

The investigation of spin effects in photon production with fermion pair in $\gamma\gamma$ -collisions

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The physics in $\gamma\gamma$ collisions strongly depends on the polarization of interacting photons.

J is the total helicity of $\gamma\gamma$ -system.

The luminosity of $J=2$ -beams can be measured using the classical QED process $\gamma\gamma \rightarrow f\bar{f}$.

On $J=0$ -beams the leading term of $\gamma\gamma \rightarrow f\bar{f}$ scattering is of order $\alpha/\pi \approx 0.002$.

The opportunity to use exclusive reaction $\gamma\gamma \rightarrow f\bar{f}\gamma$ for luminosity measurement on $J=0$ -beams.

We analyse the ratio of cross sections of $\gamma\gamma \rightarrow f\bar{f}\gamma$ scattering on $J=0$ to $J=2$ -beams depending on detector cuts.

$$\sqrt{s} = 120\text{GeV}$$

Notations:

Minimum final-state photon energy: ω_{cut} ,

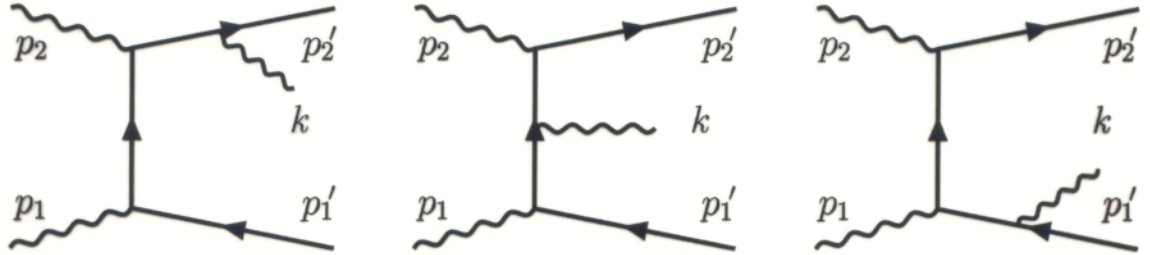
Minimum fermion energy: $E_{f,cut}$,

Minimum angle between any final and any initial particles: Θ_{cut} ,

Minimum angle between any pair of final particles: φ_{cut} .

$$\gamma(p_1, \lambda_1) + \gamma(p_2, \lambda_2) \rightarrow f(p_1', e_1') + \bar{f}(p_2', e_2') + \gamma(k, \lambda_3),$$

where λ_i and e_i' are photon and fermion helicities.



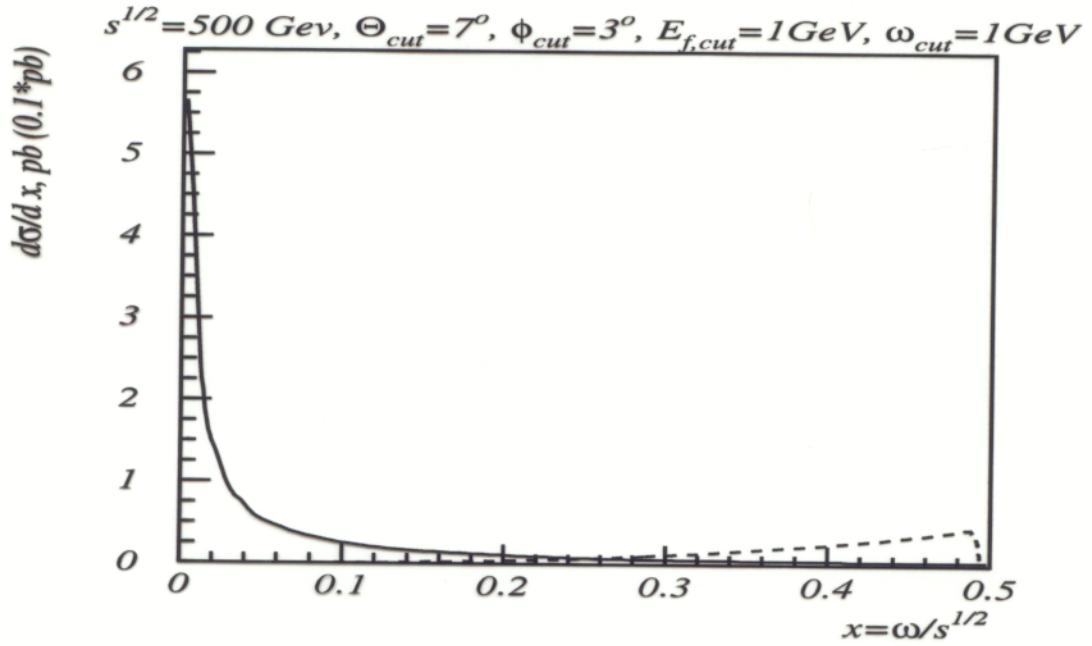
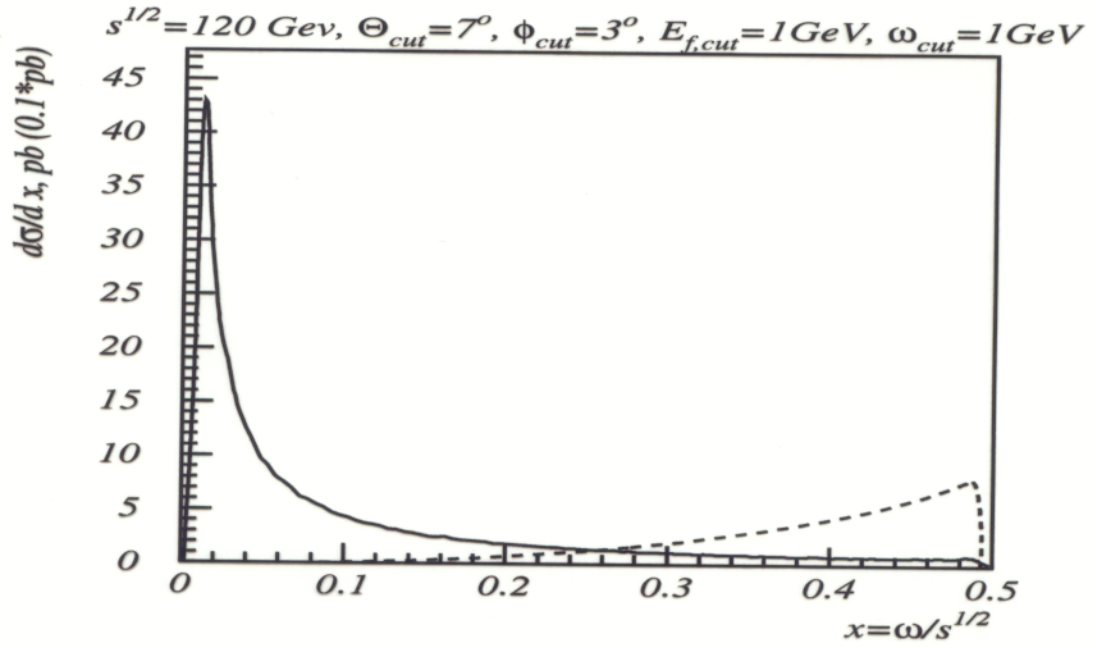
+ crossed graphs ($p_1 \leftrightarrow p_2$)

$$|M^{+-++}|^2 = 4e^6 \frac{p_1' \cdot p_2' p_2' \cdot p_2^2}{p_1' \cdot k p_2' \cdot k p_1' \cdot p_1 p_2' \cdot p_1}$$

C + P + Bose + crossing symmetries $\Rightarrow$

$$\begin{aligned} d\sigma^{+-+-} &= d\sigma^{+-++}|_{1 \leftrightarrow 2}, \quad (P + \text{Bose}) \\ d\sigma^{+-++} &= d\sigma^{+-++}|_{1' \leftrightarrow 2'}, \quad (C) \\ d\sigma^{+-+-} &= d\sigma^{+-++}|_{\substack{1 \leftrightarrow 2 \\ 1' \leftrightarrow 2'}}, \quad (CP + \text{Bose}) \\ d\sigma^{++--} &= d\sigma^{+-++}|_{\substack{k \leftrightarrow 2 \\ 1' \leftrightarrow 2'}}, \quad (C + \text{crossing}) \\ d\sigma^{++--} &= d\sigma^{++--}|_{1' \leftrightarrow 2'}, \quad (C) \\ d\sigma^{-\lambda_1, -\lambda_2, -e_1', -e_2', -\lambda_3} &= d\sigma^{\lambda_1, \lambda_2, e_1', e_2', \lambda_3}. \quad (P) \end{aligned}$$

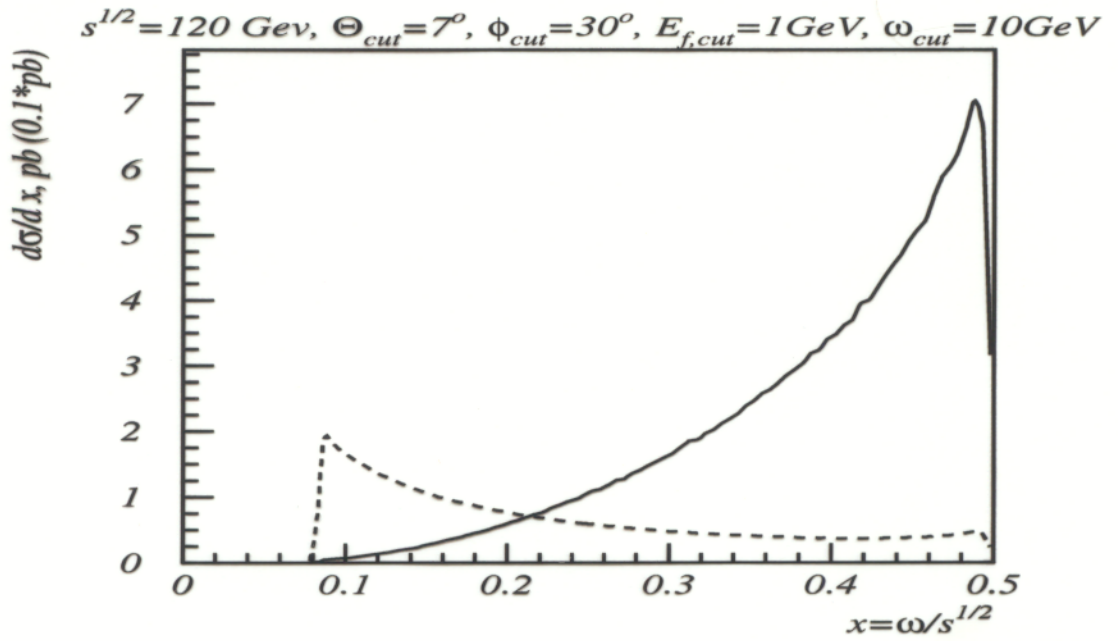
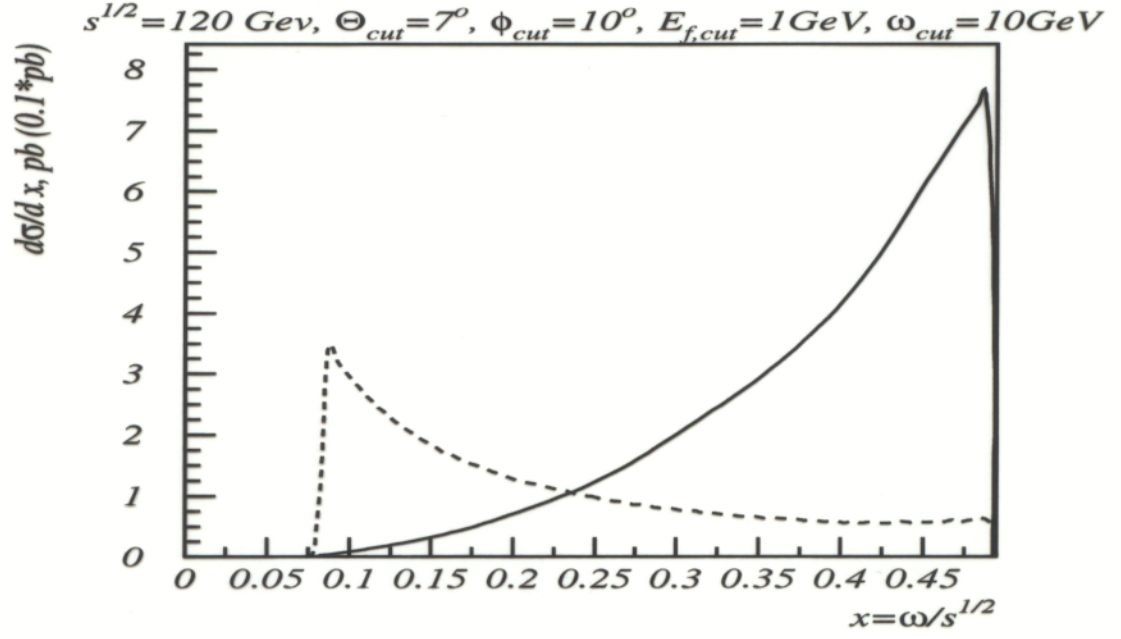
Phase space integration is performed numerically using the Monte-Carlo method.



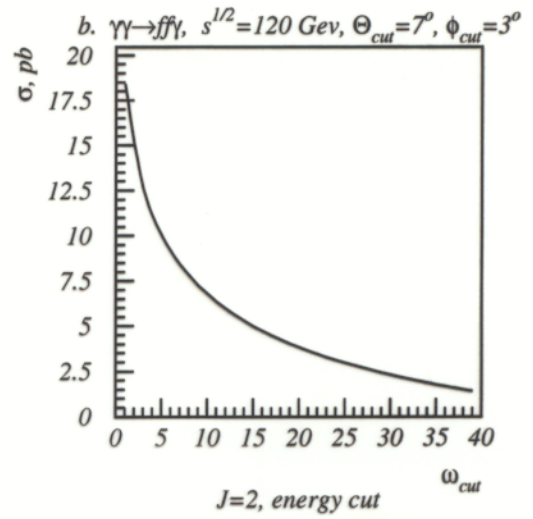
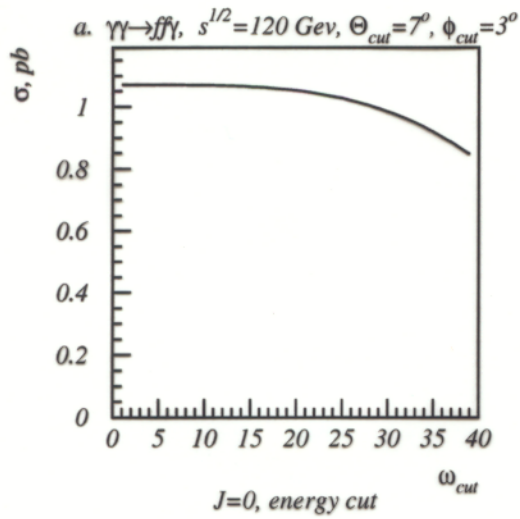
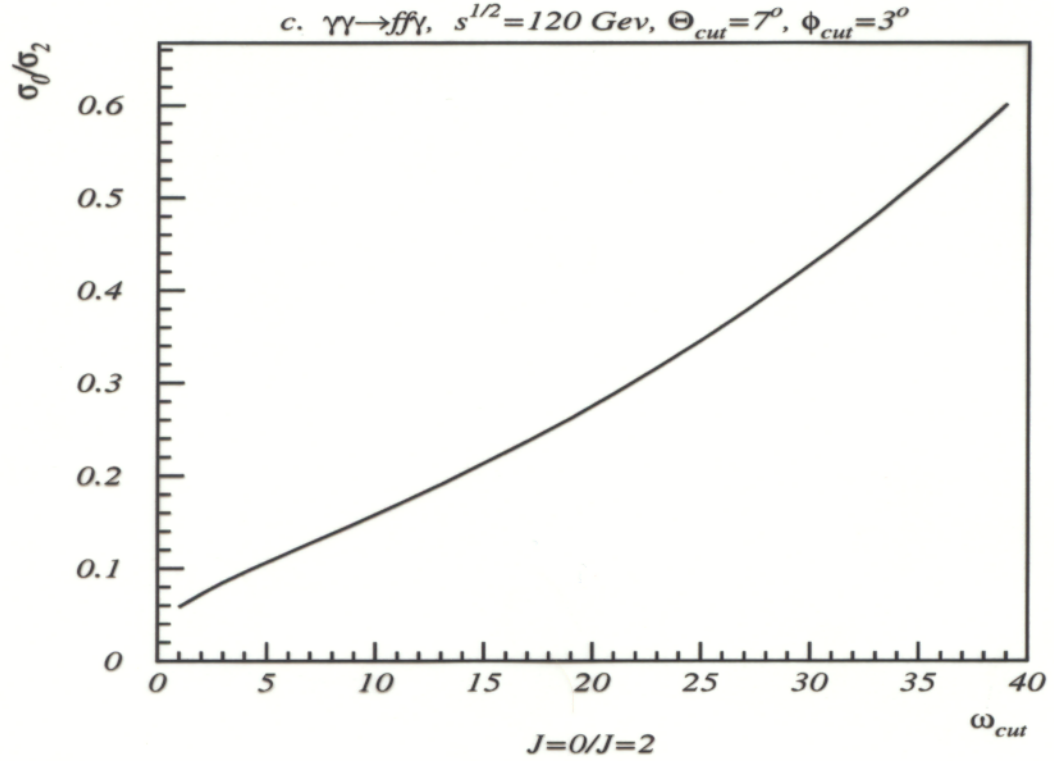
Final-stage photon spectrum: $J=0$ (dotted) and $(J=2) * 0.1$ (solid) at $\sqrt{s} = 120 \text{ GeV}$ and $\sqrt{s} = 500 \text{ GeV}$.

Cuts: $\Theta_{\text{min}} = 7^\circ$; $\varphi_{\text{min}} = 3^\circ$; $E_{f,\text{min}} = 1 \text{ GeV}$; $\omega_{\text{min}} = 1 \text{ GeV}$.

Final-stage photon spectrum: $J=0$ (solid) and $(J=2) * 0.1$ (dotted) at $\sqrt{s} = 120\text{GeV}$.

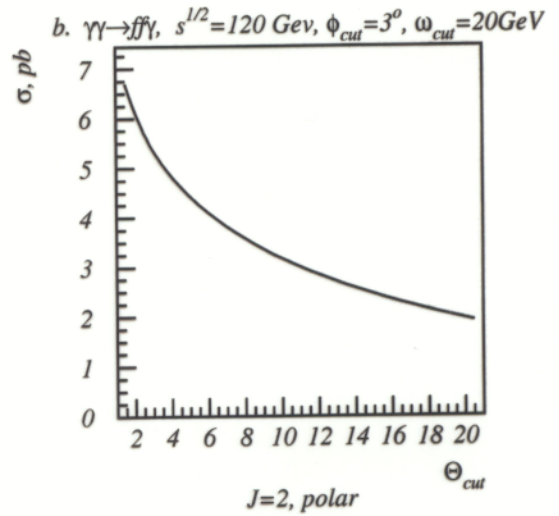
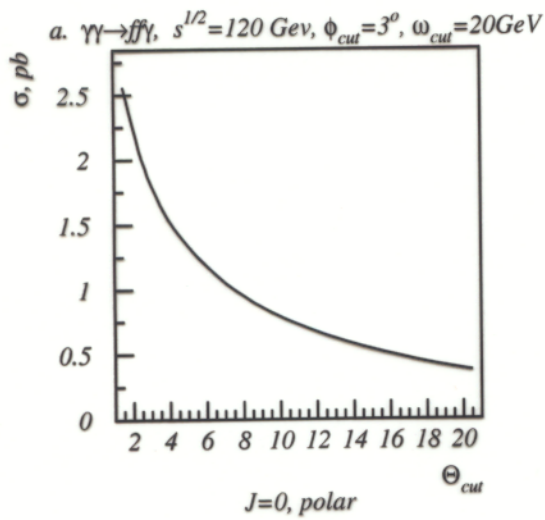
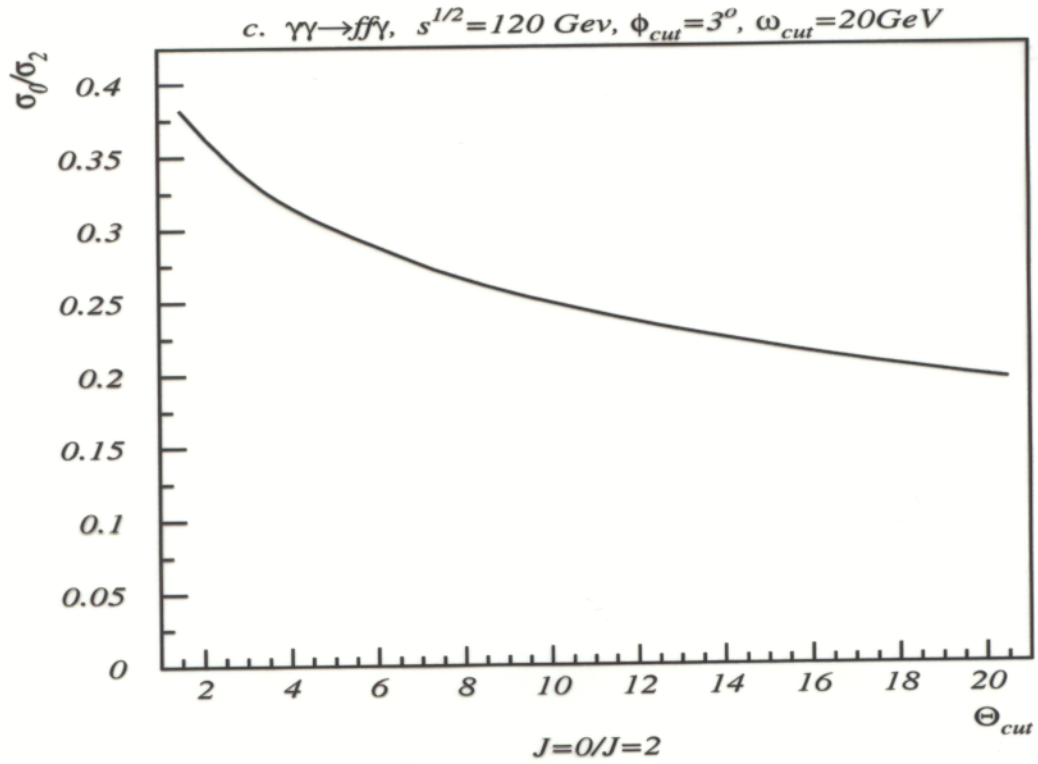


Total cross sections on $J=0$ and $J=2$ beams and their ratio.
Dependence on w_{cut} .



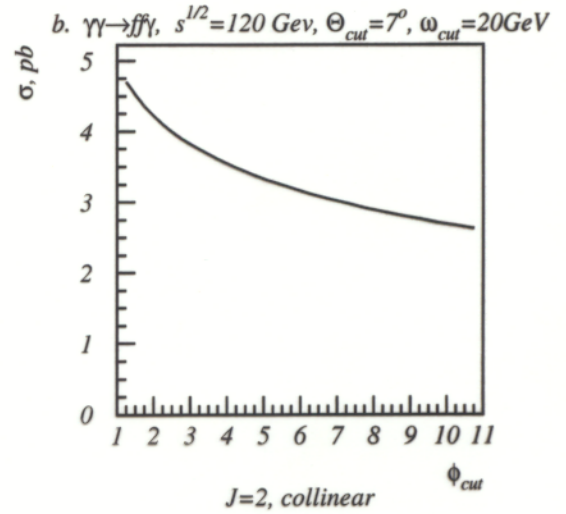
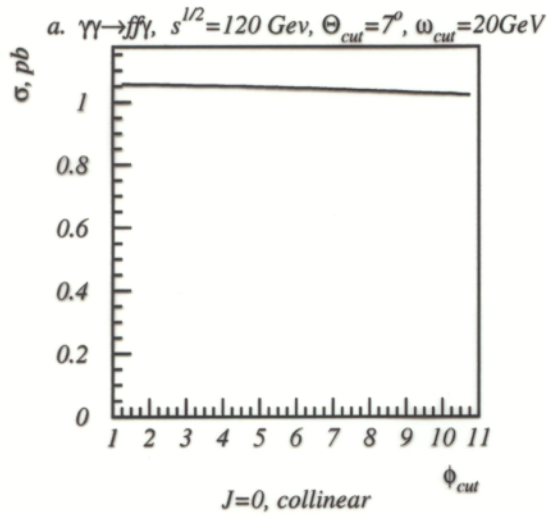
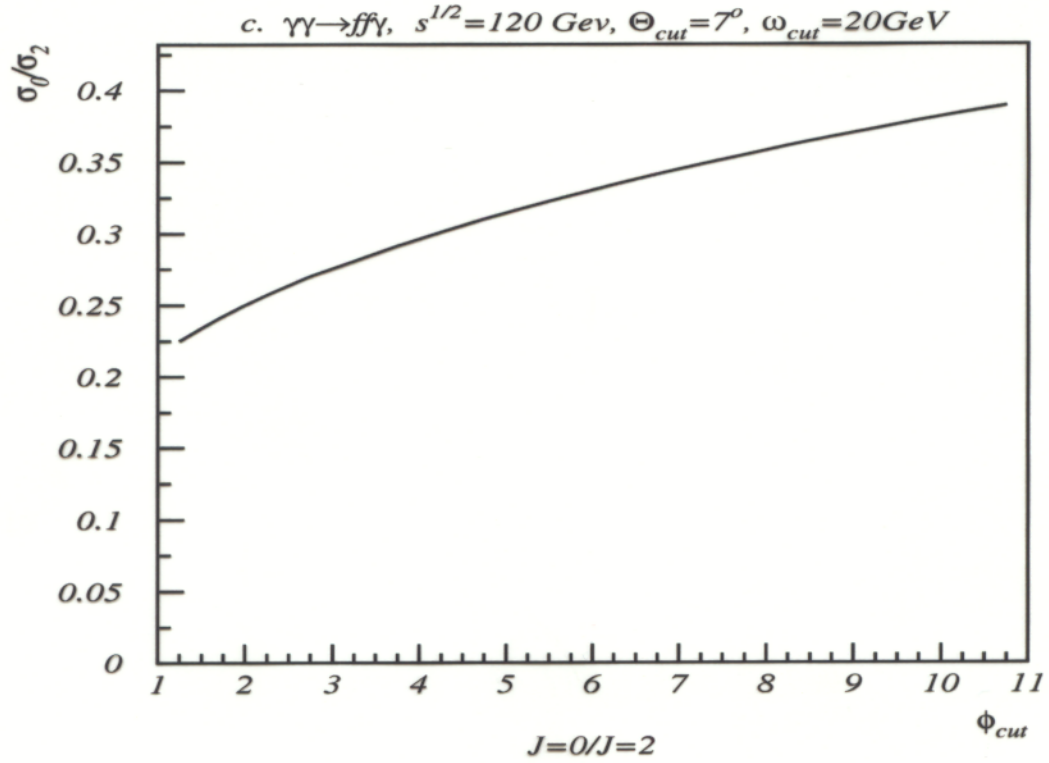
The rise of threshold on the final photon energy greatly restricts the $J=2$ -cross section, the $J=0$ reaction is almost unaffected.

Total cross section ratio $J=0/J=2$. Dependence on Θ_{cut} .

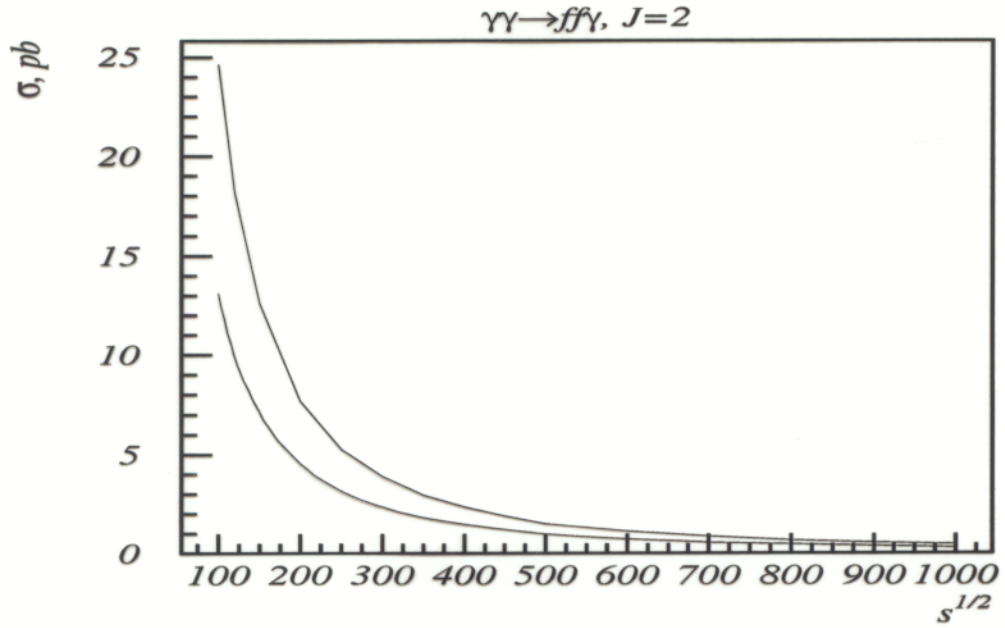
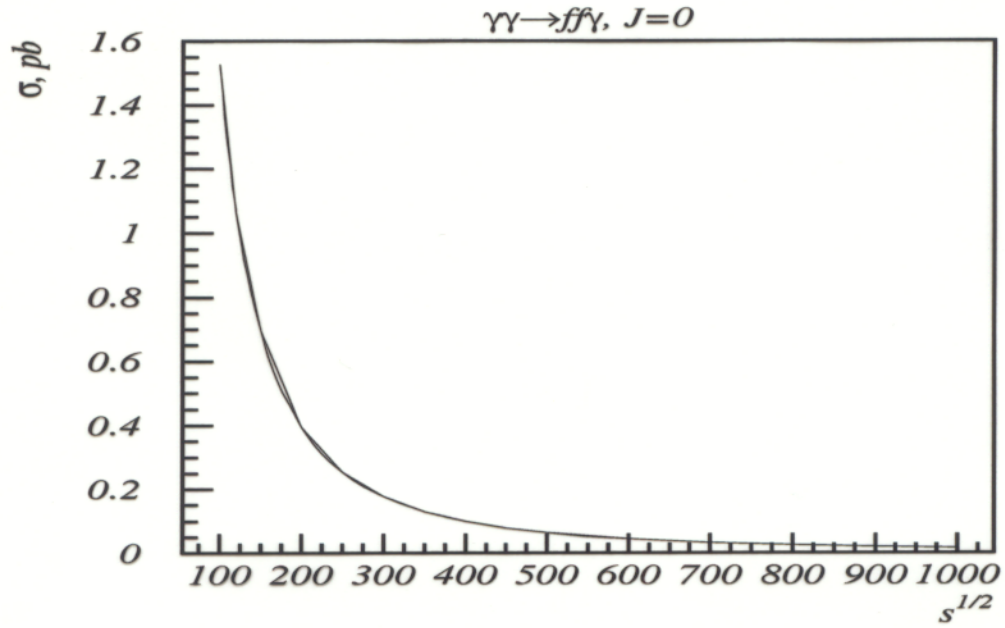


The decrease of threshold on polar angle leads to rise of ratio $J=0/J=2$, increasing both the cross sections.

Total cross section ratio $J=0/J=2$. Dependence on φ_{cut} .

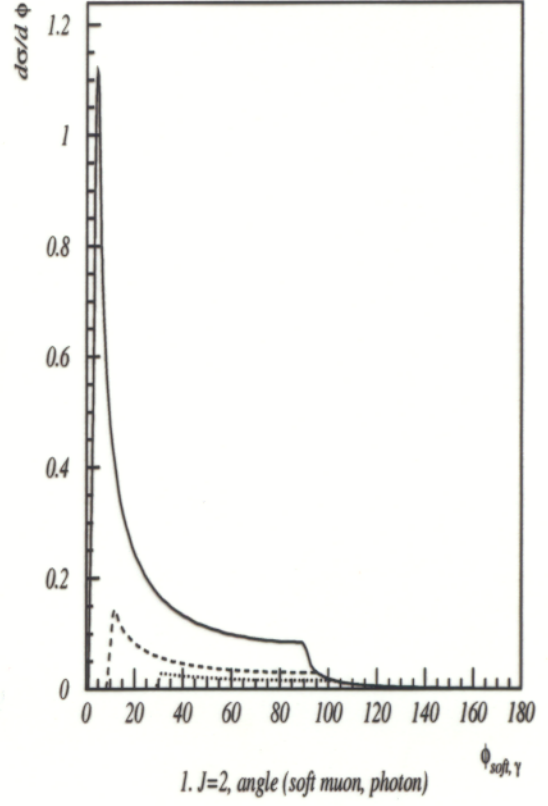
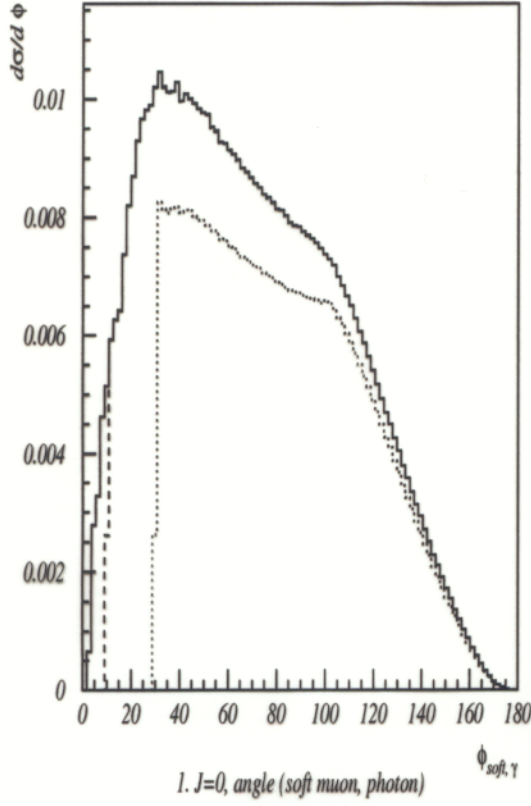


The rise of threshold on angle between final particles restricts the $J=2$ -cross section, the $J=0$ reaction is almost unaffected.



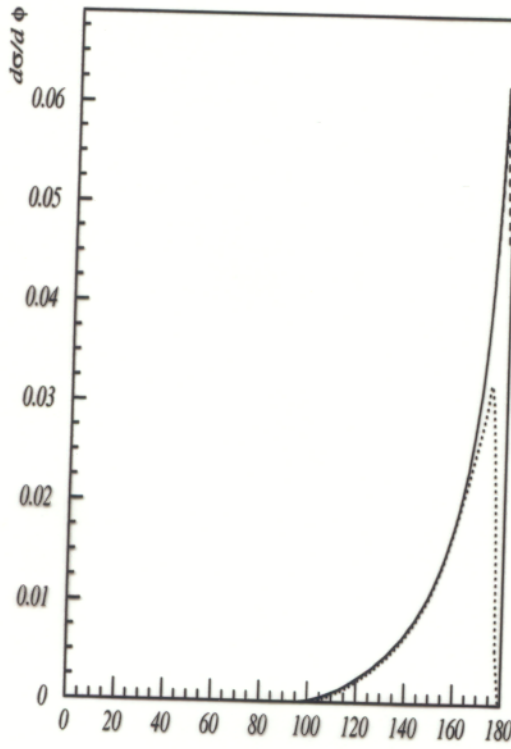
The dependence of total cross section on the c.m.s. energy.

Cuts: $\Theta_{cut} = 7^\circ$, $\varphi_{cut} = 3^\circ$, $E_{f,cut} = 1\text{GeV}$, $w_{cut} = 1\text{GeV}$ (the higher line)
and $w_{cut} = 5\text{GeV}$ (the lower line).

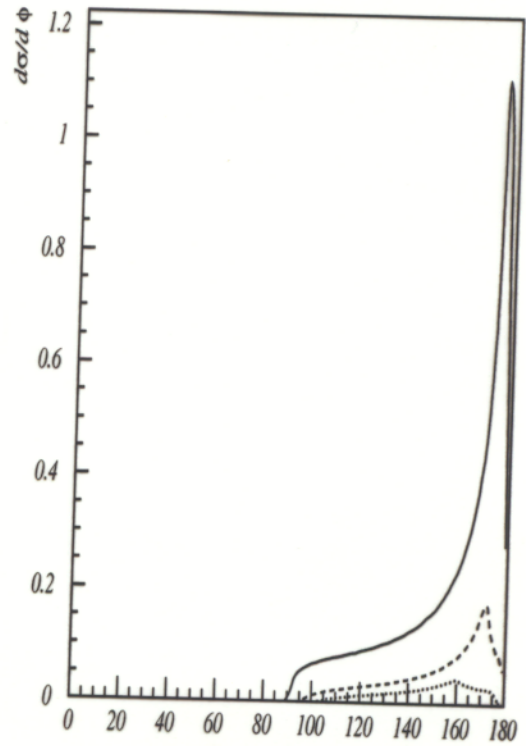


Angular plots (angle between fermion with lowest energy and final photon) at set of cuts:

1. $\Theta_{min} = 7^\circ$; $\varphi_{min} = 3^\circ$; $E_{f,min} = 1\text{GeV}$; $\omega_{min} = 1\text{GeV}$;
2. $\Theta_{min} = 7^\circ$; $\varphi_{min} = 10^\circ$; $E_{f,min} = 1\text{GeV}$; $\omega_{min} = 10\text{GeV}$;
3. $\Theta_{min} = 7^\circ$; $\varphi_{min} = 30^\circ$; $E_{f,min} = 5\text{GeV}$; $\omega_{min} = 20\text{GeV}$.



1. $J=0$, angle (hard muon, photon)



1. $J=2$, angle (hard muon, photon)

Angular plots (angle between fermion with highest energy and final photon) at set of cuts:

1. $\Theta_{min} = 7^\circ$; $\varphi_{min} = 3^\circ$; $E_{f,min} = 1\text{GeV}$; $\omega_{min} = 1\text{GeV}$;
2. $\Theta_{min} = 7^\circ$; $\varphi_{min} = 10^\circ$; $E_{f,min} = 1\text{GeV}$; $\omega_{min} = 10\text{GeV}$;
3. $\Theta_{min} = 7^\circ$; $\varphi_{min} = 30^\circ$; $E_{f,min} = 5\text{GeV}$; $\omega_{min} = 20\text{GeV}$.

Precision of luminosity measurement using the reaction $\gamma\gamma \rightarrow f\bar{f}\gamma$.

We choose the set of cuts $E_\mu > 5\text{GeV}$, $E_\gamma > 20\text{GeV}$, $\Theta_{cut} = 6^\circ$, $\varphi_{cut} = 30^\circ$ and the corresponding cross sections:

$$\begin{aligned}\sigma(J=0) &= 0.82\text{pb} \\ \sigma(J=2) &= 1.89\text{pb}\end{aligned}$$

TESLA luminosity:

$$\begin{aligned}\mathcal{L}(\sqrt{s'} > 0.8\sqrt{s'_{\max}}) &= 5.3 \cdot 10^{33}\text{cm}^{-2}\text{s}^{-1} \\ \mathcal{L}(m_H \pm 1\text{GeV}) &= 3.8 \cdot 10^{32}\text{cm}^{-2}\text{s}^{-1}\end{aligned}$$

with $\mathcal{P} \approx 90\%$

$\Rightarrow$ in a 2 years run ($2 \cdot 10^7\text{s}$):

$$\begin{aligned}\frac{\Delta\mathcal{L}}{\mathcal{L}}(\sqrt{s'} > 0.8\sqrt{s'_{\max}}) &= 0.35\% \\ \frac{\Delta\mathcal{L}}{\mathcal{L}}(m_H \pm 1\text{GeV}) &= 1.3\%\end{aligned}$$

ω_{cut}, GeV	$E_{f,cut}, GeV$	$\Theta_{cut}, ^\circ$	$\varphi_{cut}, ^\circ$	$\sigma_{J=0}, pb$	$\sigma_{J=2}, pb$
1	1	5	3	1.368	21.911
1	1	7	3	1.073	18.353
1	1	10	3	0.799	15.713
1	1	7	5	1.066	15.807
1	1	7	10	1.044	12.488
1	1	7	30	0.881	7.150
10	1	7	3	1.070	6.769
10	1	7	10	1.045	4.682
10	1	7	30	0.880	2.842
10	1	5	10	1.314	5.485
10	1	10	10	0.783	3.848
20	1	7	3	1.052	3.820
20	1	7	10	1.026	2.690
20	5	7	3	0.892	3.623
20	5	7	10	0.873	2.559
20	5	5	30	0.898	1.903
20	5	7	30	0.748	1.629
20	5	10	30	0.587	1.327

very useful
to measure
luminosity
of $J=0$

Total cross sections for $\gamma\gamma \rightarrow f\bar{f}\gamma$ for different cuts at $\sqrt{s} = 120GeV$.

Conclusion: Using detector limitations we can greatly restrict the process on $J=2$ -beams remaining the process on $J=0$ almost unchanged.