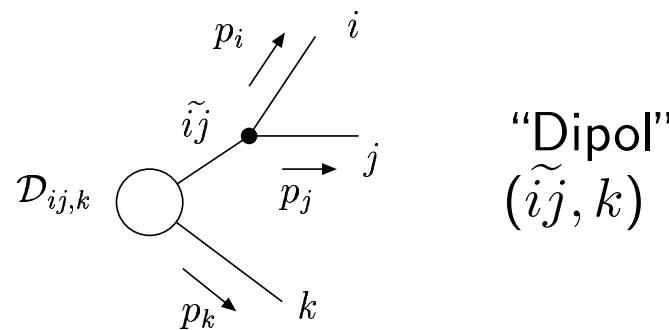
# Dipol subtraction method

Basic idea:

$$\sigma^{\text{NLO}} = \int_{m+1} \left[ (\text{d}\sigma^{\text{R}})_{\epsilon=0} - (\text{d}\bar{\sigma}^{\text{sub}})_{\epsilon=0} \right] + \int_m \left[ \text{d}\sigma^{\text{V}} + \int_1 \text{d}\bar{\sigma}^{\text{sub}} \right]_{\epsilon=0}$$

- Construction of  $\text{d}\sigma^{\text{sub}}$

Catani et al. '02



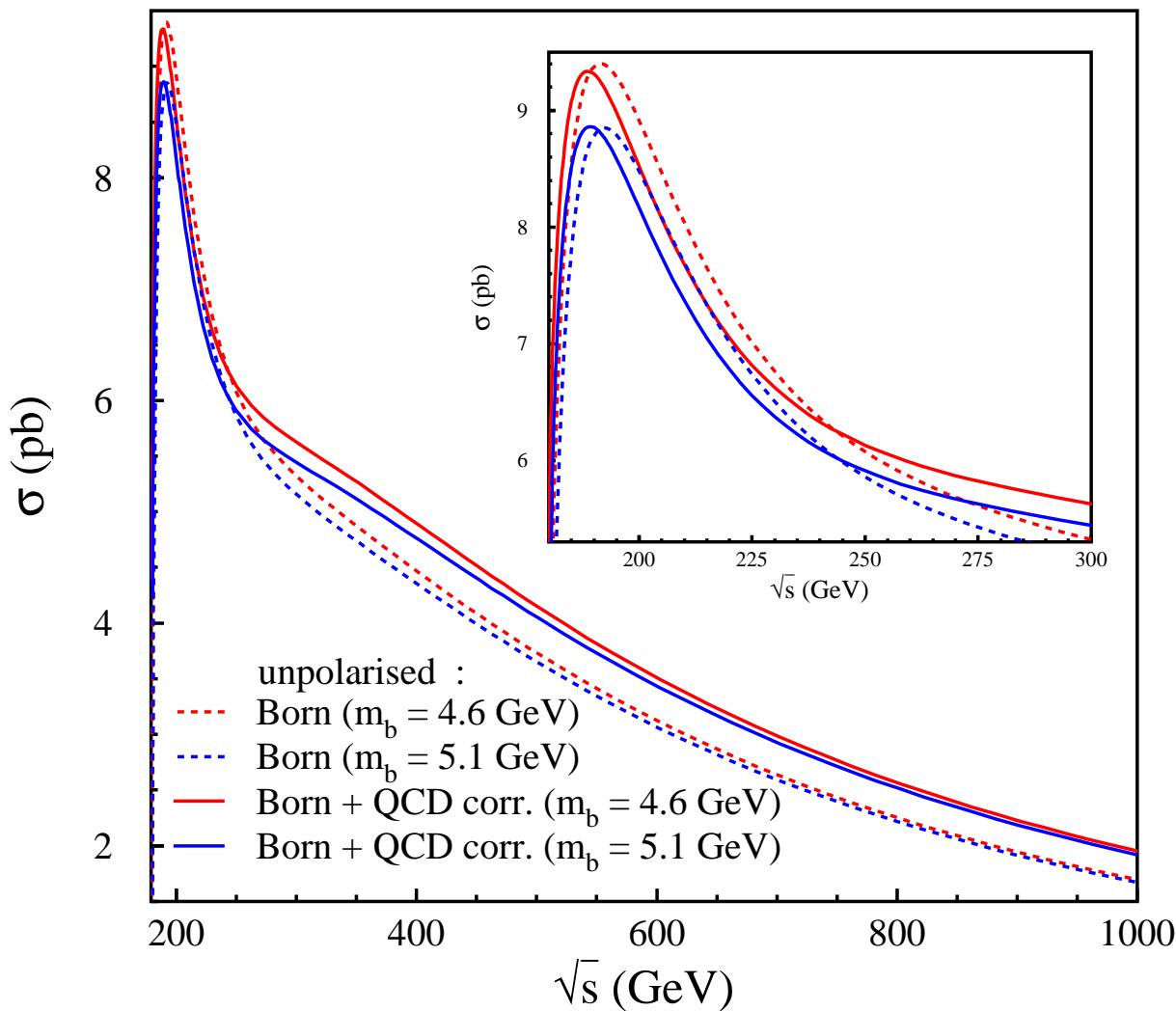
$$\int_{m+1} \text{d}\sigma^{\text{sub}} = \sum_{\text{dipoles}} \int_{m+1} \text{d}\sigma^{\text{LO}} \otimes \mathcal{D}_{ij,k}$$

- Construction of  $\text{d}\bar{\sigma}^{\text{sub}}$ :  $\int_1 \text{d}\bar{\sigma}^{\text{sub}} = \sigma^B \otimes I$

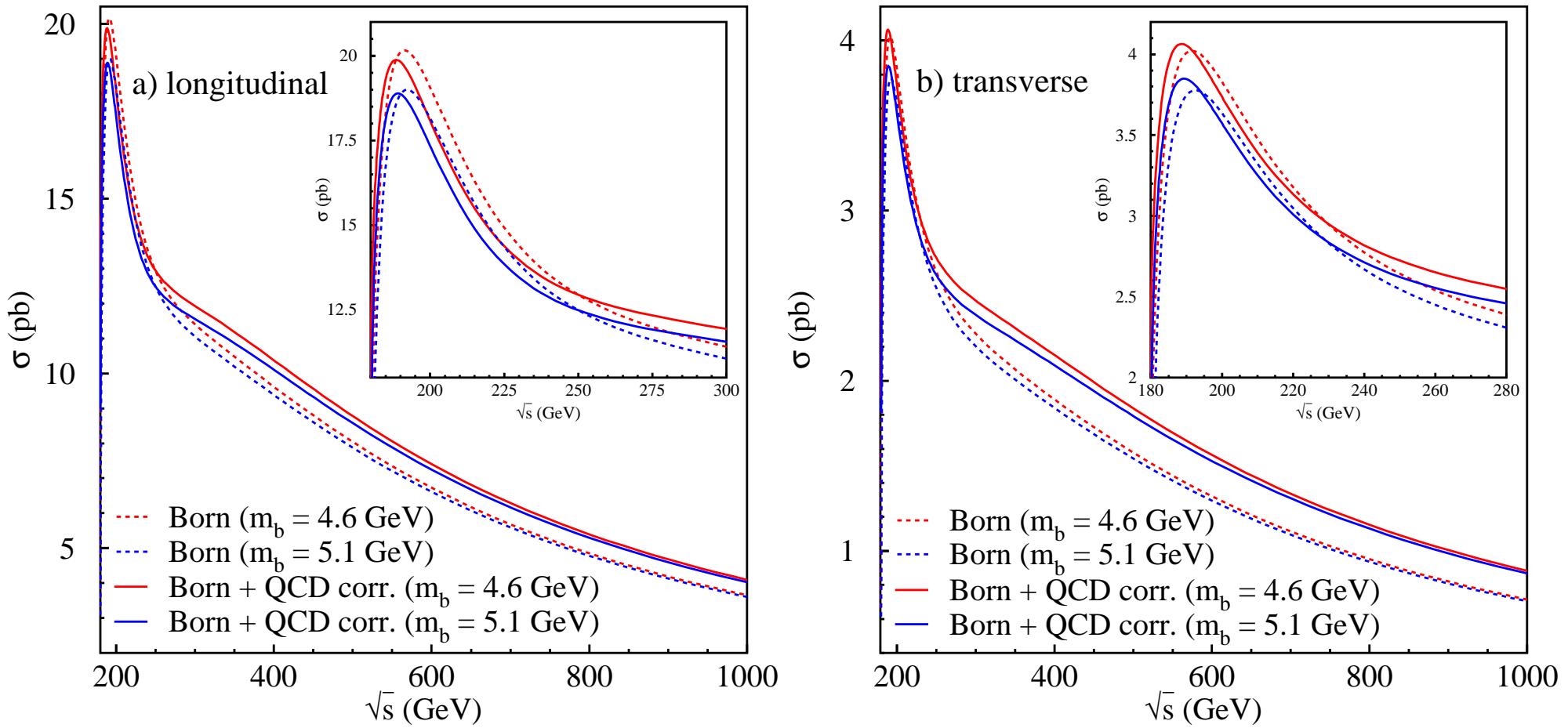
# Checks

- Check of the analytical results of the infrared finite scalar integrals with FF Oldenborgh
- $D_0$ -Box checked with the analytic result of Beenakker, Denner
- Coefficients of the scalar one- and two-point integrals checked by UV renormalisation
- Check of the IR divergent integrals and their coefficients through the cancellation with those from Catani et al.
- Factorisation in  $d$  dimensions checks the treatment of the  $\gamma$ -matrices in  $d$  dimensions
- High degree of automatisation

# Results: Total cross section

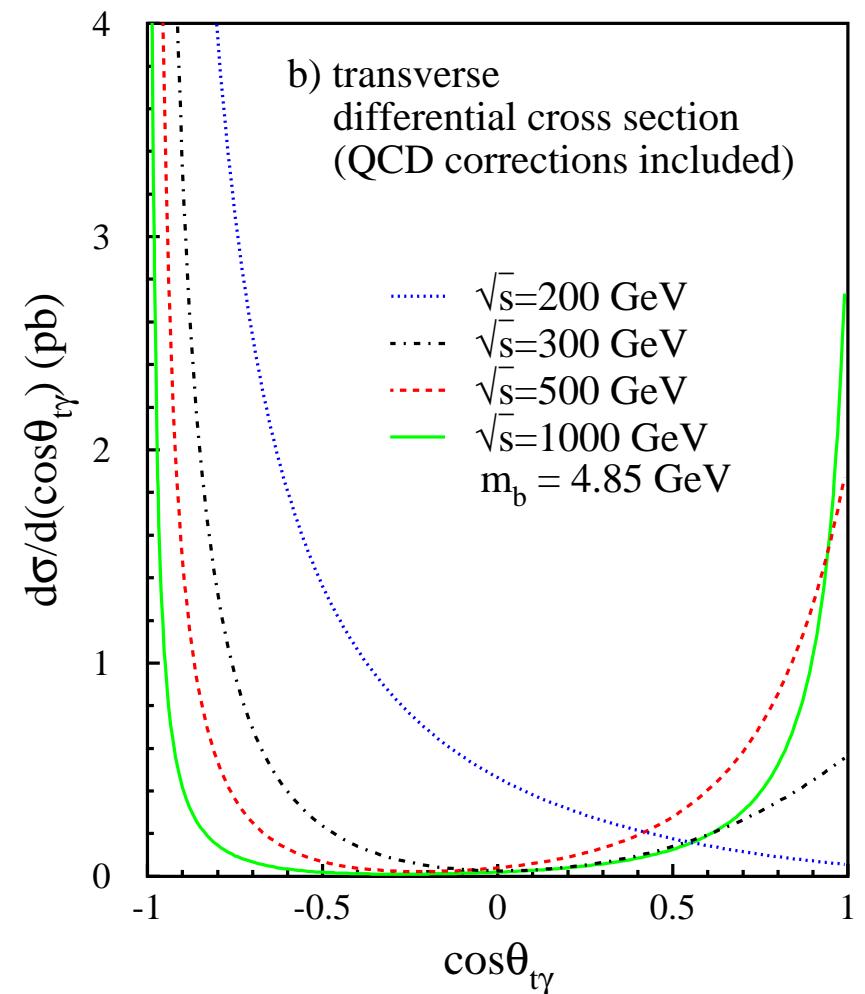
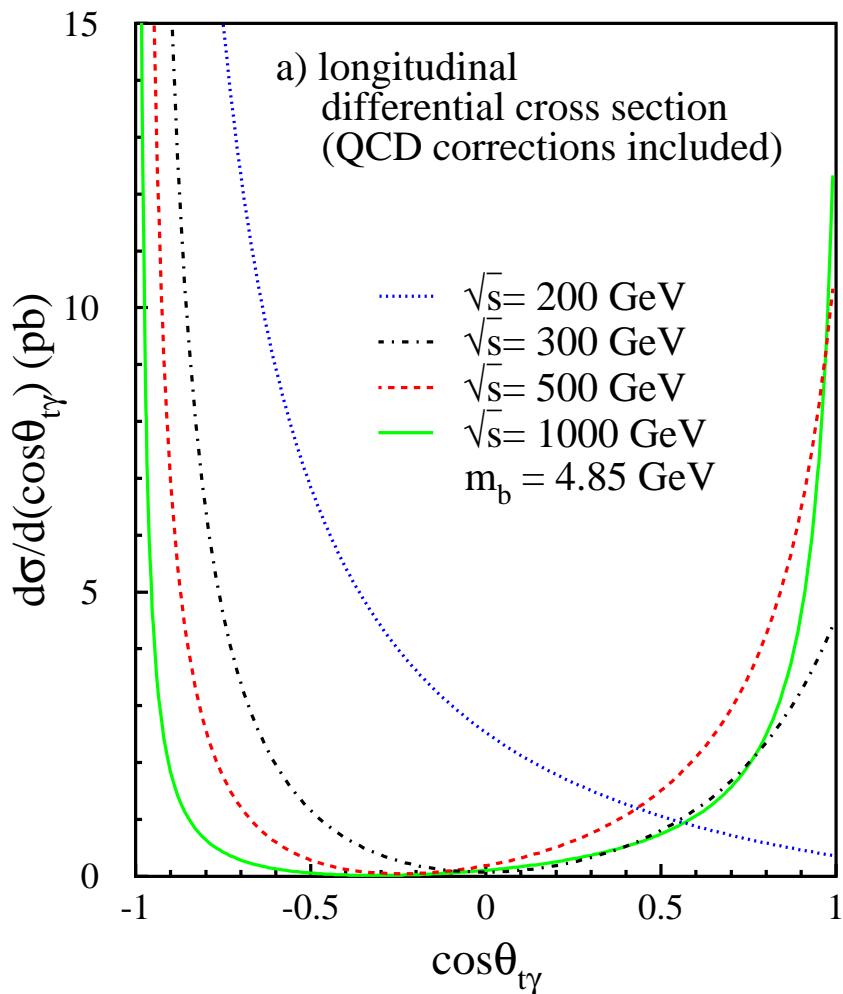


# Results



Cross section for longitudinally and transversely polarized  $W$ -bosons

# Differential cross section



⇒ initial state singularity

Dipole subtraction method allows the calculation of the QCD corrections for arbitrary observables!

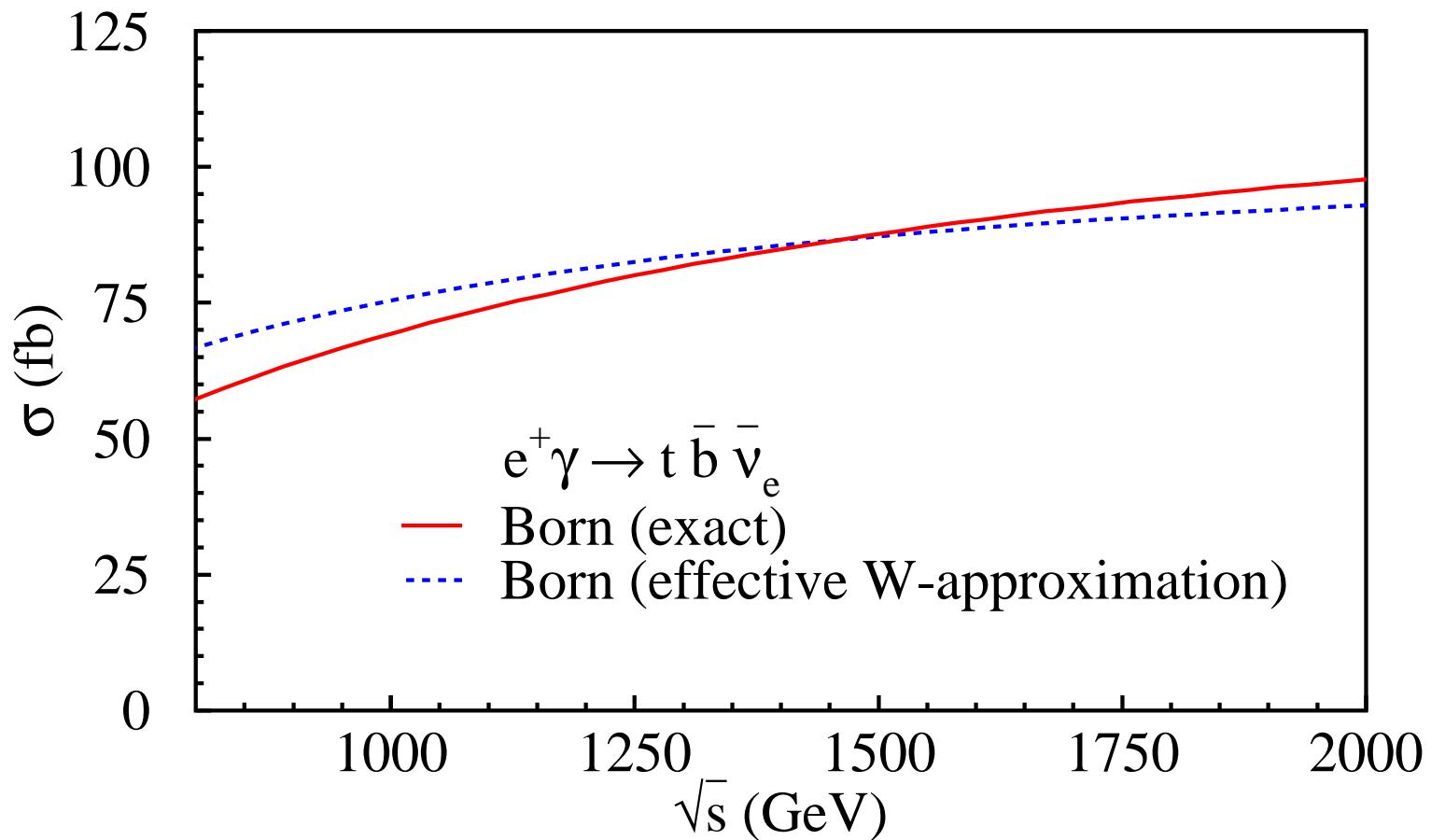
# QCD Logarithms

- QCD corrections generate  $\alpha_s \times \log(m_b)$  term
- In principle they need to be resummed  
⇒ Same framework like the LO-Resummation

Ingredients:

- Mixed evolution
  - QCD corrections to structure functions
- 
- These Logarithms are not expected to be large!

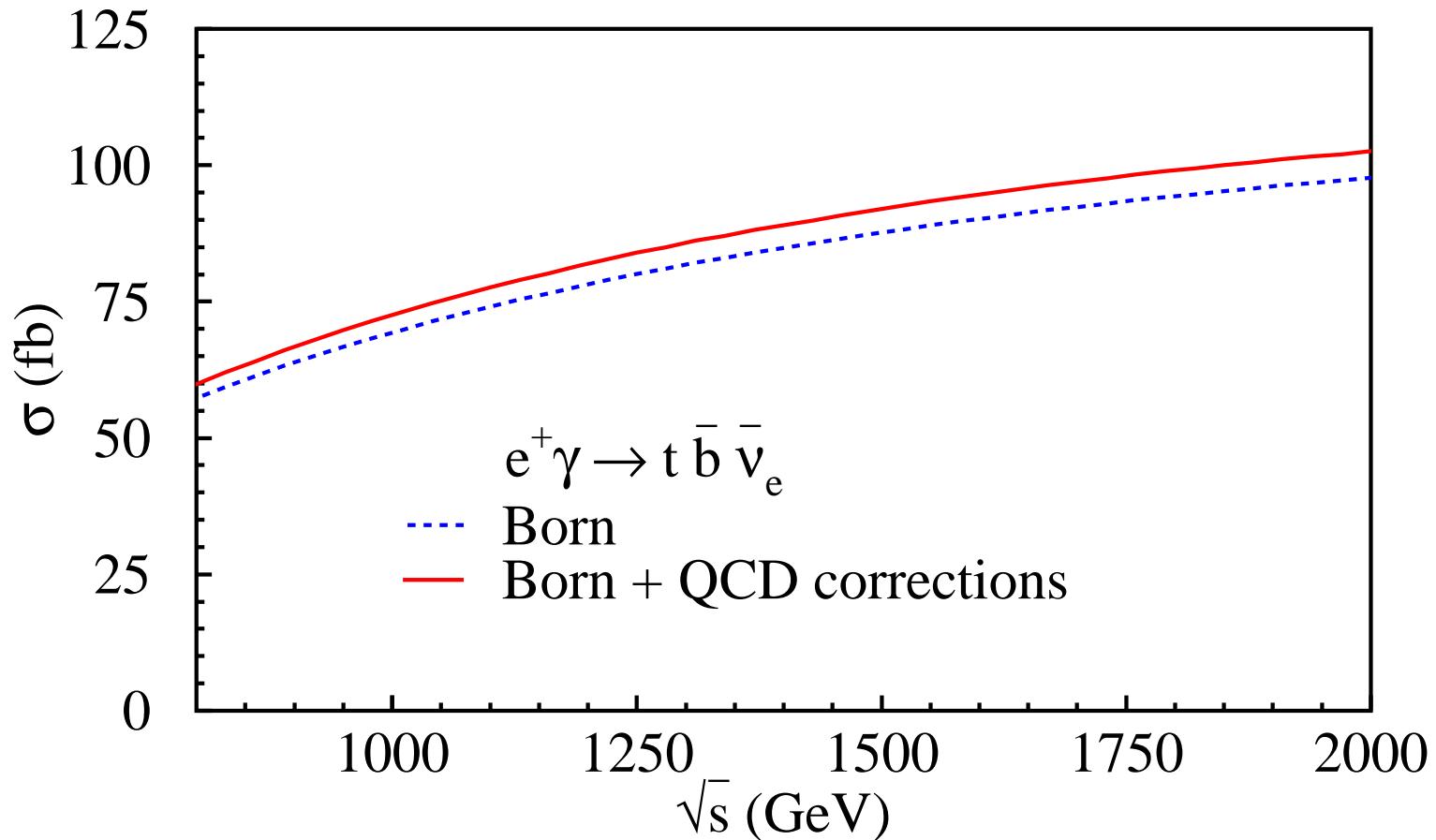
## Implementation of the distribution functions



$\Rightarrow$  Quality 10% for  $\sqrt{s} = 900$  GeV

- use exact result in LO!
- use  $W$ -approximation **only** for the **QCD** corrections!

## **QCD corrections for $e^+\gamma \rightarrow t\bar{b}\bar{\nu}$**



# Conclusions

- Dependence of the b-quark mass of the process  $W^+\gamma \rightarrow t\bar{b}$  has been studied  
→ b-quark mass effects important in threshold region
- QCD corrections of the process  $W^+\gamma \rightarrow t\bar{b}$  have been calculated  
→ corrections of the order of 10-20%
- QCD-NLO prediction for  $e^+\gamma \rightarrow t\bar{b}\bar{\nu}_e$  in the effective W-approximation has been made  
→ QCD corrections are of the order 5%  
→ important for precise measurements of  $|V_{tb}|$