Related topics

Electric field, field intensity, electric flow, electric charge, Gaussian rule, surface charge density, induction, induction constant, capacitance, gradient, image charge, electrostatic potential, potential difference.

Principle and task

Conducting spheres with different diameters are charged electrically. The static potentials and the accompanying electric field intensities are determined by means of an electric field meter with a potential measuring probe, as a function of location and voltage.

Equipment

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Electric field meter	11500.10	1
Potential probe	11501.00	1
Capacitor plate w.hole d 55 mm	11500.01	1
High voltage supply unit, 0-10 kV	13670.93	1
Conductor ball, d 20 mm	06236.00	1
Conductor ball, d 40 mm	06237.00	1
Conductor ball, d 120 mm	06238.00	1
High-value resistor, 10 MOhm	07160.00	1
Insulating stem	06021.00	2
Power supply 0-12 V DC/6 V, 12 V AC	13505.93	1
Multi-range meter A	07028.01	1
Barrel base -PASS-	02006.55	3
Stand tube	02060.00	1
Tripod base -PASS-	02002.55	1
Meter scale, demo, l = 1000 mm	03001.00	1
Rubber tubing, i.d. 7 mm	39282.00	1
Butane burner, Labogaz 206 type	32178.00	1
Butane cartridge	47535.00	2
Connecting cord, 50 KV, 500 mm	07366.00	1
Connecting cord, 750 mm, red	07362.01	3
Connecting cord, 750 mm, blue	07362.04	2
Connecting cord, 750 mm, green-yell	07362.15	2
Connecting cord, 250mm, green-yell	07360.15	2

Problems

1. For a conducting sphere of diameter 2R = 12 cm, electro-static potential is determined as a function of voltage at a constant distance from the surface of the sphere.

2. For the conducting spheres of diameters 2R = 12 cm and 2R = 4 cm, electrostatic potential at constant voltage is determined as a function of the distance from the surface of the sphere.

3. For both conducting spheres, electric field strength is determined as a function of charging voltage at three different distances from the surface of the sphere.

4. For the conducting sphere of diameter 2R = 12 cm, electric field strength is determined as a function of the distance from the surface of the sphere at constant charging voltage.

Set-up and procedure

Part 1 : Coulomb potential.

The experimental set-up is shown in Fig.1a. The voltage measuring attachment should be mounted on the electric field meter, to which the potential measuring probe is attached. The attachment and the electric field meter must be earthed. The glass rod of the potential measuring probe is connected to the burner with rubber tubing. The burner must be adjusted in such a way that a flame of approx. 5 mm burns over the tip of the probe. This assures ionisation of the air over the tip of the probe, in order to have a volume of conductive air before the probe tip.

Fig.1a: Experimental set-up used to determine the Coulomb potential.
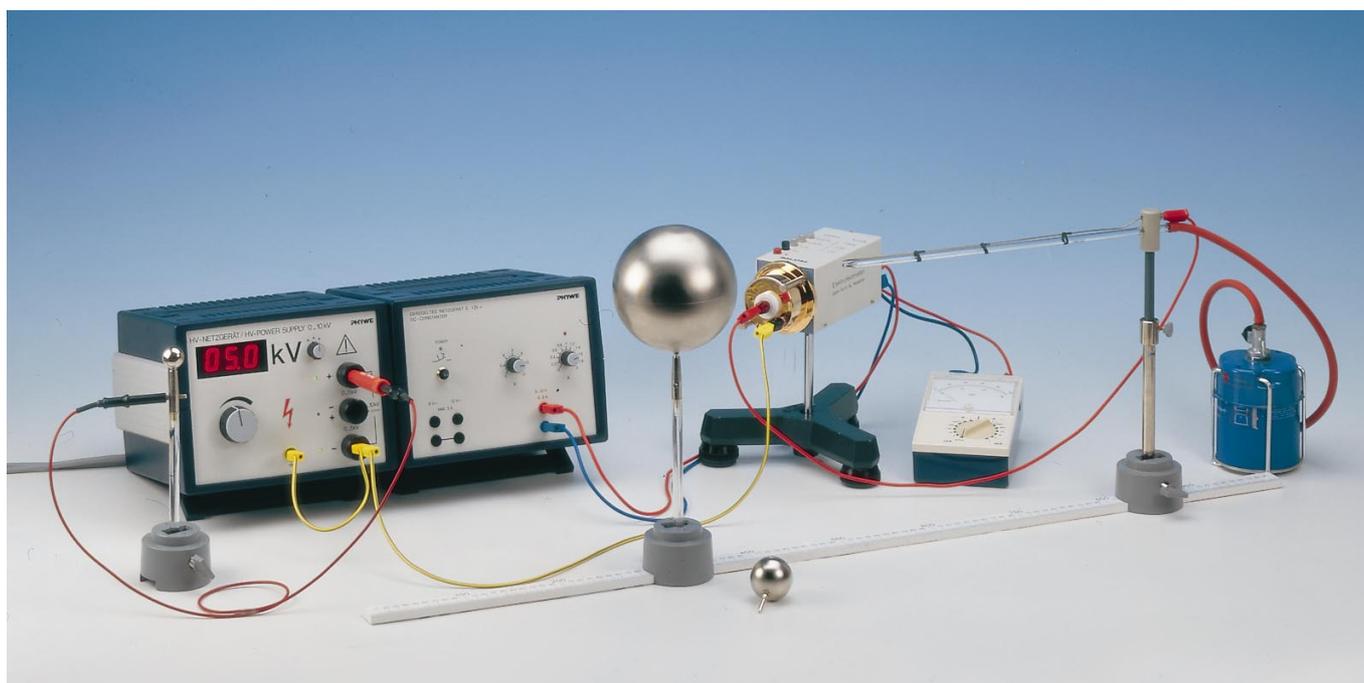
The conducting spheres, which are held on insulating supports, are connected to the positive pole of the high voltage power supply by means of a high voltage cable, over the 10 MΩ safety resistor. The negative pole of the power supply is earthed.

To begin with, the electrostatic potential of a charged sphere is determined as a function of voltage. This is done by applying voltages in steps of 1kV up to maximum of 5kV to the sphere with diameter 2R = 12 cm. During this procedure, the measuring probe should be situated about 25 cm from the surface of the sphere.

To determine the potential as a function of the distance from the centre of the sphere, a 1000 V steady voltage is applied to the sphere with 2R = 12 cm. This voltage can be measured directly with the electric field meter, the probe tip of which touches the surface of the sphere. At the beginning, the height adjusted tip of the measuring probe is situated 1 cm from the surface of the sphere. The potential is then measured for steps of 1 cm. Measurement is repeated for the conducting sphere of 2R = 4 cm.

Part 2 : Coulomb field

The experimental set-up is modified according to Fig 1b. The conducting sphere (2R=2cm), held on an insulated support, is connected to the positive pole of the high voltage power supply, as described above, in order to charge the test spheres. The height of the electric field meter with attached capacitor plate is adjusted by means of the clamp stand, so that its axis lies in the equator plane of the test sphere. The stem of the electric field meter is earthed again.

To determine field strength as a function of the charging voltage, the surface of the conducting sphere of 2R = 12 cm is placed successively at distances $r_1 = 25$ cm , $r_2 = 50$ cm and $r_3 = 75$ cm of the electric field meter capacitor plate.

The test sphere is charged to a maximum voltage of 10 kV in steps of 1 kV. After every charging procedure, the high voltage is to be set back to zero volts; after every measurement, the test sphere is to be discharged by briefly touching it with the earth lead. The measurement series is repeated with the 2R = 4 cm sphere for r = 25 cm.

To determine field strength as a function of distance r from the centre of the sphere, conducting sphere 2R = 12 cm is charged to 10kV and the electric field meter is set up in steps of 5 cm from the surface of the sphere.

After charging, high voltage is to be reset to zero, in order to avoid disturbing influences.

Theory and evaluation

At a distance r of its surface, the electric potential of a charged conducting sphere is:

$$\varphi(r) = \frac{1}{4\pi\varepsilon_0} \frac{Q}{r} \qquad (1)$$

(Q= electric charge; ε_0 = induction constant)
If the capacitance of the sphere is C and its radius R, charge Q at voltage U is given by:

$$Q = CU = 4\pi \varepsilon_0 \cdot R \cdot U \qquad (2)$$

Introducing (2) into (1) yields the following relation:

$$\varphi(r) = \frac{R}{r} U \qquad (3)$$

According to (3), Fig. 2 shows the linearity of potential $\varphi = \varphi(U)$ for r = const. = 18 cm, as measured on the conducting sphere with 2R = 12 cm.

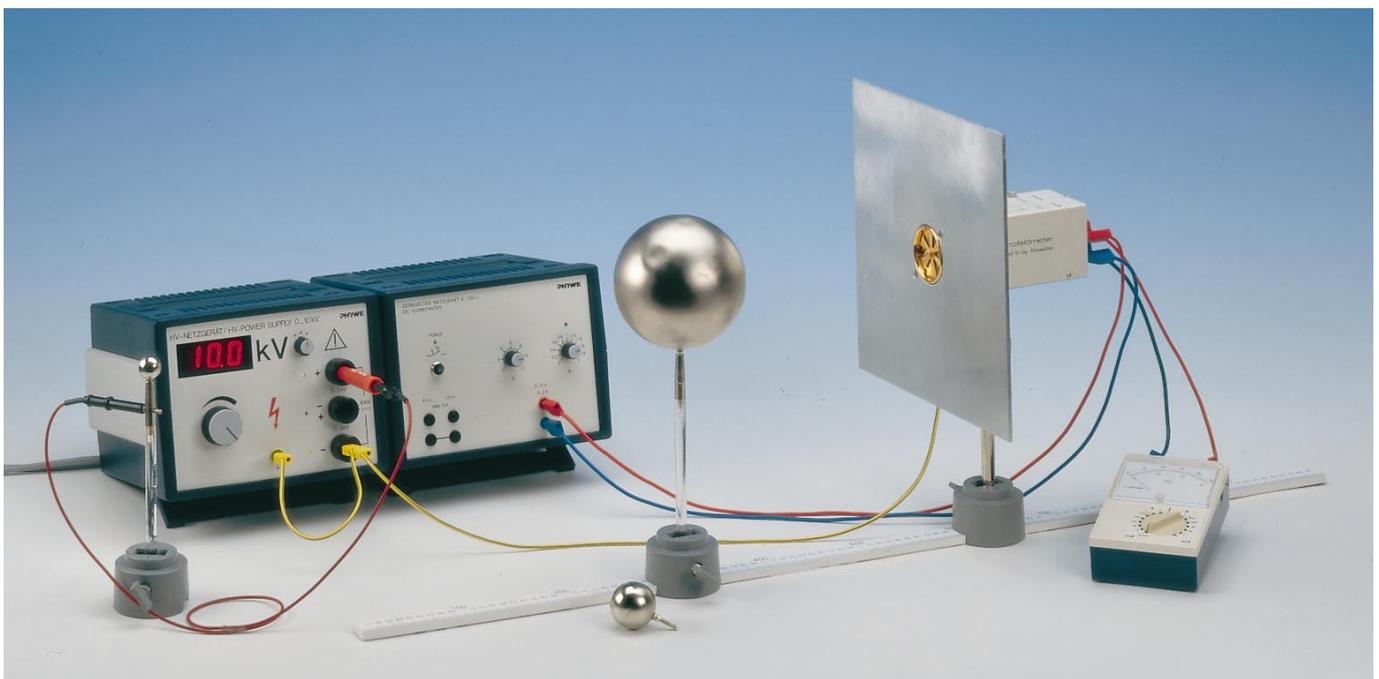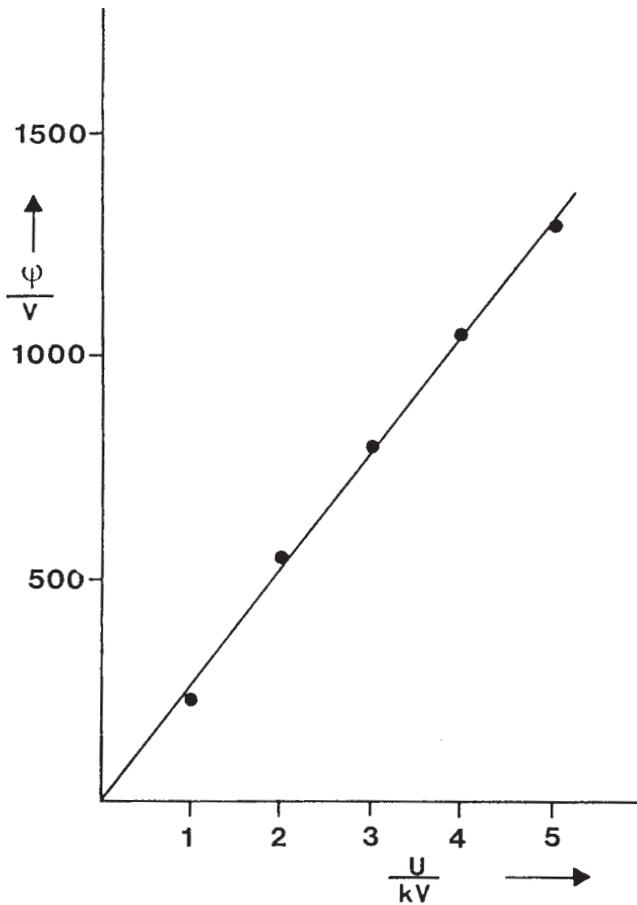Fig.1b: Experimental set-up to determine the Coulomb field.

Fig. 2 : Potential φ as a function of voltage U.

In Fig. 3 , φ is plotted against r on a double logarithmic scale, r being measured from the centre of the sphere. Fig. 3a shows the result of measurement on the conducting sphere with diameter 2R = 12 cm, Fig.3b displays the corresponding result for the sphere with diameter 2R = 4 cm. The voltage applied to the spheres was 1000 V each time. In both cases, the slope of the straight line was m $\cong$ –1, in agreement with (4); this is thus the experimental proof of the 1/r-dependence of the electric potential. For points situated near the surface of the spheres, non-linear measurement values were found, due to the influence of the flame on the tip of the probe.

If the potential field $\varphi(r)$ is known, the electric Coulomb field E for a charge Q is obtained from the negative gradient of the potential:

$$E = -\,grad\ \varphi\ = -\,d\varphi\,/\,dr = \frac{1}{4\pi\varepsilon_0}\ \frac{Q}{r^2} \qquad (5)$$

To determine the field strenght, a capacitor plate is placed before the electric field meter in order to obtain a spatially undistorted field distribution. This is shown schematically in Fig 4. An image charge is obtained inductively by means of the plate, so that the plate is situated centrally between the real and the virtual charge. The charge Q in (5) must thus be multiplied by 2.

Replacing the value of Q in (5) by (2) and considering the doubling of the charge, the following holds true:

$$E = \frac{2R}{r^2} \cdot U \qquad (6)$$

The measured field strength E is plotted as a function of voltage U in Fig. 5.

A comparison of the slope $\Delta E/\Delta U$ of the straight lines with the corresponding quotients $2R/r2$ yields the following pairs of values which agree satisfactorily:

graph 1: $\Delta E/\Delta U$ = 1,44 m^{-1}, $2R/r^2$ = 1,25 m^{-1}
graph 2: $\Delta E/\Delta U$ = 0,44 m^{-1}, $2R/r2$ = 0,38 m^{-1}
graph 3: $\Delta E/\Delta U$ = 0,18 m^{-1}, $2R/r^2$ = 0,18 m^{-1}
graph 4: $\Delta E/\Delta U$ = 0,58 m^{-1}, $2R/r^2$ = 0,55 m^{-1}.

Calculating the logarithm of (3), one obtains:

$$\log \varphi = -\log r + \log R + \log U = -\log r + k \quad (4)$$

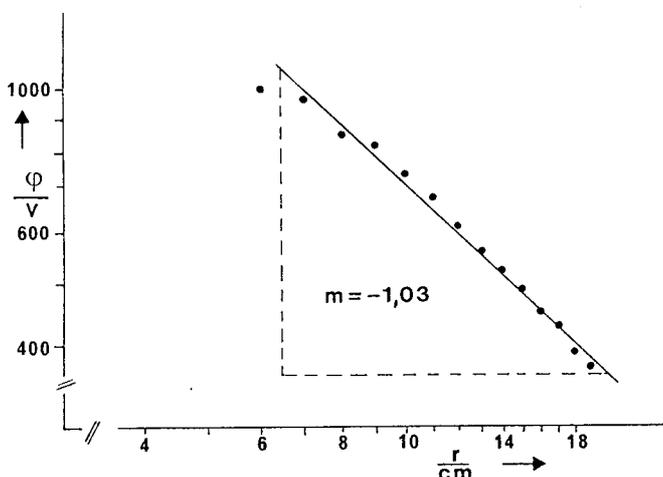if U and R are constant. (Straight line with slope m = -1).

Fig. 3: Potential φ as a Function of distance r represented in double logarithmic scale.
Fig. 3a: Sphere with 2r = 12cm;

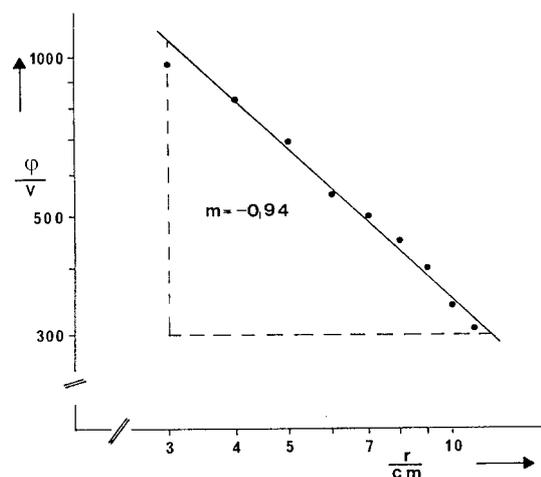Fig. 3b: Sphere with 2r 0 = 4cm.
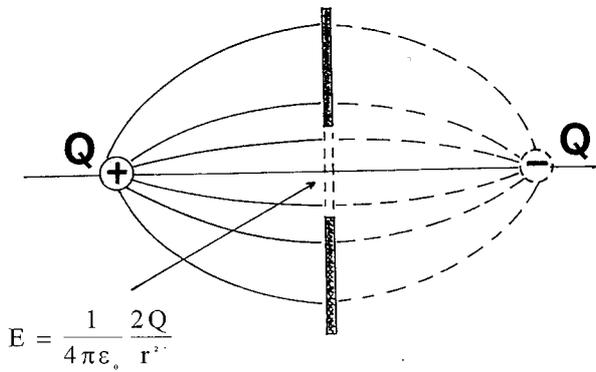
Fig. 4: Field geometry with induced image charge.

$$E = \frac{1}{4\pi\varepsilon_0}\frac{2Q}{r^2}$$

Fig. 6: Field strength E as a function of distance r in double logarithmic scale.
Sphere with 2R = 12cm.

$m = -2{,}06$

In Fig. 6, field strenght E, measured on the sphere with radius 2R = 12 cm charged at 10kV, is plotted on a double logarithmic scale as a function of distance r.
The slope of the straight line is m = –2,06. This means that the field strenght is inversely proportional to the square of the distance.
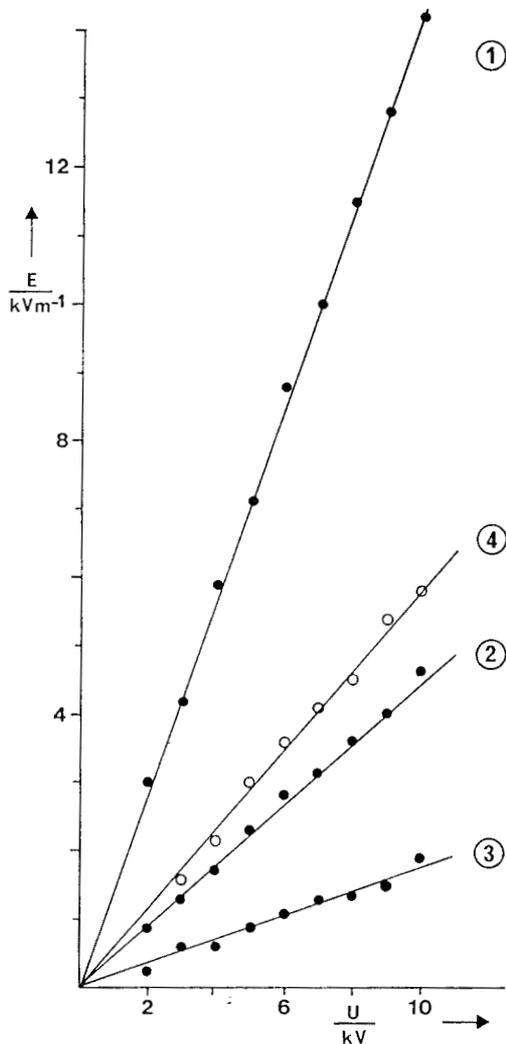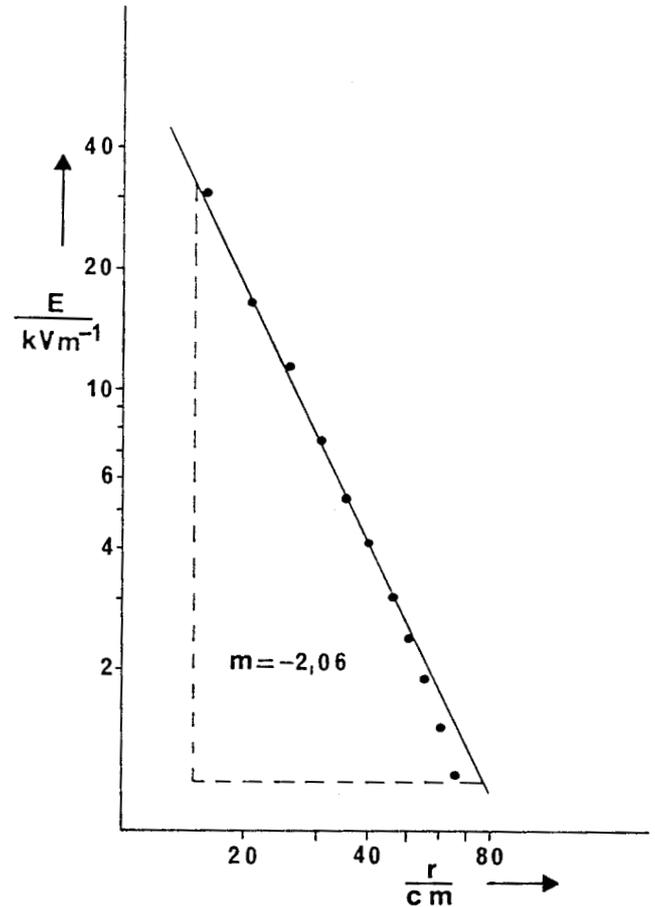

Fig. 5: Field strenght as a function of voltage.
Graphs 1-3 : sphere with 2R = 12cm; r_1 = 25cm, r_2 = 50cm, r_3 = 75 cm;
graph 4: sphere with 2R = 4cm; r_1 = 25 cm.